

Taylor adds up the forces on all bits of a body with  $N$  pieces. If all forces are internal, he gets

$$\dot{P} = \sum_{\alpha=1}^N \sum_{\beta \neq \alpha} F_{\alpha\beta}$$

If you wrote out all the terms in this double sum, **how many would there be?**

- A)  $N$
- B)  $N^2$
- C)  $N(N-1)$
- D)  $N!$
- E) Other/not really sure

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(Assume below that N-II is an experimental fact)

We just showed that we can then use N-III to *derive* the law of conservation of momentum for systems of particles.

Is the converse true? i.e.:

**If the law of conservation of total momentum of a system (of two particles) holds, can you *derive* that it MUST be the case that  $\mathbf{F}_{12} = -\mathbf{F}_{21}$ ?**

- A) Yes
- B) No
- C) Maybe *one* could, but *I* can't...

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A  ${}^8\text{Li}$  nucleus at rest undergoes  $\beta$  decay transforming it to  ${}^8\text{Be}$ , an  $e^-$  and an (anti-) neutrino.

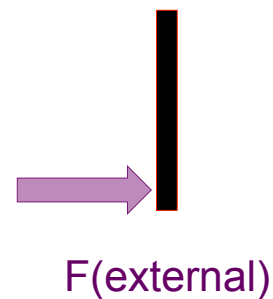
The  ${}^8\text{Be}$  has  $|p|=5 \text{ MeV}/c$  at  $90^\circ$ , the  $e^-$  has  $|p|=6 \text{ MeV}/c$  at  $315^\circ$ , what is  $|p_\nu|$ ?

${}^8\text{Li} \rightarrow {}^8\text{Be} + e^- + \bar{\nu}$   
 A) (4.2, 4.2)  
 B) (-5, 0)  
 C) (-5, -1)  
 D) (-4.2, 0.8)  
 E) (-4.2, -0.8)  
 MeV/c

$p_\nu = ???$

If you push horizontally (briefly!) on the *bottom* end of a long, rigid rod of mass  $m$  (floating in space), what does the rod initially do?

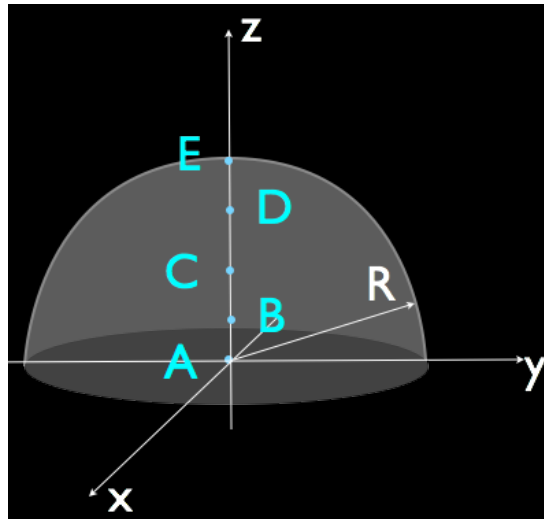
- A) Rotates in place, but the CM doesn't move  
 B) Accelerates to the right, with  $a_{\text{CM}} < F/m$   
 C) Accelerates to the right, with  $a_{\text{CM}} = F/m$   
 D) Other/not sure/depends...



Consider a solid hemisphere of uniform density with a radius  $R$ .

Where is the center of mass?

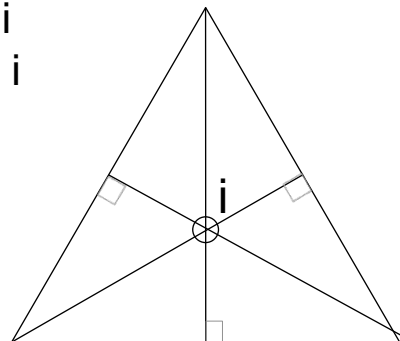
- A)  $z=0$
- B)  $0 < z < R/2$
- C)  $x=R/2$
- D)  $R/2 < z < R$
- E)  $z=R$

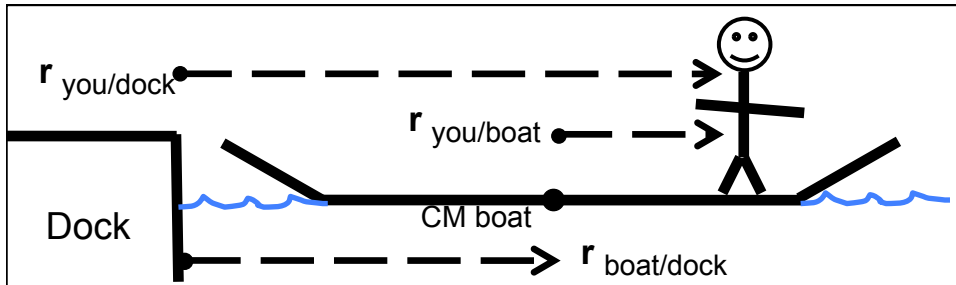


Consider a flat “isosceles triangle”.

Where is the CM?

- A) Precisely at the point  $i$
- B) A little ABOVE point  $i$
- C) A little BELOW point  $i$

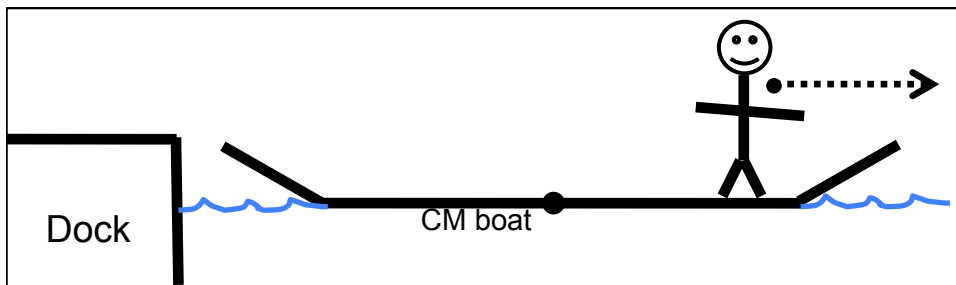




You are walking on a flat-bottomed rowboat.  
Which formula correctly relates position vectors?  
Notation:  $\mathbf{r}_{a/b}$  is “position of a with respect to b.”

A)  $\mathbf{r}_{\text{you/dock}} = \mathbf{r}_{\text{you/boat}} + \mathbf{r}_{\text{boat/dock}}$   
 B)  $\mathbf{r}_{\text{you/dock}} = \mathbf{r}_{\text{you/boat}} - \mathbf{r}_{\text{boat/dock}}$   
 C)  $\mathbf{r}_{\text{you/dock}} = -\mathbf{r}_{\text{you/boat}} + \mathbf{r}_{\text{boat/dock}}$   
 D)  $\mathbf{r}_{\text{you/dock}} = -\mathbf{r}_{\text{you/boat}} - \mathbf{r}_{\text{boat/dock}}$   
 E) Other/not sure

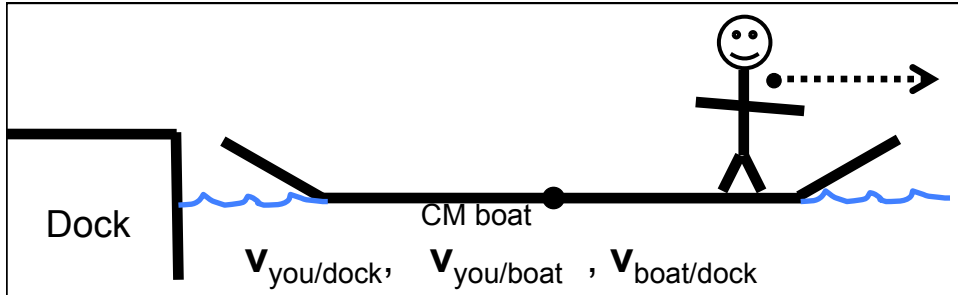
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You are walking on a flat-bottomed rowboat.  
Which formula correctly relates velocities?  
Notation:  $\mathbf{v}_{a/b}$  is “velocity of a with respect to b.”

A)  $\mathbf{v}_{\text{you/dock}} = \mathbf{v}_{\text{you/boat}} + \mathbf{v}_{\text{boat/dock}}$   
 B)  $\mathbf{v}_{\text{you/dock}} = \mathbf{v}_{\text{you/boat}} - \mathbf{v}_{\text{boat/dock}}$   
 C)  $\mathbf{v}_{\text{you/dock}} = -\mathbf{v}_{\text{you/boat}} + \mathbf{v}_{\text{boat/dock}}$   
 D)  $\mathbf{v}_{\text{you/dock}} = -\mathbf{v}_{\text{you/boat}} - \mathbf{v}_{\text{boat/dock}}$   
 E) Other/not sure

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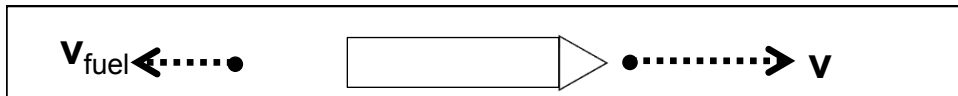


The diagram shows a stick figure walking on a boat towards the right. A dashed arrow points from the figure to the right, indicating its velocity relative to the boat. The boat is on water, and a dock is on the left. A dot on the boat represents its center of mass (CM). Below the diagram, three velocity symbols are listed:  $\mathbf{v}_{\text{you/dock}}$ ,  $\mathbf{v}_{\text{you/boat}}$ , and  $\mathbf{v}_{\text{boat/dock}}$ .

If you are walking in the boat at what feels to you to be your normal walking pace,  $\mathbf{v}_0$ , WHICH of the above symbols equals  $\mathbf{v}_0$ ?

A)  $\mathbf{v}_{\text{you/dock}}$       B)  $\mathbf{v}_{\text{you/boat}}$       C)  $\mathbf{v}_{\text{boat/dock}}$   
 D) NONE of these...

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The diagram shows a rocket moving to the right with velocity  $\mathbf{v}$ . A chunk of fuel is being ejected to the left with velocity  $\mathbf{v}_{\text{fuel}}$  relative to the rocket's reference frame.

A rocket travels with velocity  $\mathbf{v}$  with respect to an (inertial) NASA observer. It ejects fuel at velocity  $\mathbf{v}_{\text{exh}}$  *in its own reference frame*. Which formula correctly expresses the velocity  $\mathbf{v}_{\text{fuel}}$  of a chunk of ejected fuel with respect to an (inertial) NASA observer?

A)  $\mathbf{v}_{\text{fuel}} = \mathbf{v}_{\text{exh}} + \mathbf{v}$   
 B)  $\mathbf{v}_{\text{fuel}} = \mathbf{v}_{\text{exh}} - \mathbf{v}$   
 C)  $\mathbf{v}_{\text{fuel}} = -\mathbf{v}_{\text{exh}} + \mathbf{v}$   
 D)  $\mathbf{v}_{\text{fuel}} = -\mathbf{v}_{\text{exh}} - \mathbf{v}$   
 E) Other/not sure??

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