

## Final review

Physics 1010



### Reminders:

Final: Tuesday 1:30-4, G1B30. MANDATORY.  
Total scores to be posted this week (with HW 11 in)  
Loads of details about the final on Thursday

Day 29 & 30:  
Review Part 1 & 2

## Final on Tues, 1:30 in this room

- 60 multiple choice questions, worth 80 points.  
An optional long answer -- ~ 5 questions.
- Exam will be closed book.
- **Four** 3 by 5 inch formula cards. You can WRITE anything on it BY HAND. Please write your student ID on your formula card.
- Calculator and pencil/eraser
  - Calculator cannot connect to outside world. No calculators on cell phones or laptops allowed.
  - No sharing of calculators.
  - A limited supply of spare calculators are available (no guarantees they work though!)
- Exam scores and solutions will be posted after the exam on D2L.
- There will be no early or late exams given and no make-up exams.
- Balcony areas will be CLOSED on Tuesday.
- Accommodations across the hall.
- SEE THE WEB FOR WAY MORE INFO!

## Midterm 1 topics - Motion

- Position, velocity and acceleration
  - Definitions, Units
  - Scalars and vectors
  - Graphs of  $x$ ,  $v$ ,  $a$  vs time and relationships between graphs
  - Equations of motion and how to use them:
    - Constant velocity:  $x = x_0 + vt$
    - Constant acceleration:  $v = v_0 + at$
    - $x = x_0 + v_0t + \frac{1}{2}at^2$
- Forces
  - Definition, units, vector
  - $F_{gravity} = mg$  downwards
  - $F_{friction} = 0.3 \times \text{weight}$  in direction opposing motion
  - $F_{spring} = -kx$  in direction opposing extension/compression
  - $F_{net} = ma \Rightarrow$  If  $a = 0$ ,  $F_{net} = 0$
  - Free body diagrams and finding  $F_{net}$

## Midterm 2 summary

- Conservation of energy
  - $W_{ext} - |W_{friction}| = \Delta PE + \Delta KE$
  - Work done by a force =  $F \times d_{//}$
  - Looked at work done by external forces and by friction
  - GPE =  $mgh$ , KE =  $\frac{1}{2}mv^2$ , PPE =  $PV$ , SPE =  $\frac{1}{2}kx^2$ , Thermal energy = constant  $\times T$
  - Ramps, roller coasters, balls.....
  - Power = energy/s
- Bernoulli's equation
  - $E_{tot} = P + \frac{1}{2}\rho v^2 + \rho gh$
  - Conservation of energy for an incompressible fluid
- Nuclear Energy
  - potential energy wells of nucleus
  - Alpha decay
  - Fission & Fusion
  - Radioactivity

## Review Topics – midterm 3

### Light and E/M Radiation

#### Blackbody spectrum

- Introduction to EM waves and the EM spectrum
- Kelvin temperature scale
- Stefan-Boltzman law
- Shape of BB spectrum at different temperatures –  
 $\Rightarrow$  why the sun produces visible light efficiently and incandescent light bulbs don't.

#### Static electricity

- Coulomb's law for force between point charges
- Voltage and electric potential energy (EPE)

#### Electric circuits

- Ohm's Law
- Power dissipation law
- Batteries in series and Parallel

## Last sections of lectures review

### Sound / Music

- Wave basics:  $f$ ,  $T$ ,  $\lambda$ ,  $v$  (and relationships)
- Sound as pressure waves
- Amplitude of waves and associations
- How to get different notes from a violin
- Harmonics on a violin string

### Lasers / Quantum Physics

- Atomic discharge lamps
- Energy levels of electron in an atom
- How light is produced from atom
- Conditions of a laser
- Unique characteristics of a laser

**WHAT AREA DO YOU WANT IN  
Class Review Topics**

Priorities:

- a) position / velocity
- b) Force / acceleration
- c) Conservation of energy / work

Priorities:

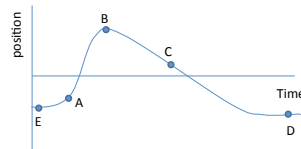
- a) Conservation of energy / work
- b) Bernoulli
- c) Nuclear energy

Priorities:

- a) Light E/M radiation
- b) Blackbody spectra
- c) Static elect/ Voltage
- d) circuits

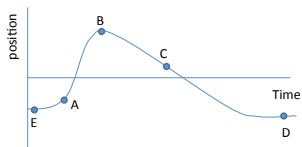
Priorities:

- a) More of the above
- b) Sound
- c) lasers



What is the person's velocity at A

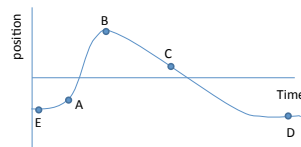
- a) Positive
- b) Negative
- c) Zero
- d) Can't be determined



What is the person's velocity at A

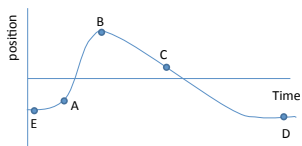
- a) Positive
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- d) Can't be determined

Velocity is the slope of a position vs time graph



Name all points where the person is stationary

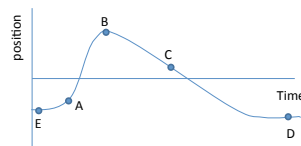
- a) E, B and D
- b) E and D
- c) All points
- d) E, C and D
- e) B only



Name all points where the person is stationary

- a) E, B and D
- b) E and D
- c) All points
- d) E, C and D
- e) B only

person is stationary when velocity = 0.  
Velocity is the slope of a position vs time graph.  
person is stationary when the graph has zero slope (horizontal) , even is only instantaneously



Name all the points where the person is accelerating

- a) A, B and C
- b) B only
- c) All points
- d) A and C
- e) A and B

Name all the points where the person is accelerating

- A, B and C
- B only
- All points
- A and C
- A and B**

When the person is accelerating his velocity is changing  
 Velocity is the slope of a position vs time graph  
 ⇒ So when he is accelerating, the slope of this graph is changing

What is the person's average velocity between points F and G?

- Something greater than zero (positive)
- Something less than zero (Negative)
- Zero
- Can't determine from this graph

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- Something greater than zero (positive)
- Something less than zero (Negative)
- Zero**
- Can't determine from this graph

Average velocity = change in position/time taken  
 At F and G the person is at the SAME position, so the change in position is 0.  
 ⇒ Average velocity is zero

**Net forces and acceleration**

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

Which diagram shows the net force on a loaded box when it is at rest?

**Net forces and acceleration**

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**E:  $F_{net} = ma$**

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Which diagram shows the net force on a loaded box accelerating to the right at  $2m/s^2$ ?

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**D:  $F_{net} = ma$**

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Which diagram shows the net force on a loaded box when it is being pushed to the right at steady velocity?

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Which diagram shows the net force on a loaded box when it is decelerating to a stop? (Prior to decelerating it was moving to the right at a steady velocity)

**Net forces and acceleration**

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**C:**

- Velocity was to right and now box is decelerating to a stop
- Direction of velocity CHANGE ( $\Delta v = v_f - v_i$ ) is to the left
- $a = \Delta v / \Delta t \Rightarrow$  also to left
- $F_{net} = ma \Rightarrow$  net force in same direction as acceleration

**Net forces and acceleration**

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

What is the magnitude of the horizontal force that I am applying to the box when it is sliding across the floor at a constant velocity?

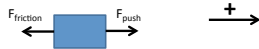
- a. 392 N
- b. 117.6 N
- c. 1306.7 N
- d. 2.9 N
- e. None of the above

**Net forces and acceleration**

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- a. 392 N
- b. 117.6 N
- c. 1306.7 N
- d. 2.9 N
- e. None of the above



$$\begin{aligned}
 F_{net} &= F_{push} - F_{friction} \\
 &= ma \\
 &= 0 \\
 F_{push} &= F_{friction} \\
 &= \mu mg \\
 &= (0.3)(40)(9.8) \\
 &= 117.6 \text{ N}
 \end{aligned}$$

**Net forces and acceleration**

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

What is the magnitude of the horizontal force that I am applying to the box when it is accelerating across the floor at 1.5m/s<sup>2</sup>?

- a. 60 N
- b. 57.6 N
- c. 588.0 N
- d. 177.6 N
- e. None of the above

**Net forces and acceleration**

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$$\begin{aligned}
 F_{net} &= F_{push} - F_{friction} \\
 F_{push} - F_{friction} &= ma \\
 F_{push} &= F_{friction} + ma \\
 &= (0.3)(40)(9.8) + (40)(1.5) \\
 &= 177.6 \text{ N}
 \end{aligned}$$

**Springs**

I have a spring which is labeled 'Spring constant = 8 N/m'. I assume that this is correct and use it to measure the mass of an apple. I attach the apple to the bottom of the spring and it stretches 12.5cm (or 0.125m). What is the mass of the apple? (assume g = 10m/s<sup>2</sup>)

- a) 0.1 kg
- b) 1kg
- c) 10kg
- d) 100kg
- e) Can't be determined.

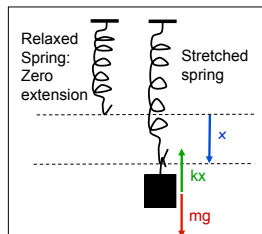
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- a) 0.1 kg
- b) 1kg
- c) 10kg
- d) 100kg
- e) Can't be determined.

In equilibrium, net force on apple = 0. Downwards force of gravity is exactly equal and opposite to upwards force from spring.

$$\begin{aligned}
 \Rightarrow mg &= kx \\
 m &= kx/g \\
 &= (8\text{N/m})(0.125\text{m})/(10\text{m/s}^2) \\
 &= 0.1 \text{ kg}
 \end{aligned}$$



Now I hang the same apple on a different spring and it stretches much less than 12.5cm. What is the spring constant of this spring?

- a) Less than 8N/m
- b) 8N/m
- c) More than 8N/m
- d) Can't determine from information given

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- b) 8N/m
- c) **More than 8N/m**
- d) Can't determine from information given

Less extension for same force  $\Rightarrow$  stiffer spring  $\Rightarrow$  higher value of  $k$ .

$mg = kx$  in equilibrium when net force = 0.

$k = mg/x$

Smaller  $x \Rightarrow$  bigger  $k$

Which spring exerted the bigger upwards force on the apple?

- a) The weak spring which had a large extension
- b) The stiffer spring (smaller extension)
- c) They exerted the same upwards force
- d) Can't tell from this information

Which spring exerted the bigger upwards force on the apple?

- a) The weak spring which had a large extension
- b) The stiffer spring (smaller extension)
- c) **They exerted the same upwards force**
- d) Can't tell from this information

In BOTH cases, in equilibrium, the net force = 0

$\Rightarrow mg = kx$

$mg$  is the weight of the apple and the same in both cases

$\Rightarrow$  The upwards force the the spring ( $kx$ ) is the same in both cases

### Energy & Work

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

When the box is travelling at a constant velocity of 3m/s, what is its KE?

- a. 360 J
- b. 180 J
- c. 60 J
- d. 120 J
- e. None of the above

### Energy & Work

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

When the box is travelling at a constant velocity of 3m/s, what is its KE?

- a. 360 J
- b. **180 J**
- c. 60 J
- d. 120 J
- e. None of the above

$$KE = 1/2 mv^2$$

### Energy & Work

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg. The warehouse floor is made of concrete and there is a coefficient of sliding friction of 0.3 between the boxes and the floor.

If I suddenly let go and stop pushing the box when it is travelling at 3m/s across the floor, how far does the box travel before it comes to a stop?

- a. 0m
- b. 0.5 m
- c. 1m
- d. **1.5m**
- e. 2m

**Energy & Work**

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d. **1.5m**  
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$$\cancel{W_{ext}} - \cancel{|W_{friction}|} = \cancel{\Delta PE} + \cancel{\Delta KE}$$

Work done by friction = KE lost

$$-|F_{friction} d| = KE_f - KE_i$$

$$-(0.3mg)(d) = 0 - \frac{1}{2} mv^2$$

$$(0.3g)(d) = \frac{1}{2} v^2$$

$$d = \frac{1}{2} v^2 / (0.3g)$$

$$= (0.5 \cdot 9) / (0.3 \cdot 9.8)$$

$$= 1.5m$$

**Energy & Work**

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg.

On the far side of the warehouse I load a box onto a light frictionless cart. I push the cart plus box up a loading ramp. The height of the ramp is 4m above the floor. The length of the ramp is 8m.

How much work do I do pushing the cart at a slow steady speed from the bottom of the ramp to the top?

a. 392 N  
b. 392 J  
c. 1568 J  
d. 40 J  
e. 39 N

**Energy & Work**

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a. 392 N  
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c. **1568 J**  
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$$\cancel{W_{ext}} - \cancel{|W_{friction}|} = \cancel{\Delta PE} + \cancel{\Delta KE}$$

Work done = GPE gained by box

$$= mgh$$

$$= (40)(9.8)(4)$$

$$= 1568 J$$

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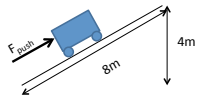
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What force do I have to apply (parallel to the surface of the ramp) to push the cart up the ramp?

a. 392 N  
b. 196 N  
c. 1568 N  
d. 0 N  
e. None of the above



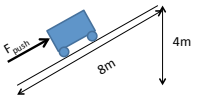
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What force do I have to apply (parallel to the surface of the ramp) to push the cart up the ramp?

a. 392 N  
b. **196 N**  
c. 1568 N  
d. 0 N  
e. None of the above



Work done = Force  $\times$  distance travelled parallel to force

$$1568 J = F_{push} \times 8m$$

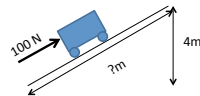
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Suppose that I can only push with a maximum force of 100 N. What is the minimum length of ramp that I need to use?

- 15.7m
- 8m
- 19.3 m
- 25.5 m
- None of the above



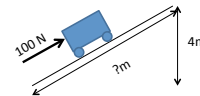
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- 8m
- 19.3 m
- 25.5 m
- None of the above



$$\text{Work done} = \text{Force} \times \text{distance travelled parallel to force}$$

$$1568 \text{ J} = 100 \text{ N} \times d$$

## Energy &amp; Work

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At the top of the ramp I let the cart go. What is its speed when it reaches the bottom of the ramp?

- 1568 J
- 78.4 m/s
- 8.9 m/s
- 6.3 m/s
- None of the above

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- 6.3 m/s
- None of the above

$$W_{\text{ext}} - |W_{\text{friction}}| = \Delta PE + \Delta KE$$

$$\text{GPE lost} = \text{KE gained}$$

$$mgh = \frac{1}{2}mv^2$$

$$2gh = v^2$$

$$v = \sqrt{2gh}$$

$$= \sqrt{2 \cdot 9.8 \cdot 4}$$

$$= 8.9 \text{ m/s}$$

## Energy &amp; Work

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This time I take the box off the cart and let it slide down the ramp. There is a frictional force between the box and ramp of 100N. Assume that we are using the 8m ramp. What is the KE of the box at the bottom of the ramp?

- 1568 J
- 784 J
- 496 J
- 768 J
- None of the above

## Energy &amp; Work

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$$W_{\text{ext}} - |W_{\text{friction}}| = \Delta PE + \Delta KE$$

$$-|(F_{\text{friction}})(d_{\text{ramp}})| = mg\Delta h + \Delta KE$$

$$= mg(h_i - h_f) + KE_f - KE_i$$

$$= mg(0 - 4) + KE_f - 0$$

$$= -4mg + KE_f$$

$$KE_f = 4mg - (F_{\text{friction}})(d_{\text{ramp}})$$

$$= 4(40)(9.8) - (100)(8)$$

$$= 768 \text{ J}$$



### Energy & Work

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On the far side of the warehouse I load a box onto a light frictionless cart. I push the cart plus box up a loading ramp. The height of the ramp is 4m above the floor. The length of the ramp is 8m.

This time I take the box off the cart and let it slide down the ramp. There is a frictional force between the box and ramp of 100N. Assume that we are using the 8m ramp. What is the speed of the box at the bottom of the ramp?

- 6.2 m/s
- 38.4 m/s
- 2.7 m/s
- 4.8 m/s
- 0m/s

### Energy & Work

I'm working in a warehouse packing goods into boxes and moving them to the loading bay. Once loaded, each box has a mass of 40kg.

On the far side of the warehouse I load a box onto a light frictionless cart. I push the cart plus box up a loading ramp. The height of the ramp is 4m above the floor. The length of the ramp is 8m.

This time I take the box off the cart and let it slide down the ramp. There is a frictional force between the box and ramp of 100N. Assume that we are using the 8m ramp. What is the speed of the box at the bottom of the ramp?

- 6.2 m/s
  - 38.4 m/s
  - 2.7 m/s
  - 4.8 m/s
  - 0m/s
- $KE = \frac{1}{2} mv^2$   
 $v = \sqrt{2 KE / m}$   
 $= \sqrt{2 * 768 / 40}$  (KE at bottom ramp from previous Q)  
 $= 6.2 \text{ m/s}$

### Bernoulli's equation

$$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$$

↑ PPE     ↑ KE     ↑ GPE

Conservation of energy for a unit volume of an incompressible liquid (e.g. water)  
 Assumes: No pumps, no friction in system of interest

#### Method:

- Pick 2 points in system
  - One where we know everything
  - One where we want to calculate a quantity
- Write an expression for  $E_{tpv}$  at both points
- Equate expressions  $E_{tpv}$  at both points
- Solve equation to find unknown quantity

My house is on the side of a hill. The water at the faucet has a mains pressure of 30 psi (200,000 Pa) above atmospheric. (Set AP as the zero of pressure). I attach a hose to the faucet and let the hose run down the hill. The faucet is open but the valve at the outlet of the hose is closed.

If the outlet of the hose is 6m vertically below the faucet, what is the pressure (above atmospheric) behind the outlet valve?

- 200,000 Pa
- 141,200 Pa
- 258,000 Pa
- 324,400 Pa
- None of the above

$$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$$

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- 200,000 Pa
- 141,200 Pa
- 258,000 Pa
- 324,400 Pa
- None of the above

$$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$$

$$\text{At faucet: } P = 200,000 \text{ Pa, } v = 0, h = 0$$

$$E_{tpv} = 200,000 \text{ Pa}$$

$$\text{At valve: } P = P_{\text{valve}}, v = 0, h = -6 \text{ m}$$

$$E_{tpv} = P_{\text{valve}} + \rho g(-6)$$

$$200,000 = P_{\text{valve}} - 1000 * 9.8 * 6$$

$$P_{\text{valve}} = 200,000 + 1000 * 9.8 * 6$$

$$= 258,800 \text{ Pa}$$

My house is on the side of a hill. The water at the faucet has a mains pressure of 30 psi (200,000 Pa) above atmospheric. I attach a hose to the faucet and let the hose run down the hill. The faucet is open but the valve at the outlet of the hose is closed.

The outlet valve is still closed and 6m below the house. I poke a small hole in the hose near the outlet valve. What is the velocity of the water leaving this hole?

- 22.8 m/s
- 20.2 m/s
- 15.4 m/s
- 9.0 m/s
- 4.6 m/s

$$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$$

My house is on the side of a hill. The water at the faucet has a mains pressure of 30 psi (200,000 Pa) above atmospheric. I attach a hose to the faucet and let the hose run down the hill. The faucet is open but the valve at the outlet of the hose is closed. The outlet valve is still closed and 6m below the house. I poke a small hole in the hose near the outlet valve. What is the velocity of the water leaving this hole?

**$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$**

a. 22.8 m/s  
b. 20.2 m/s  
c. 15.4 m/s  
d. 9.0 m/s  
e. 4.6 m/s

At faucet:  $P = 200,000 \text{ Pa}$ ,  $v = 0$ ,  $h = 0$   
 $E_{tpv} = 200,000 \text{ Pa}$

Outside hole:  $P = 0$ ,  $v = ?$ ,  $h = -6\text{m}$   
 $E_{tpv} = \frac{1}{2} \rho v^2 + \rho g(-6)$

$200,000 = \frac{1}{2} \rho v^2 - 1000 \cdot 9.8 \cdot 6$   
 $\frac{1}{2} \rho v^2 = 200,000 + 1000 \cdot 9.8 \cdot 6$   
 $= 258,800$   
 $v = \sqrt{2 \cdot 258800 / 1000}$   
 $= 22.8 \text{ m/s}$

My house is on the side of a hill. The water at the faucet has a mains pressure of 30 psi (200,000 Pa) above atmospheric. I attach a hose to the faucet. If I run the hose up the hill instead and open the outlet valve, what is the maximum vertical height of the hose outlet above the faucet at which any water will come out?

**$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$**

a. 30.5 m  
b. 20.4 m  
c. 14.7 m  
d. 9.8 m  
e. 0 m

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**$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$**

a. 30.5 m  
b. 20.4 m  
c. 14.7 m  
d. 9.8 m  
e. 0 m

At faucet:  $P = 200,000 \text{ Pa}$ ,  $v = 0$ ,  $h = 0$   
 $E_{tpv} = 200,000 \text{ Pa}$

At outlet:  $P = 0$ ,  $v = 0$ ,  $h = h_{\text{max}}$   
 $E_{tpv} = \rho gh_{\text{max}}$

$200,000 = 1000 \cdot 9.8 \cdot h_{\text{max}}$   
 $h_{\text{max}} = 20.4 \text{ m}$

### Water distribution in skyscrapers

The skyscraper water problem:

- Less pressure on the higher floors,
- Water won't make it to the top floor....

How can you solve this problem?

- Put very high pressure pump at bottom (give water enough PPE at bottom)
- Use a series of pumps up the building
- Pump water to a tank on the roof, then you will always have pressure on the floors below.

### What about speed in a pipe?

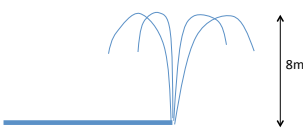
**$P + \frac{1}{2} \rho v^2 + \rho gh = E_{\text{total}}/V$**  ( $E_{\text{total}}$  per unit volume)

<http://phet.colorado.edu/en/simulation/fluid-pressure-and-flow>

I'm designing a fountain for a city park. I want the water in the fountain to squirt 8m vertically in the air. What pressure will I need in the large pipe just before the nozzle? (Assume that friction can be ignored)

a. 8000 Pa  
b. 80 Pa  
c. 80,000 Pa  
d. 12 000 Pa  
e. More information required

**$E_{tpv} = P + \frac{1}{2} \rho v^2 + \rho gh$**



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a. 8000 Pa  
 b. 80 Pa  
 c. 80,000 Pa  
 d. 12 000 Pa  
 e. More information required

$E_{\text{tpv}} = P + \frac{1}{2} \rho v^2 + \rho gh$   
 Top of water jet:  $v = 0, P = 0, h = 8\text{m}$   
 In pipe:  $v = 0, h = 0, P = ?$   
 $E_{\text{tpv}}$  is same in both locations  
 $P_{\text{pipe}} = \rho gh_{\text{jet}}$   
 $= 1000 * 10 * 8$   
 $= 80,000 \text{ Pa}$

### More Bernoulli!!

I have a tank of water that is 4m deep.  
 What is the pressure of water at the bottom on the tank?  
 (Set AP as the zero of pressure,  $\rho = 1000\text{kg/m}^3$  for water)

### More Bernoulli!!

I have a tank of water that is 4m deep.  
 What is the pressure of water at the bottom on the tank?  
 (Set AP as the zero of pressure)

I'm going to set the zero of height at the surface of the water.

At surface:  $P = 0, v = 0, h = 0$   
 $E_{\text{tpv}} = 0$

At bottom of tank:  $P = ?, v = 0, h = -4\text{m}$   
 $E_{\text{tpv}} = P + \rho g(-4)$

$0 = P - 4\rho g$   
 $P = 4 * 1000 * 9.8$   
 $= 39200 \text{ Pa}$

### More Bernoulli!!

I have a tank of water that is 4m deep.  
 (Set AP as the zero of pressure)  
 I drill a small hole in the side of the tank 2m below the surface.  
 What is the velocity of water leaving the hole?

### More Bernoulli!!

I have a tank of water that is 4m deep.  
 (Set AP as the zero of pressure)  
 I drill a small hole in the side of the tank 2m below the surface.  
 What is the velocity of water leaving the hole?

I'm going to set the zero of height at the surface of the water.

At surface:  $P = 0, v = 0, h = 0$   
 $E_{\text{tpv}} = 0$

Just outside hole:  $P = 0, v = ?, h = -2\text{m}$   
 $E_{\text{tpv}} = \frac{1}{2} \rho v^2 + \rho g(-2)$   
 $0 = \frac{1}{2} \rho v^2 - 2\rho g$

Rearrange to solve for v:  $v = 6.3 \text{ m/s}$

### More Bernoulli!!

I have a water pump that produces water at pressure  $P_{\text{pump}}$  at the outlet. If I want to pump water to a height of 8m above the pump, what is the minimum pressure that the pump needs to produce?

**More Bernoulli!!**

I have a water pump that produces water at pressure  $P_{\text{pump}}$  at the outlet. If I want to pump water to a height of 8m above the pump, what is the minimum pressure that the pump needs to produce?

At output of pump:  $P = P_{\text{pump}}$ ,  $v = 0$ ,  $h = 0$   
 $E_{\text{tpv}} = P_{\text{pump}}$   
 (v is equal to zero because when the pump has this minimum pressure only a tiny bit of water is JUST flowing out of the top end of the pipe. The flow rate in the pipe is negligible).

At top of pipe:  $P = 0$ ,  $v = 0$ ,  $h = 8\text{m}$ .  
 $E_{\text{tpv}} = \rho g(8)$

$P_{\text{pump}} = 1000 \cdot 9.8 \cdot 8 = 78400 \text{ Pa}$

**More Bernoulli!!**

I have a water pump that produces water at pressure  $P_{\text{pump}}$  at the outlet. If I want the water to leave a small nozzle at the end of the pipe (8m above the pump) at a velocity of 2m/s, what pressure must the pump produce?

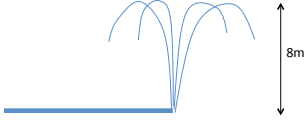
**More Bernoulli!!**

I have a water pump that produces water at pressure  $P_{\text{pump}}$  at the outlet. If I want the water to leave a small nozzle at the end of the pipe (8m above the pump) at a velocity of 2m/s, what pressure must the pump produce?

At pump:  $P = ?$ ,  $v = 0$  (amount of water leaving small nozzle is negligible),  $h = 0$ .  
 $E_{\text{tpv}} = P_{\text{pump}}$

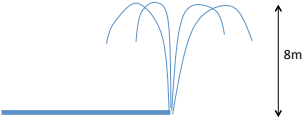
Just outside nozzle:  $P = 0$ ,  $v = 2\text{m/s}$ ,  $h = 8\text{m}$   
 $E_{\text{tpv}} = \frac{1}{2} \rho (2^2) + 8\rho g$

$P_{\text{pump}} = \frac{1}{2} \rho (2^2) + 8\rho g$   
 $= \frac{1}{2} \cdot 1000 \cdot 4 + 8 \cdot 1000 \cdot 9.8$   
 $= 80400 \text{ Pa}$



What is the speed of the water immediately after the nozzle?

- ~15.3 m/s
- ~12.5 m/s
- ~8.7 m/s
- ~4.3 m/s
- Water does not come out



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- ~15.3 m/s
- ~12.5 m/s
- ~8.7 m/s
- ~4.3 m/s
- Water does not come out

$E_{\text{tpv}} = P + \frac{1}{2} \rho v^2 + \rho gh$

Inside pipe:  $v = 0$ ,  $P = 80,000 \text{ Pa}$ ,  $h = 0$   
 After nozzle:  $v = ?$ ,  $h = 0$ ,  $P = 0$

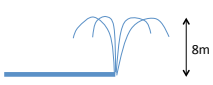
$E_{\text{tpv}}$  is same in both locations

$P_{\text{pipe}} = \frac{1}{2} \rho v^2$   
 $v = \sqrt{2P_{\text{pipe}}/\rho}$   
 $= \sqrt{2 \cdot 80,000 / 1,000}$   
 $= 12.6 \text{ m/s}$



If the fountain squirts  $2\text{m}^3$  of water in the air every second, what is the power produced by the pump that is supplying the pressurized water to the nozzle?

- 78400 W
- 2 W
- 1000 W
- 237,806 W
- 156,800 W



If the fountain squirts  $2\text{m}^3$  of water in the air every second, what is the power produced by the pump that is supplying the pressurized water to the nozzle?

a. 78400 W  
 b. 2 W  
 c. 1000 W  
 d. 237,806 W  
 e. 156,800 W

Power = energy supplied to water / sec  
 = GPE gained by water / sec  
 =  $mgh/s$   
 =  $(m/s) \times g \times h$

Mass of water squirted per second =  $2\text{m}^3 \times 1000\text{kg}/\text{m}^3$   
 = 2000kg

Power =  $2000 \times 9.8 \times 8$   
 = 156,800 W

### Recipe- how to make an atom:

Ingredients: 1 teaspoon protons  
 1 teaspoon neutrons  
 1 cup of electrons

- Proton (positive charge)
- Neutron (no charge)
- Electron (negative charge)

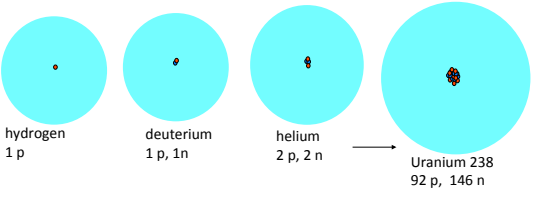
- Mix protons and neutrons thoroughly.
- Bake at 100 million degrees until sticks together to form solid dense nucleus (about .0000001 s).
- Frost with lightly with fluffy layer of negative electrons.
- Chill before serving!

atom size:  
 Radius of nucleus is 10,000 times smaller than nucleus-electron distance

### Each element has different number of protons.

Atom ingredients:

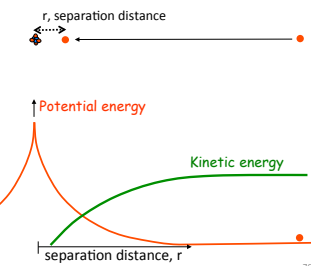
- Proton (positive charge) - charge =  $1.6 \times 10^{-19}$  Coulombs  
 mass =  $1.66 \times 10^{-27}$  kg.
- Neutron (no charge) - no charge  
 mass =  $1.66 \times 10^{-27}$  kg.
- Electron (negative charge) - charge =  $-1.6 \times 10^{-19}$  Coulombs  
 mass =  $9.10 \times 10^{-31}$  kg



hydrogen 1 p  
 deuterium 1 p, 1n  
 helium 2 p, 2 n  
 Uranium 238 92 p, 146 n

What if threw proton so starts out going towards nitrogen nucleus with a lot of speed (lots of kinetic energy)?

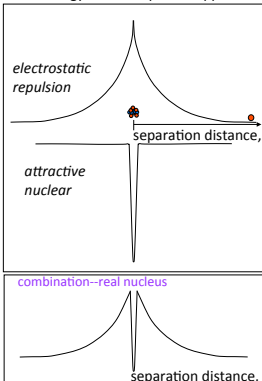
Starts with lots of kinetic energy  $\rightarrow$   
 Repelling force from nucleus slows down proton  $\rightarrow$   
 Proton's kinetic energy converted into electrostatic potential energy, as it gets closer to nucleus



Potential energy curves- represent energy to bring particles together.

Gravity energy analogy. if at center, want to roll down hill/fly apart ... lots of electrostatic potential energy

### Potential energy curve for proton approaching nucleus



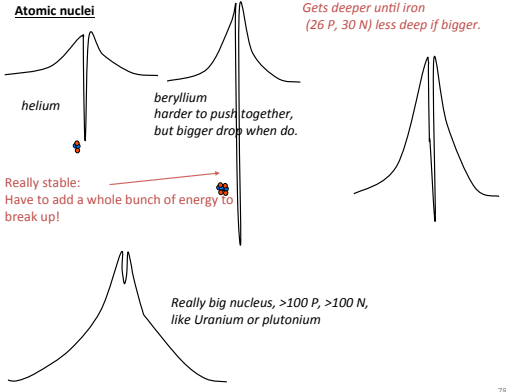
Energy scale gigantic compared to chemical energy. Why? Simple coulomb's law.

$$F = k \frac{(\text{charge of \#1})(\text{charge of \#2})}{r^2}$$

Chemistry- forces between electrons and protons on distance scale of atomic size ( $> 10^{-10}$  m).

Nuclear forces- forces between protons on distance scale 10-100,000 times smaller. 10,000 times closer means forces 100,000,000 times bigger because of  $1/r^2$ . Lots more potential energy stored!!!

### Atomic nuclei



Gets deeper until iron (26 P, 30 N) less deep if bigger.

Really stable: Have to add a whole bunch of energy to break up!

Really big nucleus,  $>100$  P,  $>100$  N, like Uranium or plutonium

**tunneling difficulty = width x depth of tunnel**

hard- takes long time, billions of years!

medium

easy!, happens in millionths of a second!

How much energy released?  
 a. 1 most, 2 second, 3 least  
 b. 2 most, 1, 3 least  
 c. 3 most, 2, 1 least  
 d. 3 most, 1, 2 least

energy is difference from bottom of crater to outside.  
 3 is most, 2 second, 1 is least

### Another Sim

(because this is hard to do at home)

<http://phet.colorado.edu/en/simulation/nuclear-fission>

### Neutron Induced fission- key to atomic bombs

- two smaller nuclei
- few extra free neutrons
- LOTS OF ENERGY!!
- (+sometimes other bad stuff)

simulation

Neutron absorbed →  
 Excites U235 nucleus up above potential barrier →  
 Splits into two smaller nuclei... which zoom apart due to electrostatic repulsion!

### BACK TO CHAIN REACTION

Fission Nuclear explosion: "atomic bomb"

Very special stuff: Uranium 235 or plutonium

Why Ur 235 not 238? U 238 has 3 extra neutrons help hold it together. Deeper crater in potential energy.

Eats extra neutrons!

U235 and U238 atoms are placed into a container, which are likely to result in a chain reaction (resulting in explosion) when a free neutron triggers fission of one of the U235:

- #2 only
- #1, #2, and #5
- #2 and #4
- #2, #3, and #4
- #2, #4, and #5.

Lots of uranium in the ground... why not just blow up?

Correct answer is c. (#2 and #4) Analysis:  
 #1 is too sparse .. most neutrons will leave box before hitting another U235.  
 #2 is good.. Pure U235, densely packed, large package  
 #3 has too many U238's... more U238's than 235's. Free neutrons more likely to be absorbed by 238's than to hit and fission another 235.  
 #4 is OK ... More U235's than 238's, still densely packed, large package  
 #5 is too small of package ... neutrons likely to escape package before hitting another U235.

### Fusion bomb or "hydrogen bomb"

Basic process like in sun. Stick small nuclei together.

Which will release more energy during fusion?  
 a. Deuterium combining with deuterium  
 b. Deuterium combining with tritium

Answer is b. Incoming deuterium particle has comparatively more potential energy!

### Fusion bomb or "hydrogen bomb"

Basic process like in sun. Stick small nuclei together.

Stick hydrogen isotopes together to make helium.

activation energy of 100 million degrees  
push together energy required  
energy released if push over the hump

Simple if can push hard enough- just use sun or fission bomb. More energy per atom than fission. Can use LOTS of hydrogen.

**⇒ End up with GIGANTIC bombs**  
1000 times bigger than first fission bombs

85

### Wavelength

For periodic waves, we can identify a wave length,  $\lambda$ , by measuring the distance between unique points

Periodic wave space  
Periodic wave

### Electromagnetic waves can have any wavelength

Scientific notation is useful!

gamma rays X-rays ultraviolet rays infrared rays radar FM TV shortwave AM

Wavelength (meters)

Visible Light

Wavelength (nanometers)

87

### The electromagnetic spectrum

- All EM radiation is a periodic modulation of the electric field
- All EM radiation travels at speed  $c = 3 \times 10^8$  m/s
- $c = \lambda \times f$
- Visible light is just one part of the electromagnetic spectrum with specific range of  $\lambda$  (and  $f$ )

Purple light has a wavelength of 400 nm. What is its frequency?  
(1 nm =  $1 \times 10^{-9}$  m)

a.  $7.5 \times 10^5$  Hz  
b.  $7.5 \times 10^{14}$  Hz  
c.  $1.3 \times 10^{-6}$  Hz  
d. 1333 Hz  
e.  $400 \times 10^9$  Hz

$f = c/\lambda$

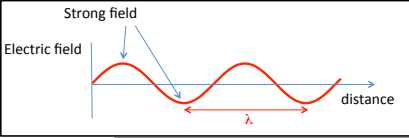
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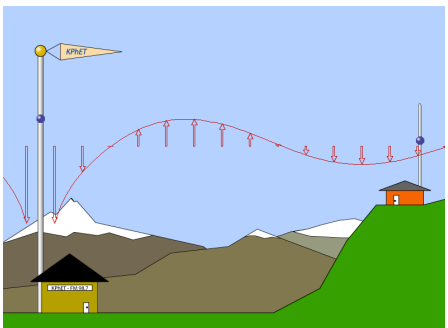
$f = c/\lambda$   
Use standard units!

### What is Electric field?

- Light is periodic modulation of "electric field"



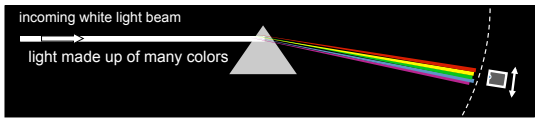
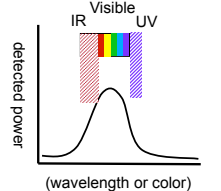
- Electric field exists everywhere in space
- Describes the force on a charged particle at each point in space
- Vector – has a magnitude and direction
- Units: Newtons/Coulomb
- Contains energy
- Created by charges (and created in other ways)
- Analogy: Like gravitational field describes the force on a particle with mass
- Balloon demo

<http://phet.colorado.edu/en/simulation/radio-waves>

### The spectrum of white light?

A spectrometer measures the spectrum (range of wavelengths or frequencies) in light

White light

- Defined as the spectrum of EM radiation emitted by the sun
- All visible  $\lambda$  present with roughly equal intensity

### Blackbody spectrum and temperature

- Everything that has a non-zero temperature emits a spectrum of EM radiation
- The spectrum of EM radiation coming from a black object is called the "blackbody spectrum."
- Black object: Absorbs and emits all EM  $\lambda$  easily
- Go to the [blackbody spectrum simulation](#)
- BB spectrum determined by temperature only.
- The temperature of the object affects both
  - The total power of EM radiation emitted by the object
  - The range of wavelengths emitted (the spectrum)

### Temperature and total emitted power (brightness)

Stefan-Boltzman law gives total electromagnetic power (energy/second) out of a hot object at temperature T

$$\text{Power} = e \times \sigma \times T^4 \times A$$

$e$  = "emissivity"; how well the light gets out  
 $\sigma$  = Stefan-Boltzmann constant,  $\sigma = 5.67 \times 10^{-8} \text{ J}/(\text{s m}^2 \text{ K}^4)$   
 $T$  = Temperature of object (in Kelvin!)  
 $A$  = Area of surface

What is 2400 degrees C in degrees K?

- 2127 K
- 2400 K
- 8.8 K
- 2673 K
- None of the above



What is 2400 degrees C in degrees K?

a. 2127 K  
 b. 2400 K  
 c. 8.8 K  
 d. 2673 K  
 e. None of the above

$Temp (K) = Temp (C) + 273$

### The Kelvin Temperature Scale: Links T to motion

Temperature Scales		
Fahrenheit	Celsius	Kelvin
Boiling Point of Water	100°C	373.15 K
Highest Temp. ever recorded in US	56.7°C	330 K
Room temp.	18°C	291 K
Freezing Point of Water	0°C	273.15 K
	-18°C	255 K
Moon, at its coldest	-173°C	100 K
Absolute Zero	-273°C	0 K

← All motion stops

Temperature (K)

- 10<sup>10</sup> → Hydrogen bomb
- 10<sup>7</sup> → Interior of the Sun
- 10<sup>6</sup> → Solar corona
- 10<sup>3</sup> → Surface of the Sun
- 10<sup>2</sup> → Copper melts
- 10<sup>1</sup> → Water freezes
- 10<sup>0</sup> → Liquid nitrogen
- 10<sup>-1</sup> → Liquid hydrogen
- 10<sup>-2</sup> → Liquid helium
- 10<sup>-3</sup> → Lowest temperature achieved = 10<sup>-7</sup> K

• 1 degree Kelvin = 1 degree Celsius = 9/5 degree Fahrenheit  
 • 0 degree Celsius = 273 K

Identify spectrum of radiation given off by person (37 C) and a block of barely frozen ice (0 C).

a. 2 is person, 1 is ice,  
 b. 1 is person, 2 is ice,  
 c. None, because ice gives off no thermal radiation,  
 d. 1 is both ice and person because they are almost identical  
 e. 3 is person, one of the others is ice.

Identify spectrum of radiation given off by person (37 C) and a block of barely frozen ice (0 C).

b. 1 is person, 2 is ice,

Anything with a non-zero temperature emits EM radiation. The ice and the person are both so cold that the radiation is not visible. The person is a bit hotter than ice, so gives off more radiation ( $\propto T^4$ ), and has peak power at a slightly shorter  $\lambda$ . ( $\propto 1/T$ ).

The plot above shows the BB spectrum of an object at the temperature of a typical lightbulb. Why is the lightbulb <20% efficient?

a. Not all of the electrical power going into the lightbulb gets converted into EM power  
 b. Less than 20% of the electrical power in gets converted to IR power  
 c. All the electrical power going in gets converted to EM power but less than 20% is at visible wavelengths  
 d. Visible light is at shorter wavelengths and therefore doesn't contain EM energy  
 e. The surface area of the lightbulb filament is too small for an efficient conversion of electrical power to visible EM power.

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What type of EM radiation is emitted from the surface of the earth?

- Primarily UV
- Primarily visible
- Primarily IR
- IR and visible
- All parts of the EM spectrum at roughly equal intensities

$\lambda_{\text{max}} \sim 1/T$

Remember to use T in K

What type of EM radiation is emitted from the surface of the earth?

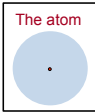
- Primarily UV
- Primarily visible
- Primarily IR
- IR and visible
- All parts of the EM spectrum at roughly equal intensities

Look at [BB phet](#) at temperature of earth

### Source of electricity: Electric charges

Everything (earth, you, the table etc) made of tiny particles called atoms  
Atoms are made up of 3 even tinier particles:  
Electrons, neutrons and protons

Particle	Charge	Mass
Electron	-e	$9.11 \times 10^{-31}$ kg
Proton	+e	$1.67 \times 10^{-27}$ kg
Neutron	0	$1.67 \times 10^{-27}$ kg



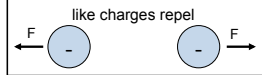
The atom

$e = 1.6 \times 10^{-19}$  Coulombs  
Coulomb (C) is the unit of charge

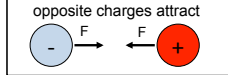
**Static electricity:** What happens when charges are stationary  
**Electricity (and electric currents):** What happens when charges (usually electrons) are moving

### Putting this together: Electric Force

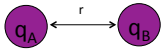
like charges repel



opposite charges attract



Consider 2 'point' charges, A and B. What force does charge A feel?



Observed behavior:

- Force depends on  $q_A$  and  $q_B$ : More charge, more force
- Force depends on distance between them ( $r$ ): less distance, more force

**Coulomb's Law:**  
Force of B on A =  $\frac{kq_Aq_B}{r^2}$

- Describes the force between 2 point charges
- k is Coulomb constant =  $8.99 \times 10^9$  N m<sup>2</sup>/C<sup>2</sup>
- $q_A$  and  $q_B$  are amount of charge in coulombs (C)
- r is separation in m

**1 Coulomb =  $6 \times 10^{18}$  electron charges!**

[Electric Hockey Simulation!](#)

$\text{Force of B on A} = \frac{kq_Aq_B}{r^2}$

Place charge (B) 2cm from charged puck (A). See charged puck fly away

Now place charge (B) 1 cm away from charged puck (A).  
Compared to previous situation force on A will be:

- half as large
- same size
- twice as large
- four times larger
- something else.

d. four times larger since force depends on  $1/r^2$   
⇒ distance smaller, force larger

Place charge (B) 1cm away from charged puck (A) as in previous Q.  
Add a second charge to B, right on top of first.  
Compared to previous question, force on A is:

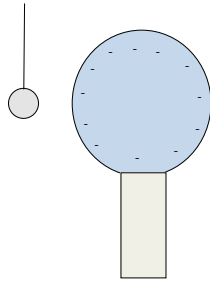
- ½
- same
- x 2
- x 4
- something else.

c. x 2 because force on A goes like (charge of A x charge of B),  
... in this Q we doubled the charge on B

Bring uncharged metalized mylar balloon up to Van de Graaff.

**Predict** what will happen:

- Before it touches
  - Not affected by VdG
  - Attracted to it
  - Repelled
- After touching
  - Not affected by VdG
  - Attracted to it
  - Repelled



Bring uncharged metalized mylar balloon up to Vandergraft.

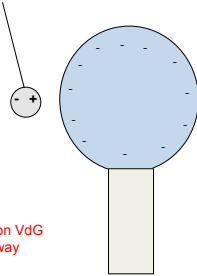
**Predict what will happen:**

- Before it touches
- After it touches

1. Before touching

- Not affected by VdG
- Attracted to it**
- Repelled

- Charges in neutral ball are polarized by - charge on VdG
- + charges move closer to VdG, - charges move away
- Force between charges =  $\frac{kq_1q_2}{r^2}$
- + charges on ball are closer to VdG, so force of attraction is strongest



Bring uncharged metalized mylar balloon up to Vandergraft.

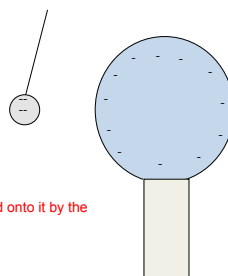
**Predict what will happen:**

- Before it touches
- After it touches

2. After touching

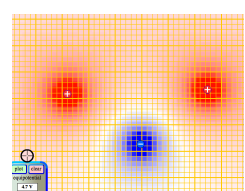
- Not affected by VdG
- Attracted to it
- Repelled**

- When balloon touches, - charges are pushed onto it by the other - charges on the VdG
- Now balloon is negatively charged like VdG
- Like charges repel



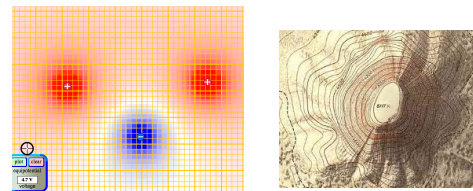
### Voltage has to do with conditions of system

- Amount of charge
- Distance from that charge
- Like the electric force (related but different)



### Voltage is like the height of mountain

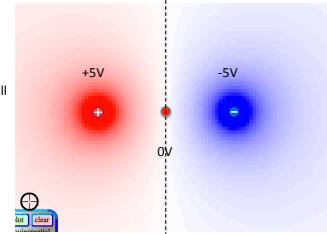
- Think Topographical maps



### Voltage tells you what a + charge will do

+V is like top of hill  
-V is like valley

Where is 0 V?



What will a +q do at 0V:


- Be attracted to higher voltage
- Be attracted to lower voltage
- Not be impacted

b) Just like a ball rolls down hill

### Voltage is like the height of mountain

- Voltage
- Charge, q
- Electrical Potential Energy
- Height (and gravity)
- Mass, m
- Gravitational potential Energy

EPE = q ΔV      GPE = m g Δh



Two metal plates connected by a battery.  
Battery maintains a voltage difference of  $V$  between the plates

Plate A is grounded (set to zero  $V$ )  
What is the voltage of plate B?

- 0
- $+V$
- $-V$
- Can't determine from information given

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Plate A is grounded (set to zero  $V$ )  
What is the voltage of plate B?

- 0
- $+V$
- $-V$
- Can't determine from information given

Note: Conductors (bits of metal, wires etc) are a constant voltage all over

What will happen to the charge  $q$  if we let go of it (ignore gravity)?

- Nothing
- It will fly over to plate A
- Sparks will fly
- Something else

What will happen to the charge  $q$  if we let go of it (ignore gravity)?

- Nothing
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- Sparks will fly
- Something else

$q$  has a  $+$  charge. It will be repelled by  $+$  charges on plates B and attracted to  $-$  charges on plate A

**Electrostatic potential energy and voltage**

New force: Electrostatic force between charges  
New PE: Electric Potential Energy (EPE)

Forces and PE go in pairs - Remember gravitational force:  
- Do work against gravitational force ( $mg$ ) to raise an object's GPE ( $mgh$ )  
- Similarly, do work against electric force to raise an object's EPE

$EPE = q \Delta V$ , where  $q$  = charge of object and  $\Delta V$  is voltage difference  
Like GPE with  $q \leftrightarrow m$  and  $\Delta V \leftrightarrow \Delta h$

Voltage ( $V$ )

- tells you EPE of any charge at that location in space
- Tells you work required to bring a unit charge from  $V = 0$  to that location
- Determined by surrounding charges.  
Closer you are to  $+$  charge the more  $+$  the voltage
- A grounded object is always at  $V = 0$
- Usually most interested in  $\Delta V$ : voltage difference between 2 locations

**Best understood by doing practice questions!**

**Electrostatics Summary**

- Positive and negative charge: Like charges repel, opposites attract
- Coulombs law for point charges:  $F = \frac{k q_A q_B}{r^2}$   
Force acts along line joining particles
- Voltage: Determines EPE of charge at that location in space  
Close to  $+$  charges voltage is more  $+$  and vice versa  
Grounded object is at  $0V$   
(Also called Electric Potential)
- EPE:  $= q\Delta V$   
New form of potential energy  
Lots of analogies to GPE ( $\Delta V \leftrightarrow \Delta h$ ,  $q \leftrightarrow m$ )

### Flashlights, circuits, batteries, and power

- Given batteries, light bulbs, and wire, how can we design a light bulb circuit
  - that will burn brightest,
  - that will last longer,
  - that will be dim,
  - that will turn on and off.
- How can you control and predict current and power in light bulbs?
- All this basic circuit stuff applies to home wiring, home electronics, heaters etc.
- Thursday lecture ... help save lives ... physics of dangers of electrocution.

**Builds on electrostatics (like charges repel, opposite charges attract, voltage, EPE)**  
 .....but now electrons are moving.....  
 ..... need to start thinking like an electron!

### Electric circuits: some important ideas

- Current is conserved (electrons don't appear/disappear)
- Change in V over circuit = V of battery, or energy source
- $V = IR$  (Ohm's law)
  - useful for whole circuit ( $R_{total}, V_{total},$  give  $I_{total}$ )
  - or individual component (e.g.  $R_{bulb}, V_{bulb}$  give  $I_{bulb}$ ),
  - .....Don't mix and match.
- $P = IV = I(IR) = I^2R$  } power dissipated by resistance R  
 =  $(V/R)V = V^2/R$  }
- Resistors in series:
  - Resistances add:  $R_{tot} = R_1 + R_2$
  - Current through all resistors is the same
- Resistors in parallel:
  - Voltage drop across parallel legs of circuit is same

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### light bulb circuit: Wiring

What will happen when hook up battery to flashlight bulb with 2 wires as shown?

a. light up   b. barely light up   c. not light up

### light bulb circuit: Wiring

What will happen when hook up battery to flashlight bulb with 2 wires as shown?

a. light up   b. barely light up   c. not light up

**Complete circuit:** electrons are able to flow all the way around and back into battery, producing a steady current (I)

If there is a break in the circuit they will pile up at the break and push back (Coulomb's law) preventing any more from flowing (I=0)

Electrons must have a complete conducting circuit to flow

### light bulb circuit: Battery

Voltage difference between ends of battery... 1.5 Volts, 9 Volts, 12 Volts

$\Delta EPE = q \Delta V$

What happens to EPE of electrons as they flow around the loop?

- EPE is always the same.
- EPE increases through battery; EPE decreases through circuit.
- EPE decreases through battery; EPE increases through circuit.

### Circuit elements summary

**Wires:** Make complete circuit necessary for steady flow of electrons  
 Usually have negligible (zero) resistance

**Battery:** Has positive charges piled up at one terminal and negative charges at the other  
 Provides voltage difference  $\Delta V$  around circuit  
 Provides each electron with  $q \Delta V = eV$  of EPE to spend in circuit  
 Provides push for electrons around circuit (bigger V, bigger push)

**Bulb:** Filament is a high resistance wire in which electrons lose their energy as heat

### Energy changes in circuit

**Battery:**  
Chemical to EPE of electrons

**In circuit wires:**  
EPE to KE of electrons

**In bulb:**  
KE of electrons to thermal energy (random KE) of filament atoms

**Filament surface:**  
Thermal energy of filament atoms to radiated energy (light)

**In Battery:**  
heat and light

### This is a task for Electron man!

Circuits – Think like an electron

**Useful tip:**  
In questions, assume connecting wires have zero R and e<sup>-</sup> lose zero energy in them, unless told otherwise

- Same current through connecting wires and filament.
- $R_{\text{filament}} \gg R_{\text{wires}}$
- Almost all energy lost in filament.

### Circuit language

**Resistance (R)** of a circuit element is measure of how hard it is for electrons to pass through.  
Units: Ohms ( $\Omega$ )

**Current (I)**: charge per second flowing past a point in the circuit  
(= # electrons per second  $\times$  charge on electron)  
Units: Amps (1 A = 1 C/s)

**Voltage (difference) ( $\Delta V$ )**

a) **Across battery:** Measure of EPE given to each e<sup>-</sup> as it passes through battery. EPE given = eV. Related to pushing force on electrons in circuit

b) **Across a resistor (wire, filament etc):** Measure of EPE lost by each e<sup>-</sup> as it passes through. EPE lost = eV.  
Unless told otherwise voltage difference across connecting wire = 0.  
Units: Volts (V)

**Ohm's Law:  $\Delta V = IR$**

- Resistance of component
- Current through component
- Voltage dropped across component

**Note:** All quantities specific to one component. Don't mix and match!

### Batteries in series (nose to tail)

Compare the brightness of the bulbs in case 1 and case 2.  
All bulbs and batteries are identical

- Case 2 twice as bright as case 1
- Case 2 same brightness but runs twice as long
- Case 2 **more** than twice as bright as case 1
- Case 2 produces no light

### Batteries in series (nose to tail)

c. case 2 is more than twice as bright

Electrical power into bulb = EM power out.

Method 1:  $P_{\text{in}} = \Delta V_{\text{bulb}}^2 / R$

Case 1:  $P_{\text{in}} = \Delta V^2 / R$

Case 2:  $P_{\text{in}} = (2 \Delta V)^2 / R = 4 \Delta V^2 / R$

(In addition, since filament is hotter in case 2 a greater fraction of the radiated EM power is in visible range.)

Method 2:  
 $P_{\text{in}} = I_{\text{bulb}} \times \Delta V_{\text{bulb}}$   
Both I and V double in case 2  $\Rightarrow P_{\text{in}} = \times 4$

### Batteries in parallel

Compare the brightness of the bulbs in case 1 and case 2.  
All bulbs and batteries are identical

- 2 twice as bright as 1
- 2 same brightness
- 2 more than twice as bright as 1
- 2 produces no light

**Batteries in parallel**

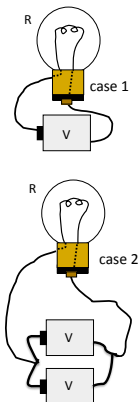
Compare the brightness of the bulbs in case 1 and case 2.  
All bulbs and batteries are identical

a. 2 twice as bright as 1  
b. **2 same brightness**  
c. 2 more than twice as bright as 1  
d. 2 produces no light

**Why?**  
Think like an electron.  
In either battery in case two, the electron has the same Electric potential energy =  $EPE = q \Delta V$

Note: an electron doesn't get to go through both batteries, it's one or the other

Same energy to deposit in identical bulbs  
**What is the difference then?**



**Batteries in parallel**

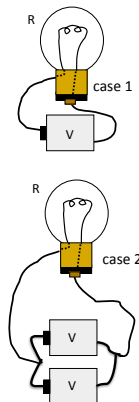
**What is the difference then?**

Each battery can produce a given amount of Current (electrons/ second) for a certain amount of time

Note: rating on batteries is in Amp-Hours! (what is an amp-hour?)

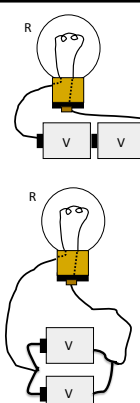
Zoinks.. With two batteries I have a greater reservoir of electrons to draw from.

Case 2: last twice as long!



**Summary:**  
- Series: more energy for each electron! (brighter) how you make a 9 V out of D-Cells, or AAAs

- Parallel: longer lasting difference between AAAs and D cells



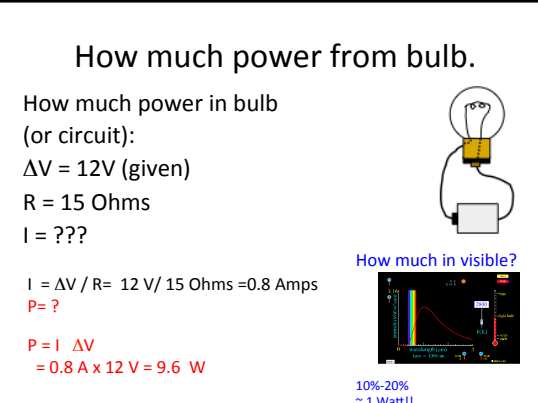
**How much power from bulb.**

How much power in bulb (or circuit):  
 $\Delta V = 12V$  (given)  
 $R = 15 \text{ Ohms}$   
 $I = ???$

$I = \Delta V / R = 12 V / 15 \text{ Ohms} = 0.8 \text{ Amps}$   
 $P = ?$

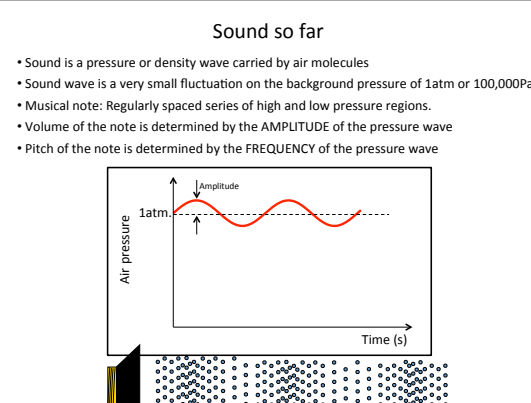
$P = I \Delta V = 0.8 A \times 12 V = 9.6 \text{ W}$

How much in visible?  
10%-20%  
~ 1 Watt!!



**Sound so far**

- Sound is a pressure or density wave carried by air molecules
- Sound wave is a very small fluctuation on the background pressure of 1atm or 100,000Pa
- Musical note: Regularly spaced series of high and low pressure regions.
- Volume of the note is determined by the AMPLITUDE of the pressure wave
- Pitch of the note is determined by the FREQUENCY of the pressure wave



**Thinking about waves:**

Frequency (f)	# of oscillations/sec	(Hz = 1/s)
Wavelength ( $\lambda$ )	Distance of one complete cycle	(m) (e.g. distance between pressure maximums)
Period (T)	Time for one complete oscillation	(s)
Speed (v)	Distance traveled per second	(m/s)

**Relationships among these variables:**  
 $v = \lambda \times f$   
 Distance per second = distance per oscillation  $\times$  # of oscillations per second  
 $f = 1/T$   
 # oscillations per second = 1/time for one oscillation  
 $v = \lambda / T$

**Volume and amplitude**

**Question: If I increase the volume, what will happen to the signal from the microphone?**

- The peaks will go up and the valleys will go down.
- The peaks will get closer together.
- The whole signal will go up.
- Both a and b.
- Nothing will happen

DO EXPERIMENT....

**How to change the pitch (note) of the speaker?**

To get a higher pitch sound, we need to adjust the speaker to:

- vibrate back and forth more rapidly, taking a smaller amount of time for each cycle
- vibrate back and forth at the same rate as before, but the range of it's back and forth motion is larger.
- receive more power
- vibrate back and forth more slowly, taking a longer amount of time for each cycle
- vibrate back and forth at the same rate as before, but the range of it's back and forth motion is smaller.

What if we wanted to change the pitch of the tone produced by the speaker?

To get a higher pitch sound, we need to adjust the speaker so that:

- It vibrates back and forth more rapidly, taking a smaller amount of time for each cycle
- It vibrates back and forth at the same rate as before, but the range of it's back and forth motion is larger.
- It receives more power
- It vibrates back and forth more slowly, taking a longer amount of time for each cycle
- It vibrates back and forth at the same rate as before, but the range of it's back and forth motion is smaller.

In physics/wave language this is called adjusting the **frequency (f)**

**How do we get notes of different pitch from a violin?**

Get the strings to vibrate at different frequencies  
 ⇒ Must control the vibrations or 'wave motion' of the strings

Remember, for ANY wave:  $v = f \times \lambda$

Frequency (pitch) of violin note  $\Rightarrow f = v / \lambda$  ← Wavelength of string motion  
 Speed of wave (on string)

To change the pitch (frequency) of a note we can

- Change  $v$  - the speed of waves on the string  
 - change thickness or tension of the string
- Change  $\lambda$  - the wavelength  
 - change the length of the string

a) Changing pitch by **speed of waves** on a string

$$v_{\text{string}} \sim \frac{F_T}{m_L} \quad f = \frac{v_{\text{string}}}{\lambda}$$

- How do violinists tune their strings?
  - Adjust the tension ( $F_T$ )
  - Mass on spring tells us:
    - Increasing  $F_T$  like increasing the stiffness of the spring (same mass)
    - Bigger spring force ⇒ accelerates and oscillates more quickly
- Why does the G string produce a lower note than the E string?
  - G string is thick ⇒ large mass per length ( $m_L$ )
  - E string is thin ⇒ small mass per length
  - Mass on spring expts:
    - Thicker string like bigger mass (same spring)
    - More mass ⇒ accelerates and oscillates more slowly

b) Change note by **Wavelength of waves** on a string

If we could only control the frequency of a violin string with thickness and tension, the violin would have 4 notes.....

But,  $f = \frac{v_{\text{string}}}{\lambda}$  so we can also change the frequency by changing the wavelength

Simplest or fundamental oscillation of a violin string

How much of a wavelength does this fundamental motion demonstrate?

- 1 wavelength
- 2 wavelengths
- ¼ wavelength
- ½ wavelength

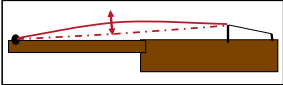


### Wavelength of waves on a string

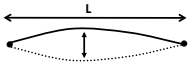
If we could only control the frequency of a violin string with thickness and tension, the violin would have 4 notes....

$$f = \frac{v_{\text{string}}}{\lambda}$$

So we can also change the frequency by changing the wavelength



Simplest or fundamental oscillation of a violin string



How much of a wavelength does this fundamental motion demonstrate?

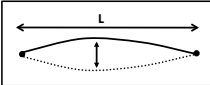
- 1 wavelength
- 2 wavelengths
- 1/4 wavelength
- 1/2 wavelength

### Wavelength of waves on a string

If we could only control the frequency of a violin string with thickness and tension, the violin would have 4 notes....

$$f = \frac{v_{\text{string}}}{\lambda}$$

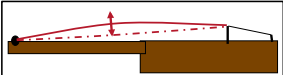
So we can also change the frequency by changing the wavelength



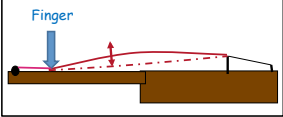
$$L = \frac{1}{2} \lambda \Rightarrow \lambda = 2L$$

$$\Rightarrow f_1 = \frac{v_{\text{string}}}{\lambda_1} = \frac{v_{\text{string}}}{2L}$$

- Fundamental wavelength and hence frequency directly related to length of string
- Can change fundamental frequency by shortening the string with fingers
- Fundamental frequency of string determines that pitch that we hear

$$f_1 = \frac{v_{\text{string}}}{\lambda_1} = \frac{v_{\text{string}}}{2L}$$


Longer string  
Longer wavelength,  
lower frequency

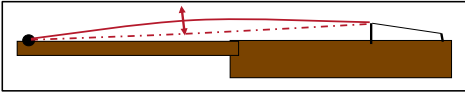


Shorter string  
Shorter wavelength  
Higher frequency

DEMO CAPO

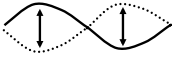
### Harmonics

- String is tied down at each end.
- It oscillates back and forth.
- The simplest way for the string to flex is like this:

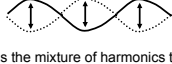


Fundamental frequency, 1<sup>st</sup> harmonic.  
 $f_1 = v_{\text{string}}/2L$

But it can also flex in more complicated ways and we call these higher harmonics



2<sup>nd</sup> harmonic:  
half the wavelength, twice the frequency  
 $f_2 = 2f_1 = v_{\text{string}}/L$



3<sup>rd</sup> harmonic:  
third the wavelength, three times the frequency,  
 $f_3 = 3f_1 = 3v_{\text{string}}/2L$

It is the mixture of harmonics that each instrument produces along with the fundamental that gives it its unique sound

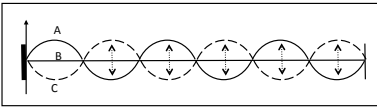
DEMO STANDING WAVE

### More questions on harmonics

A string is clamped at both ends and then plucked so that it vibrates in the mode shown below, between two extreme positions A and C.

Which harmonic mode is this?

- fundamental,
- second harmonic,
- third harmonic,
- 6<sup>th</sup> harmonic




A, B and C are snapshots of the string at different times.

answer: 6<sup>th</sup> harmonic – there are 6 points of maximum displacement along the string

Harmonic demo

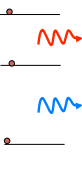
### Review of atom discharge lamps-- neon signs.

Energy levels metal, bulb filament, or not stuck in atom (like sun). If hot, jump between all diff. levels. Wiggle around, all colors.

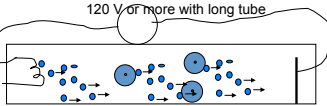


Energy levels in isolated atom.

kick up, only certain wavelengths when come down.



In discharge lamps, lots of electrons given bunch of energy (voltage). Bash into atoms. ("discharge tube")



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### Atomic Models & Light

### Neon / Discharge Lamps Sim

Note: different atoms have different energy levels (orbits for electrons), resulting in different energies of light (colors) coming out

<http://phet.colorado.edu/en/simulation/discharge-lamps>

atoms lazy- always want to go back to lowest energy state. Have to get rid of energy, send it off as light.

1 Fast electron or light hits atom  
or

2 Excited atom

3 Atom back to low energy

Light emitted

Ground state (lowest possible)

#### Important Ideas

- 1) Electrons in atoms only found in specific energy levels
- 2) Different set of energy levels for different atoms
- 3) 1 photon emitted per electron jump down between energy levels. Photon color determined by energy difference.
- 4) electron spends very little time ( $10^{-8}$  s) in excited state before hopping back down to lowest unfilled level.
- 5) If electron not stuck in atom, can have any energy.

Hydrogen      Lithium

Energy

Electron energy levels in 2 different atoms ... Levels have different spacing.

Atoms with more than one electron ... lower levels filled.

(not to scale)

### Laser-- Light Amplification by Stimulated Emission of Radiation

repeated cloning of photons to produce LOTS of identical photons of light.

Requirements: 1) stimulated emission (always have)  
2) population inversion of bunch of atoms (hard)  
3) optical feedback (mirror)

photon, little piece of wave, we often draw as little ball because less work.

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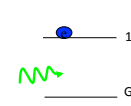
photon, little piece of wave, we often draw as little ball because less work.

Everything to know about interaction of light and atoms. 3 easy steps.

1. absorption of light

2. Spontaneous emission of light. Electron jumps down from upper level, gives off light. Randomly in any direction.

"Stimulated emission" of light. First realized by A. Einstein



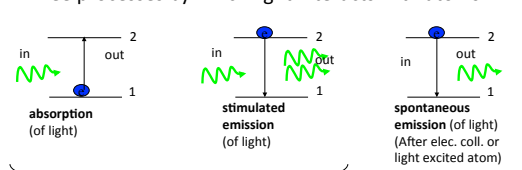
Photon hits atom already in higher energy level.  
original photon continues and atom emits second identical one

photon      atom in excited state

second identical photon comes out. Atom jumps down.  
Cloning photon.

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Three processes by which light interacts with atoms




absorption (of light)      stimulated emission (of light)      spontaneous emission (of light) (After elec. coll. or light excited atom)

Surprising fact. Chance of stimulated emission of excited atom **EXACTLY** the same as chance of absorption by lower state atom. Critical fact for making a laser.

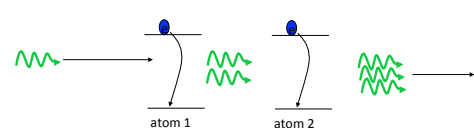
Laser-- just use stimulated emission to clone photon many times ( $\sim 10^{20}$ /sec)  
Light Amplification by Stimulated Emission of Radiation

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what will come out on the right? Think before you pick...  
a. 1 photon, b. 2 photons, c. 3 photons, d. 4 photons, e. 8

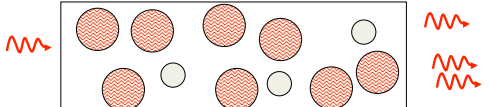
c. 3 Double at first atom, then both hit second but atom only has enough energy to give off one more photon.



atom 1      atom 2

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so now see how to get population inversion, will give amplification of red light. If enough atoms in upper, will lase.



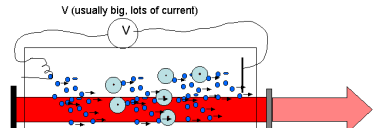
PhET Simulation

But much easier if not let light all escape. Reuse mirror to reflect the light.

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can get amplification, but to really build up to nice high power beam need feedback of mirrors.

Open laser He-Ne with exposed discharge tube and mirrors.



V (usually big, lots of current)

gas laser like Helium Neon.  
Just like neon sign with helium and neon mixture in it and mirrors on end.

Diode laser- same basic idea, but light produced like in light emitting diode at P-N diode junction.

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What have we learned in this section:

- 1) Lasers (pump up to population inversion, put mirrors around it, stimulated emission will take care of the rest)
- 2) For operation, lasers need at least 3 energy levels (ground state and 2 excited states). It helps if the middle level has a long lifetime ("metastable")
- 3) How glow in the dark toys work
- 4) Lots of cool demonstrations. Looked at emission spectra. Disassembled a working laser.

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## Many applications of lasers

- High energy small area:
  - Cutting: surgery, laser welding
  - “communication” (and weapons)



- Focus light into extremely small spot:
  - (diffraction limit, because in phase!)
  - CDs, DVDs, ...



- Collimated beam
  - Tracking, leveling,

- Pure color
  - LIDAR....



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