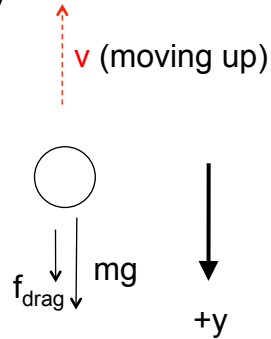


Drag force is: $\vec{f}_D = -b\vec{v} - cv^2\hat{v}$

Consider a mass moving UP
(Let's define DOWN as the +y direction)
Which eq'n of motion is correct?

- A) $m dv_y/dt = +mg - bv_y - cv_y^2$
- B) $m dv_y/dt = +mg - bv_y + cv_y^2$
- C) $m dv_y/dt = +mg + bv_y - cv_y^2$
- D) $m dv_y/dt = +mg + bv_y + cv_y^2$
- E) Other!



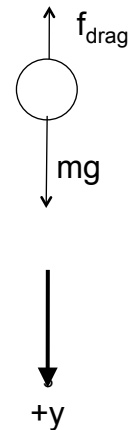
1

Drag force is $\vec{f}_D = -b\vec{v} - cv^2\hat{v}$

(Let's define DOWN as the +y direction)
While moving *up*, the correct expression was:
 $m dv_y/dt = +mg - bv_y + cv_y^2$

If the object is now moving DOWN,
which term(s) in that equation will change sign?

- A) mg (only)
- B) the linear term (only)
- C) the quadratic one (only)
- D) *more* than one term changes sign
- E) NONE of the terms changes sign.



Assuming you have two spheres made of the *same material*, but one has a larger diameter. When dropped in air, which one will reach the higher terminal velocity, the bigger one or the smaller one?

- A) The bigger one
- B) The smaller one
- C) both are the same
- D) ???

4

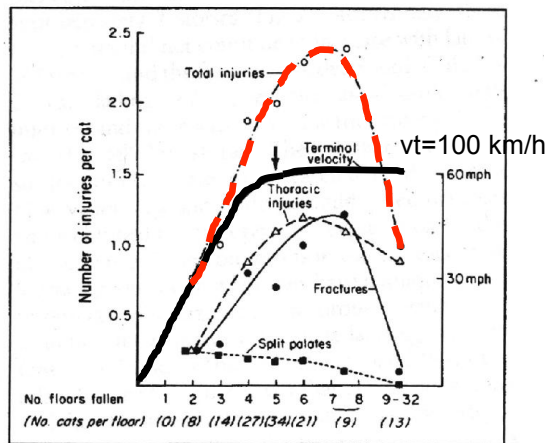


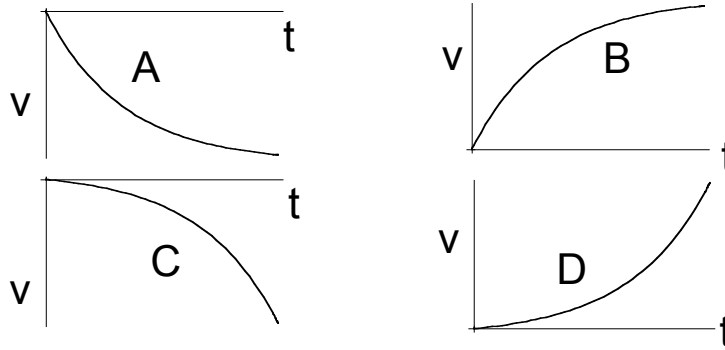
Figure 2—Relationship of injuries to distance fallen and velocity in 132 cats with high-rise syndrome: \downarrow points to terminal velocity (—); total number of injuries/cat (\circ , - - - -); number of thoracic injuries (pulmonary contusions + pneumothorax)/cat (\bullet , —); number of fractures/cat (Δ , - - -); number of split palates/cat (\blacksquare , ·····).

Journal of the American Veterinary Medical Association, 1978 ₅

The solution to the equation describing an object falling from rest with linear air drag was

$$v_y(t) = -v_t(1 - e^{-t/\tau})$$

Which figure best shows this sol'n?



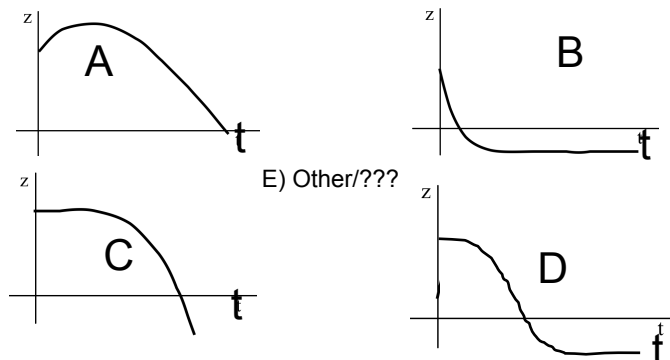
E) Other/???

6

The solution to the eq'n describing an object falling from rest from $h > 0$ with linear air drag was

$$v_y(t) = -v_t(1 - e^{-t/\tau})$$

Which figure best shows height, $y(t)$?



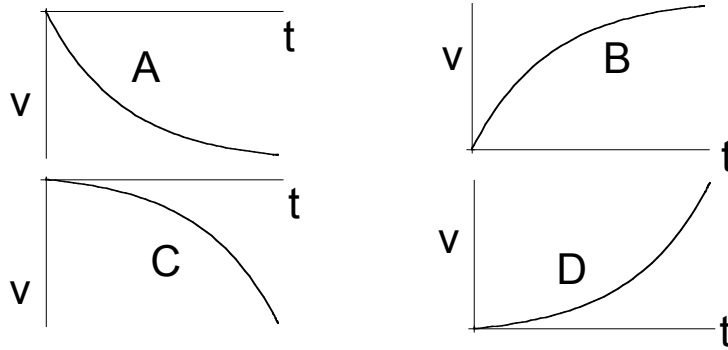
E) Other/???

E) Other/???

The solution to the equation describing an object falling from rest with quadratic air drag was

$$v_y(t) = -v_t \tanh(gt/v_t)$$

Which figure best shows this sol'n?



E) Other/???

8

Which of these two plots seems more realistic for a tennis ball trajectory, comparing (in each graph) the path with (purple), and without (blue), drag.



C) Neither of these is remotely correct!

9

With quadratic air drag, $v(t)=v_0/(1+t/\tau)$

where $\tau=m/(cv_0)$, and $c=(1/2)c_0 A \rho_{\text{air}}$.

(For a human on a bike, c is of order .2 in SI units)

Can you confirm that c is about 0.2? (c_0 is ~ 1 for non-aerodynamic things, and $\sim .1$ for very- aerodynamic things.)

Roughly **how long does it take for a cyclist on the flats to drift down** from $v_0=10$ m/s (22 mi/hr) to ~ 1 m/s?

- A) a couple seconds
- B) a couple minutes
- C) a couple hours
- D) none of these is even close.

In real life, the answer is shorter than this formula would imply. Why?

10

An object is launched directly upwards with initial speed v_0 .

Compare the time t_1 to reach the top to the time t_2 to return back to the starting height.

- A) $t_1 > t_2$
- B) $t_1 = t_2$
- C) $t_1 < t_2$
- D) Answer depends on whether v_0 exceeds v_t or not.

11

A tennis ball is hit directly upwards with initial speed v_0 . Compare the time T to reach the top (height H) to the time and height in an ideal (vacuum) world.

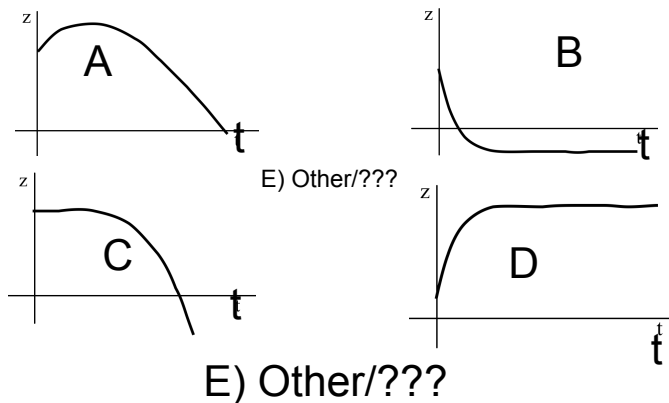
- A) $T > T_{\text{vacuum}}, H \approx H_{\text{vacuum}}$
- B) $T > T_{\text{vacuum}}, H < H_{\text{vacuum}}$
- C) $T \approx T_{\text{vacuum}}, H < H_{\text{vacuum}}$
- D) $T < T_{\text{vacuum}}, H < H_{\text{vacuum}}$
- E) Some other combination!!

12

The solution to the eq'n describing an object thrown up from $h > 0$ with linear air drag was

$$v(t) = -g\tau + \tau(v_0/\tau + g)e^{-t/\tau}$$

Which figure best shows height, $z(t)$?



13

The solution for an object moving horizontally with linear air drag was
 $v(t) = v_0 e^{-t/\tau}$ if $v(t=0) = v_0 > 0$
 Which figure best shows this sol'n?

