## PHYS 2210 Fall 2010 Homework Set 12

## Due at 9:30 AM on December 2nd, 2010 Show your work!

1. (1 pt) Prove this orthogonality relation:

$$\int_{-\pi}^{\pi} \sin(mx)\sin(nx)dx = 0 \text{ if } m \neq n$$
$$= \pi \text{ if } m = n$$

For full credit you must explicitly show the steps to evaluate the integral, and may not use a computer or integral table.

- 2. (1 pt) Find the Fourier Transform of a Gaussian,  $f(x) = e^{-x^2/(2\sigma^2)}$ , and show that it is also a Gaussian. (You will likely need to consult an integral table for this one.) What is the standard deviation of this transformed Gaussian?
- 3. (2 pt) Boas 7.12.12. Just find  $g(\alpha)$ . You don't have to plug back in and find f(x).
- 4. (3 pt) Boas 13.2.2
- 5. (3pt) Boas 13.2.8