

CT-1. Which of these operators is a linear operator?

I.  $L(x) = x^2$                       II.  $L(x) = A \cdot \frac{d^2x}{dt^2}$

III.  $L(x) = \sin(x)$                       IV.  $L(x) = A \cdot x + B$

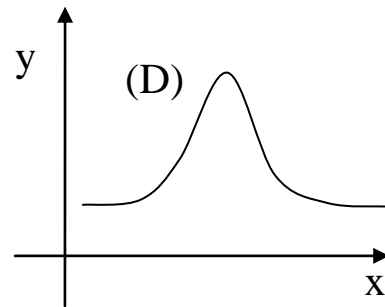
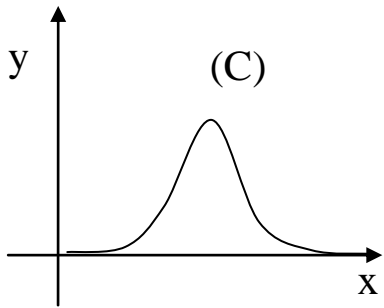
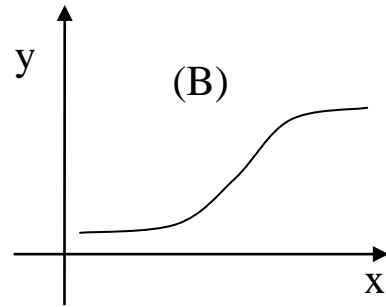
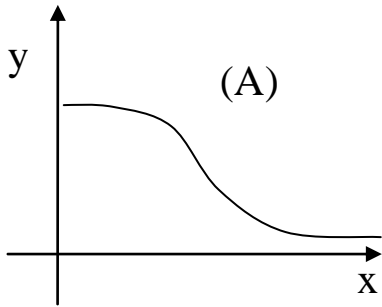
V.  $L(x) = \exp(x) = e^x$

**A) 1 of these                      B) 2 of these                      C) 3                      D) 4**

**E) All 5 of these**

CT-2. What is the shape of the function

$$f(x) = \frac{1}{\sqrt{(x - x_0)^2 + C^2}}, \quad C > 0$$



CT-3. Consider the function  $f(t) = A \exp\left(-i 2\pi n \frac{t}{T}\right)$ ,  $n \neq 0$

What can you say about the these 4 integrals?

I.  $\int_{-T/2}^{+T/2} f(t) dt$

II.  $\int_0^{+T} f(t) dt$

III.  $\int_{1.5T}^{2.5T} f(t) dt$

IV.  $\int_{511T}^{512T} f(t) dt$

A) All are real and non-zero

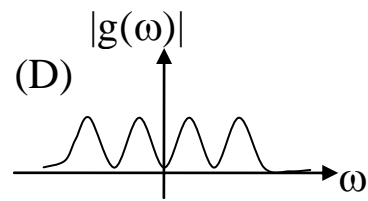
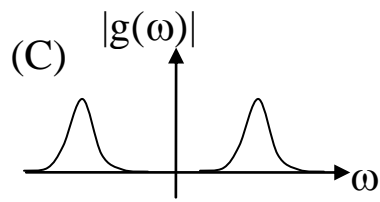
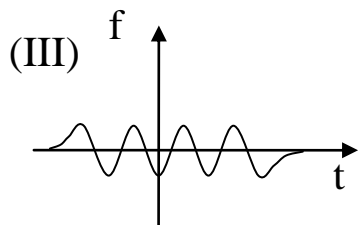
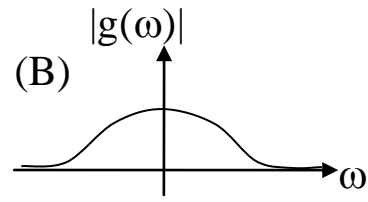
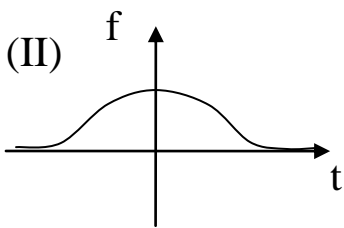
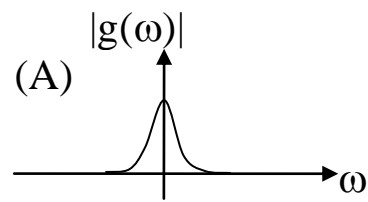
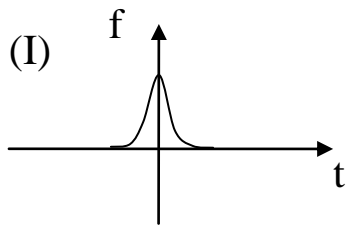
B) All are zero

C) All are pure imaginary and non-zero

D) All are non-zero. Some are real, some are imaginary.

E) Some are real, some are imaginary, at least one is zero.

CT-4. Match the function  $f(t)$  to the magnitude of its Fourier Transform  $|g(\omega)|$ :



(I) has transform (A) or (B)?

(III) has transform (C) or (D)?