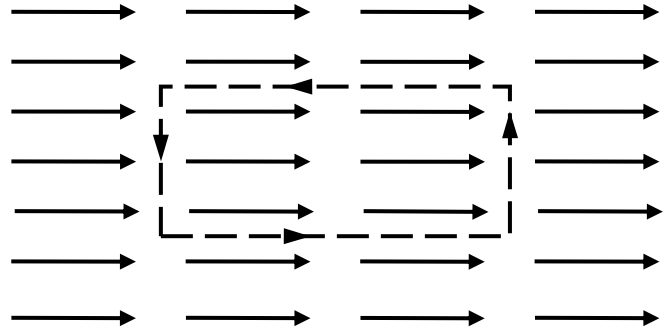


CT3-1. Consider the vector field

$\vec{F} = F \hat{x}$ , where  $F$  is a constant, and consider the closed square path  $L$  shown.



What can you say about the line

integral  $\oint_L \vec{F} \cdot d\vec{s}$  ?

- A)  $\oint_L \vec{F} \cdot d\vec{s} = 0$
- B)  $\oint_L \vec{F} \cdot d\vec{s} > 0$
- C)  $\oint_L \vec{F} \cdot d\vec{s} < 0$

D) It cannot be determined from the information given.

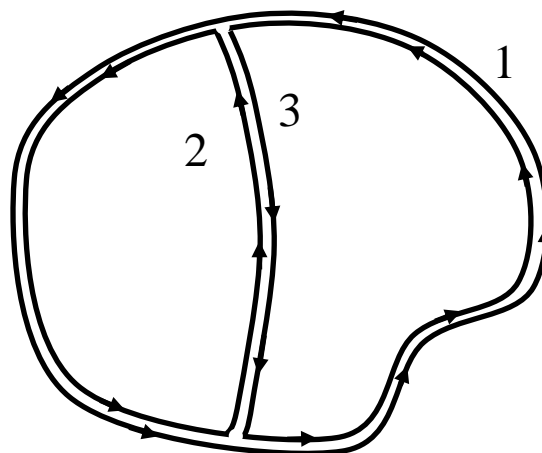
CT3-2. Consider the three closed paths 1, 2, and 3 in some vector field  $\vec{F}$ , where paths 2 and 3 cover the larger path 1 as shown. What can you say about the 3 path integrals  $\oint_1 \vec{F} \cdot d\vec{s}$ ,  $\oint_2 \vec{F} \cdot d\vec{s}$ ,  $\oint_3 \vec{F} \cdot d\vec{s}$  ?

A)  $\oint_1 > \oint_2 + \oint_3$

B)  $\oint_1 < \oint_2 + \oint_3$

C)  $\oint_1 = \oint_2 + \oint_3$

D) Answer depends on the vector field  $\mathbf{F}$ .



CT3-3. Consider the following two vector fields. Which vector field has zero curl everywhere?

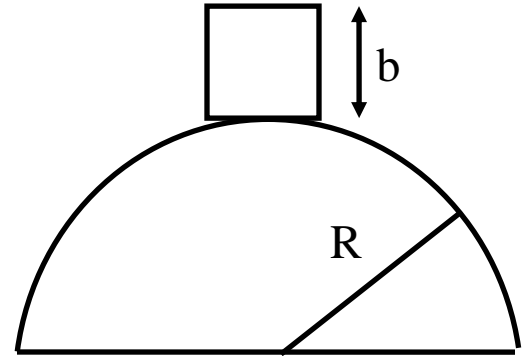
- A) Neither 1 nor 2.
- B) 1 only.
- C) 2 only.
- D) Both 1 and 2.

CT3-4. Consider the following two vector fields. Which vector field has zero curl everywhere?

- A) Neither 1 nor 2.
- B) 1 only.
- C) 2 only.
- D) Both 1 and 2.

CT3-5. A square object of edge length  $b$  is perched on top of a stationary cylinder of radius  $R$ , as shown. The square can roll without slipping on the surface of the cylinder. Is the square in stable equilibrium?

- A) Yes, the equilibrium is always stable
- B) No, the equilibrium is always unstable
- C) The equilibrium is always neutral
- D) The nature of the equilibrium depends on the relative size of  $b$  and  $R$ .



CT3-6. A particle oscillates in a one-dimensional potential. Which of the following properties guarantees simple harmonic motion?

- i) The period  $T$  is independent of the amplitude  $A$
  - ii) The potential  $U(x) = b x^2$  ( $b > 0$ )
  - iii) The force  $F = -k x$  (Hooke's law,  $k > 0$ )
  - iv) The position is sinusoidal in time:  $x = A \sin(\omega t + \alpha)$
- A) only 1 property guarantees simple harmonic motion  
B) exactly 2 properties guarantee simple harmonic motion  
C) exactly 3 properties guarantee simple harmonic motion  
D) all (any one of the properties guarantees simple harmonic motion)

CT3-7. A particle oscillates in a potential well which is not a simple  $U(x) \sim x^2$  harmonic well. The well  $U(x)$  can be written as a Taylor series expansion about the equilibrium point  $x_0$  (at which the first derivative  $dU/dx$  vanishes) :

$$U(x) = U(x_0) + \frac{1}{2}U'' \cdot (x - x_0)^2 + \frac{1}{3!}U''' \cdot (x - x_0)^3 + \dots$$

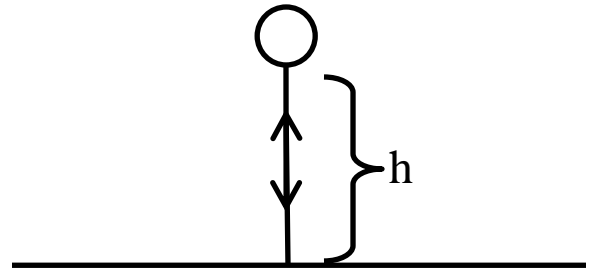
The higher derivatives  $U''$  and  $U'''$  are nonzero at  $x = x_0$ .

In the limit of very small oscillations, that is, in the limit of  $(x - x_0) \rightarrow 0$ , what can you say about this potential well?

- A) The well definitely becomes harmonic..
- B) The well definitely becomes anharmonic.
- C) Whether the well becomes harmonic or anharmonic depends on the function  $U(x)$ .

CT3-8. Consider a super ball which bounces up and down on super concrete. After the ball is dropped from an initial height  $h$ , it bounces with no dissipation and executes an infinite number of bounces back to height  $h$ . Is the motion of the ball in  $z$  simple harmonic motion?

- A) Yes, it is definitely simple harmonic motion.
- B) No, it is definitely not simple harmonic motion.
- C) It cannot be determined from the information given.





CT3-9. A particle is oscillating, back and forth with amplitude  $A$ , in a potential well  $U(x) = kx^4$ ,  $k > 0$ . Notice that, compared to the harmonic  $x^2$  potential, the anharmonic  $x^4$  potential has a flatter bottom and steeper sides. When the amplitude of oscillation is increased, what happens to the period  $T$  of the oscillation for the anharmonic  $x^4$  potential?

- A) period  $T$  increases, as  $A$  increases
- B) period  $T$  decreases, as  $A$  increases
- C) period  $T$  remains constant, as  $A$  increases.

