

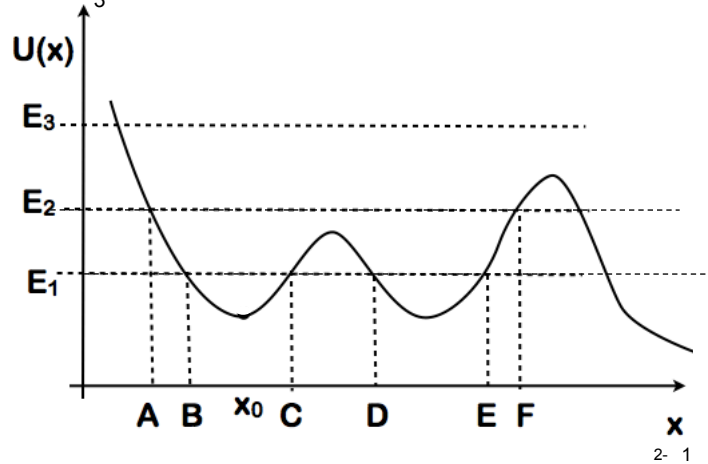
Which statements are true about a particle located at x_0 ?

I- If it has energy E_1 , it can move between B and E

II- If it has energy E_2 it is bounded between A&F, it cannot escape

III- A particle with E_3 is unbounded

- A) All
- B) II only
- C) III only
- D) I&II
- E) II&III



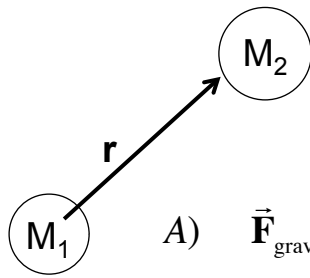
Summary from last class:

- 1-D systems, $U(x)$ yields $F(x) = -dU/dx$

- Equilibrium when $U'(x) = 0$

- Stable Equilibrium if $U''(x) > 0$

- Plots of $U(x)$ vs x give us immediate information (about binding, motion, $v(x)$, $v(t)$, equilibrium, ...)



What is the force of gravity on (pointlike) M_2 caused by (pointlike) M_1 ?

A) $\vec{\mathbf{F}}_{\text{grav}} = -G \frac{M_1 M_2}{r^2} \hat{r}$

B) $\vec{\mathbf{F}}_{\text{grav}} = +G \frac{M_1 M_2}{r^2} \hat{r}$

C) $\vec{\mathbf{F}}_{\text{grav}} = -G \frac{M_1 M_2}{r^3} \vec{r}$

D) $\vec{\mathbf{F}}_{\text{grav}} = +G \frac{M_1 M_2}{r^3} \vec{r}$

E) None of these or MORE than one of these!!

2- 3

GRAVITY

- Newton's law of gravity
- Gravitational force (direct integration)
- gravitational field
- Symmetry and Invariance arguments
- gravitational potential, and PE

2- 4

A “little man” is standing a height z above the origin. There is an infinite line of mass (uniform density) lying along the x -axis.

Which *components* of the local \mathbf{g} field can little man argue against *just by symmetry alone*?

- A. ONLY that there is no g_x
- B. ONLY that there is no g_y
- C. ONLY that there is no g_z
- D. ONLY that there is neither g_x nor g_y
- E. That there is neither g_x , g_y , nor g_z

2- 5

A “little man” is standing a height z above the origin. There is an infinite line of mass (uniform density) lying along the x -axis.

He has already decided $\vec{g}(x,y,z) = g_z(x,y,z) \hat{\mathbf{k}}$

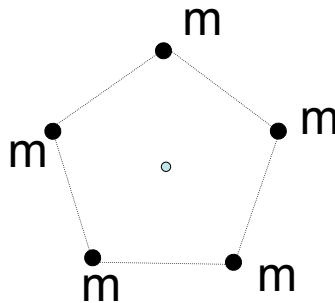
Which *dependences* of the local $g_z(x,y,z)$ field can he argue against, *just by symmetry alone*!

- A. ONLY that there is no x dependence, i.e. only that $\vec{g}(x,y,z) = g_z(y,z) \hat{\mathbf{k}}$
- B. ONLY that there is no y dependence
- C. ONLY that there is no z dependence
- D. ONLY that there is neither x nor y dependence
- E. That there is neither x , y , nor z dependence.

2- 6

^{2.5} 5 masses, m , are arranged in a regular pentagon, as shown.

What is the g field at the center?



- A) Zero
- B) Non-zero
- C) Really need trig and a calculator to decide

2-

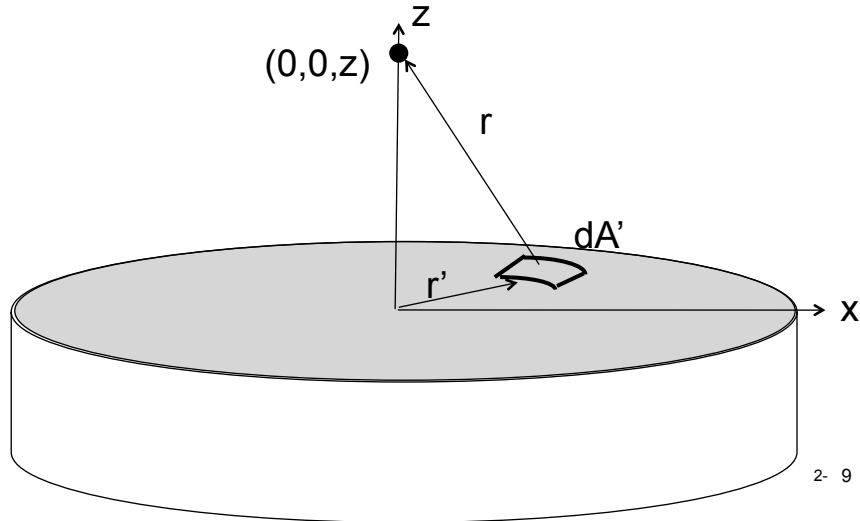
Force, potential energy, gravitational potential, gravitational acceleration

- What is the practical difference between \vec{F} , U , \vec{g} , and Φ ?
 - A. U and Φ are fields while \vec{F} and \vec{g} are not.
 - B. They have different masses.
 - C. \vec{F} , U depend on both masses, while \vec{g} , and Φ depend on only one mass.
 - D. \vec{F} and \vec{g} are easier to calculate.
 - E. U and Φ are energies, while \vec{F} and \vec{g} are forces.

2-

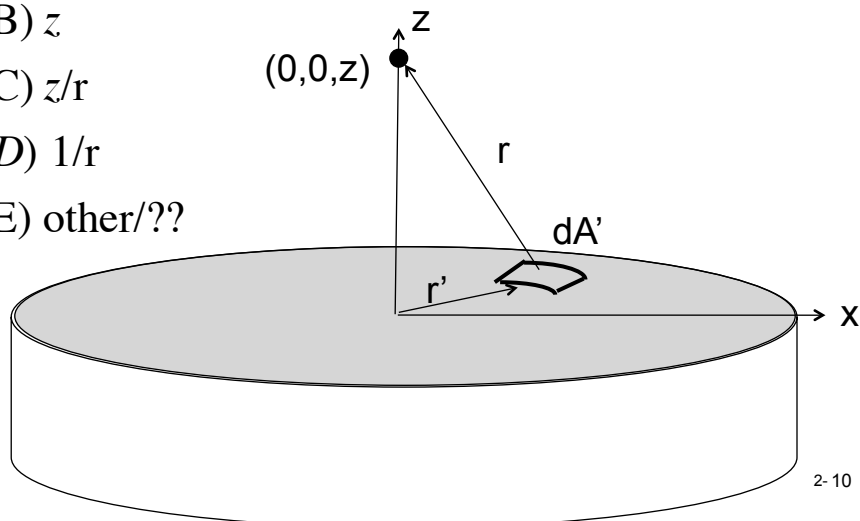
For \vec{g} along the z-axis above a massive disk, we need

$$(\vec{g})_z = -G \iiint \frac{\rho(r')}{r^2} (\hat{r})_z dV' = -G \iint_{\text{disk}} \frac{1}{r^2} (\hat{r})_z \sigma dA'$$



$$(\vec{g})_z = -G \iint_{\text{disk}} \frac{1}{r^2} (\hat{r})_z \sigma dA' \quad \text{What is } (\hat{r})_z = ?$$

- A) 1
- B) z
- C) z/r
- D) $1/r$
- E) other/??



$$(\vec{g})_z = -G\sigma \iint_{disc} \sigma \frac{z}{r^3} dA' \quad \text{What is } \frac{1}{r^3} = ?$$

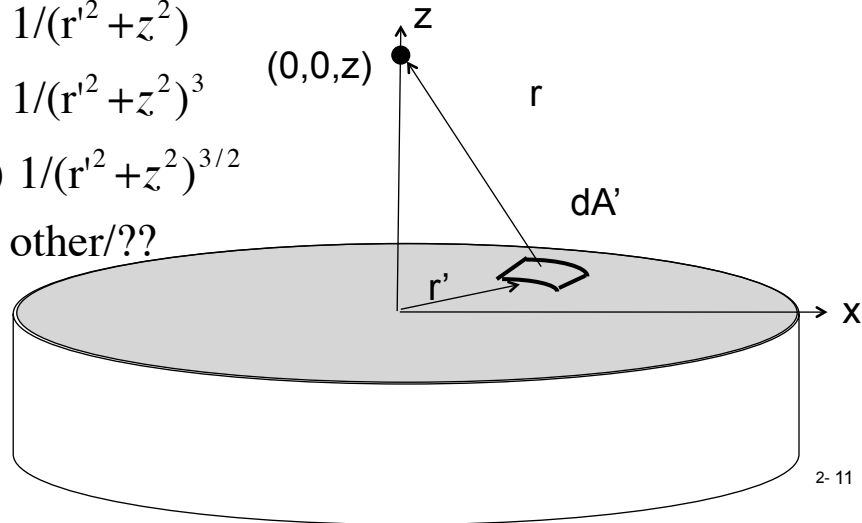
A) $1/(r'^3 + z^3)$

B) $1/(r'^2 + z^2)$

C) $1/(r'^2 + z^2)^3$

D) $1/(r'^2 + z^2)^{3/2}$

E) other/??



2.16

Above the disk, $g_z(0,0,z)=$

$$(\vec{g})_z = +2\pi G\sigma z \left[\frac{1}{\sqrt{a^2 + z^2}} - \frac{1}{z} \right] \quad (\text{if } z > 0)$$

If $z \gg a$, let's Taylor expand. What should we do first?

2-

Above the disk, $g_z(0,0,z)=$

$$(\vec{g})_z = +2\pi G\sigma z \left[\frac{1}{\sqrt{a^2 + z^2}} - \frac{1}{z} \right] \quad (\text{if } z > 0)$$

If $z \gg a$, let's Taylor expand. What should we do first?

A) Find d/dz of this whole expression, and evaluate it at $z=0$

B) Rewrite $\frac{1}{\sqrt{a^2 + z^2}} = \frac{1}{a\sqrt{1+(z/a)^2}}$ and then use the "binomial" expansion $(1+\varepsilon)^n \approx (1+n\varepsilon+\dots)$

C) Rewrite $\frac{1}{\sqrt{a^2 + z^2}} = \frac{1}{z\sqrt{1+(a/z)^2}}$ and then use the "binomial" expansion.

D) Just expand $(a^2 + z^2)^{-1/2} \approx a^{-1/2} - (1/2)z^2/a^{5/2} + \dots$

2-

Summary

$$\vec{F}_{\text{grav, points}} = -G \frac{M_1 M_2}{r^2} \hat{r}$$

$$\vec{F}_{\text{grav, M2 a point}} = -G \iiint_{V'} \frac{\rho(r')}{r^2} dV' \hat{r}$$

$$\vec{g} = \vec{F}_{\text{grav, on point m}} / m$$

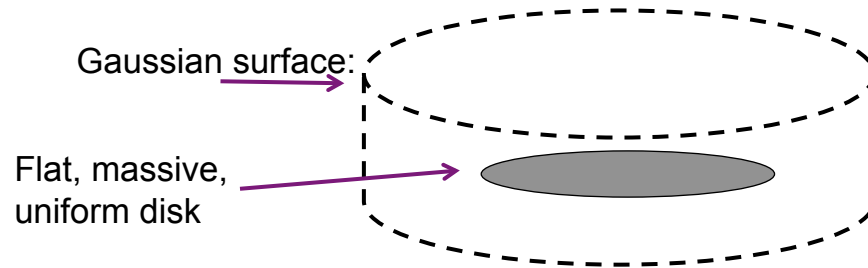
$$\text{PE : } U(r)_{\text{for point M2 near point M1}} = -G \frac{M_1 M_2}{r}$$

$$\text{Grav. potential : } \Phi(r)_{\text{near point M1}} = -G \frac{M_1}{r}$$

$$\text{Gauss'law : } \oiint \vec{g} \cdot d\vec{A} = -4\pi G M_{\text{enclosed}}$$

2-14

For the example of the uniform disk, could we have used Gauss' law with the Gaussian surface depicted below?



- A) Yes, and it would have made the problem much easier!!!
- B) Gauss' law applies, but it would not have been *useful* to compute "g"
- C) Gauss' law would not even apply in this case

2-15