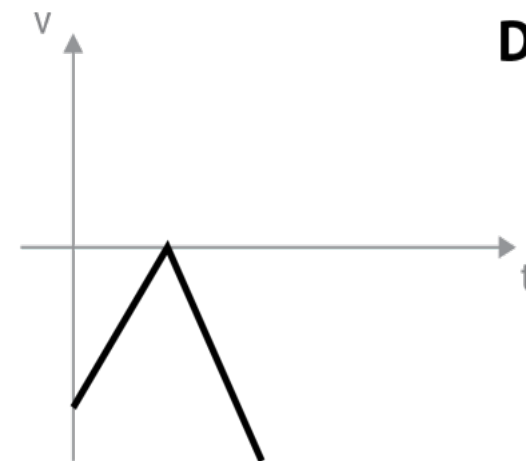
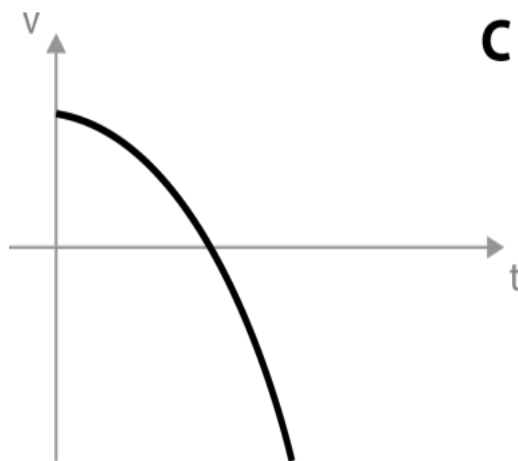
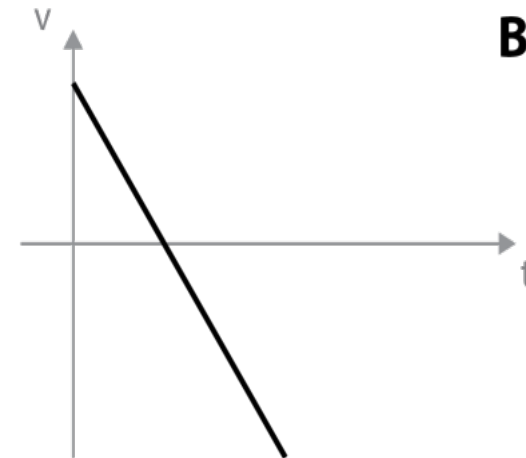
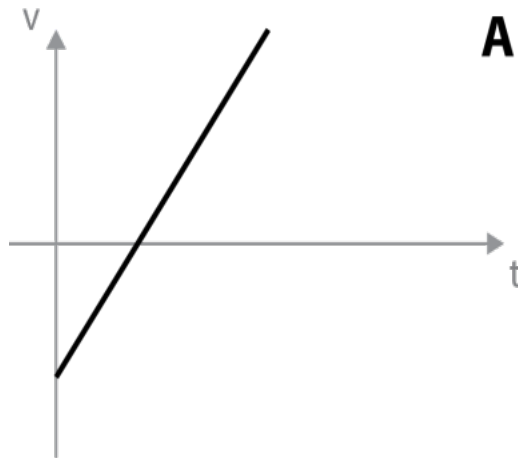


**Spring 2014**

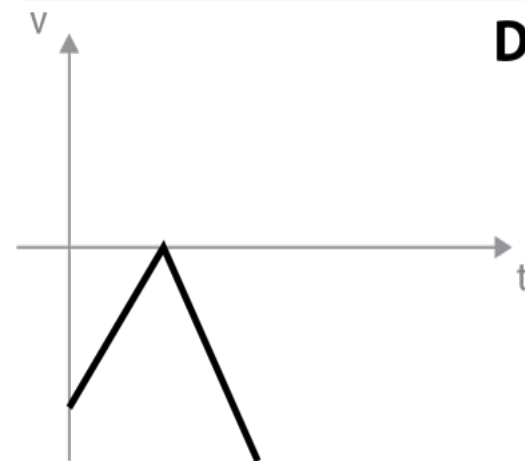
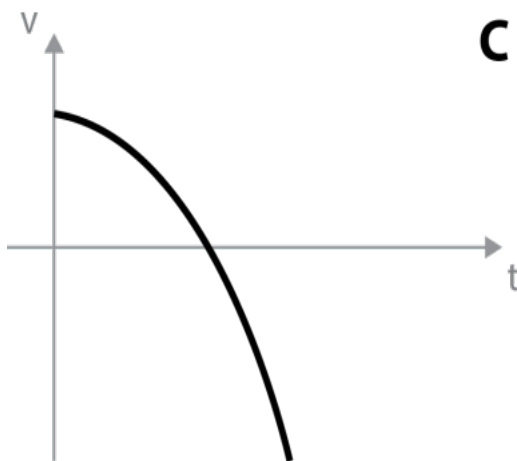
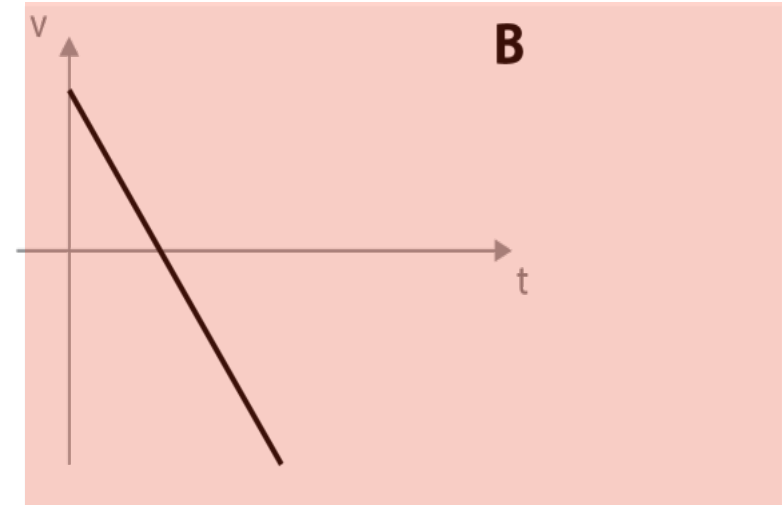
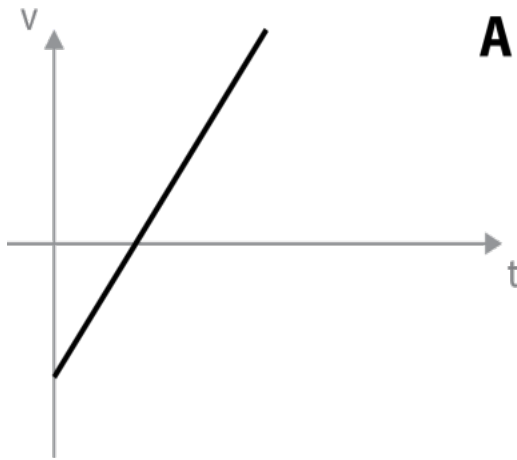
**PHYS-2010**

**Lecture 8**

I throw a ball up in the air (the ball leaves my hand at  $t=0$ ) (+y is up). What does the velocity vs. time graph look like?



I throw a ball up in the air (the ball leaves my hand at  $t=0$ ) (+y is up). What does the velocity vs. time graph look like?



# Announcements

- Read Giancoli Sections 3.1-3.5.
- **CAPA assignment # 3** is due next Tuesday at 11 pm.
- **Written homework # 2** is due today at 4 PM.
- **Midterm Exam 1** will be Thursday, Feb 6, 7:30-9:15 PM.
- **Practice exam** is posted on D2L.
- More details about the exam are on the next slide on the course website:  
[http://www.colorado.edu/physics/phys2010/phys2010\\_sp14/exams.html](http://www.colorado.edu/physics/phys2010/phys2010_sp14/exams.html)
- Special informal **review session** held by Rosemary Wulf on Tue. Feb. 4, 5-6:30 PM, in Duane G125.

# Materials to study for Mid-Term I

- **Giancoli Ch.1 – Ch. 3.4.**
- In-class **Clicker Questions & Lecture Materials.**
- Your **CAPAs.**
- **Written Homeworks 1 & 2.**
- **Recitation Assignments and Lab.**
- **Giancoli web site:** “Practice Questions”, “MCAT Study Guide”, “Practice Problems”. Link on course web site.
- Old **practice exam** posted on D2L.
- Dr. Michael **Dubson’s Chapter Notes** (link on course website).

## Last time ...

We finished discussion of kinematics (description of motion) **in 1D** (Ch. 2):

- Definitions of position, displacement, velocity, acceleration.
- Constant acceleration equations.
- Graphs of position, velocity, acceleration vs. time.

New Topic:

Vectors and 2-dimensional motion  
(Ch. 3)

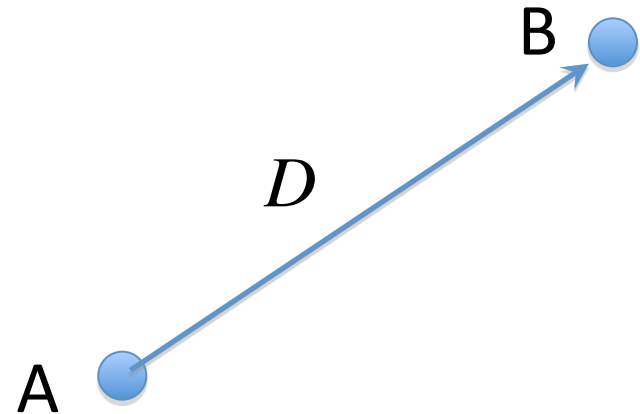
# Expressing motion in 2D: Vectors

Example: Displacement

“net effect of the motion”

represented with a **vector**:

--- a mathematical object with a “*magnitude*” (length) and a “*direction*”.



Other examples of **vectors**:

$$\vec{v}, \vec{a}, \vec{p}, \vec{F}$$

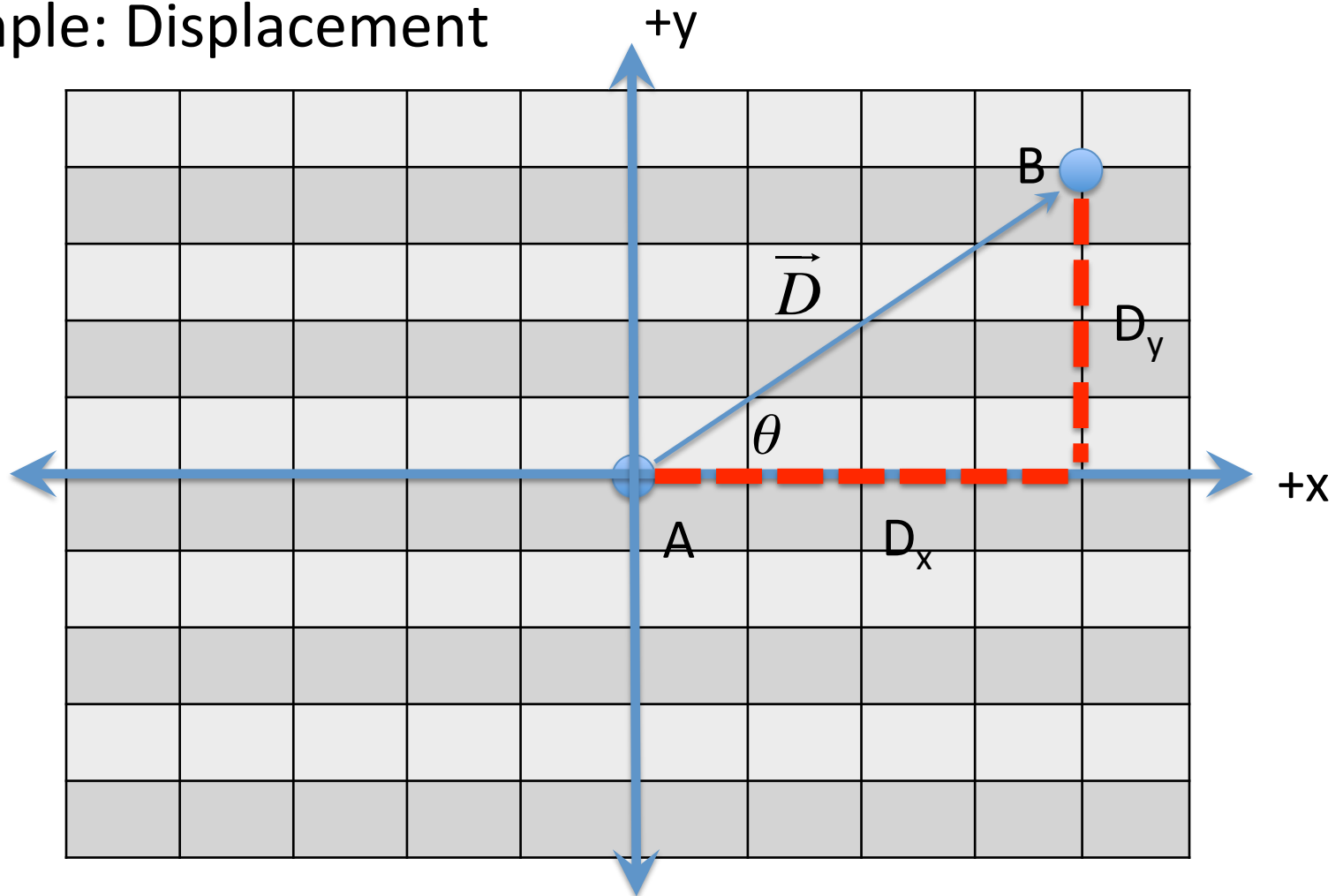
Non-vector quantities are called “scalars”:

$$E, m, W, T, \rho$$



# Components of Vectors

Example: Displacement





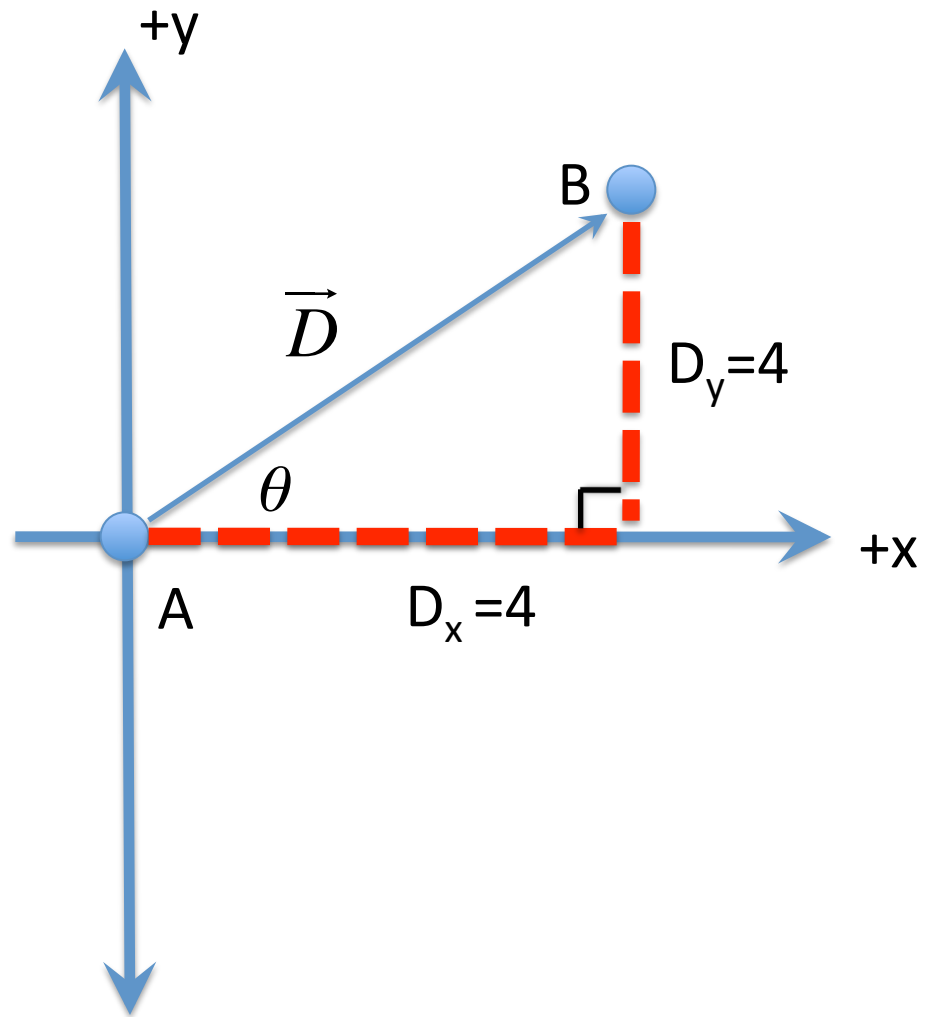
# Magnitude from Vector Components

Example: Displacement

$$\vec{D} = (D_x, D_y) = (4, 4)$$

$$D = |\vec{D}| = \sqrt{D_x^2 + D_y^2}$$
$$= \sqrt{32}$$

Pythagorean Theorem



A displacement vector  $\vec{V}$  has has x-component  $V_x = 4$  km and y-component  $V_y = 3$  km.

What is the length (or magnitude) of the vector  $\vec{V}$  ?

A) 5 km

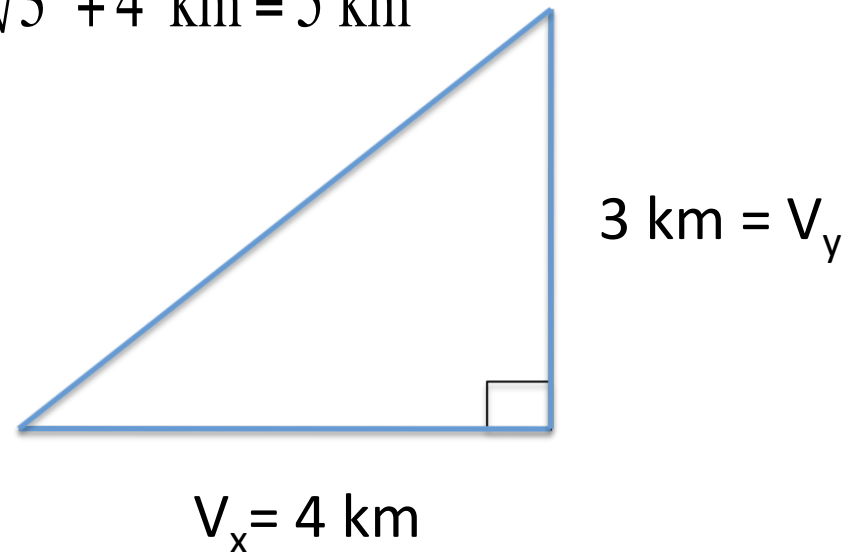
B) 16 km

C) 25 km

D) 32 km

E) 49 km

$$V = |\vec{V}| = \sqrt{3^2 + 4^2} \text{ km} = 5 \text{ km}$$



# Vector Components and Trigonometry

Example: Displacement

$$\sin \theta = o / h \rightarrow o = h \sin \theta$$

$$\cos \theta = a / h \rightarrow a = h \cos \theta$$

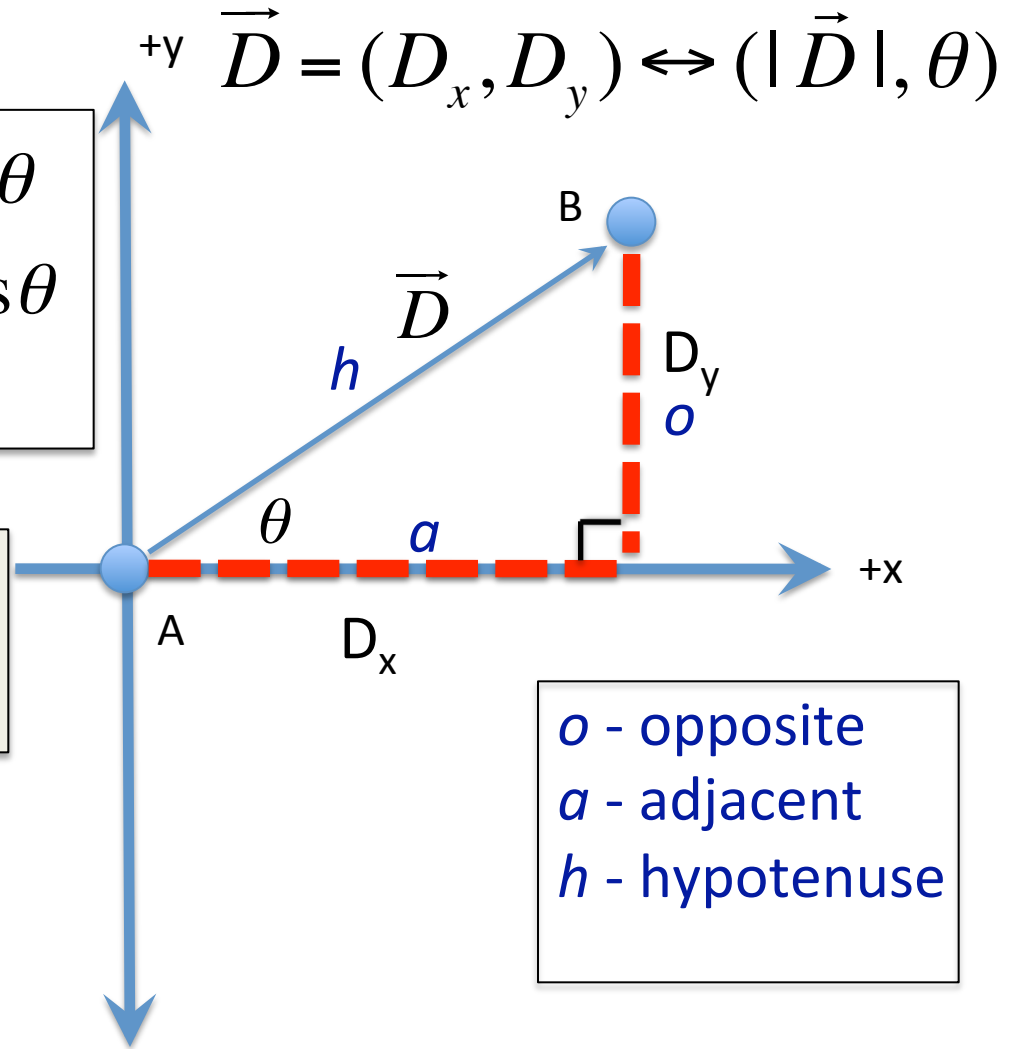
$$\tan \theta = o / a$$

$$\theta = \tan^{-1}(o / a)$$

= “angle whose tangent is o/a”

Angles measured in  
degrees or radians:

$$2\pi \text{ rad} = 360^\circ$$



$o$  - opposite  
 $a$  - adjacent  
 $h$  - hypotenuse

Angle  $\theta = \pi/4$  radians. What is the measure of  $\theta$  in degrees?

- A)  $30^\circ$
- B)  $45^\circ$
- C)  $60^\circ$
- D)  $90^\circ$
- E)  $180^\circ$

$$\pi = 180 \text{ deg}$$

$$\pi/4 = 180/4 = 45 \text{ deg}$$

Consider the triangle below. Which one of the following is correct?

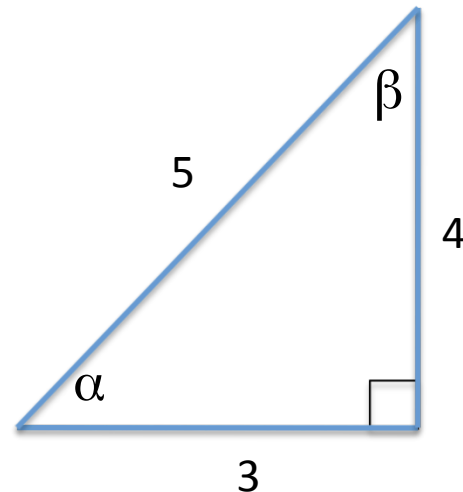
A)  $\cos \alpha = 4/5$

B)  $\sin \alpha = 3/5$

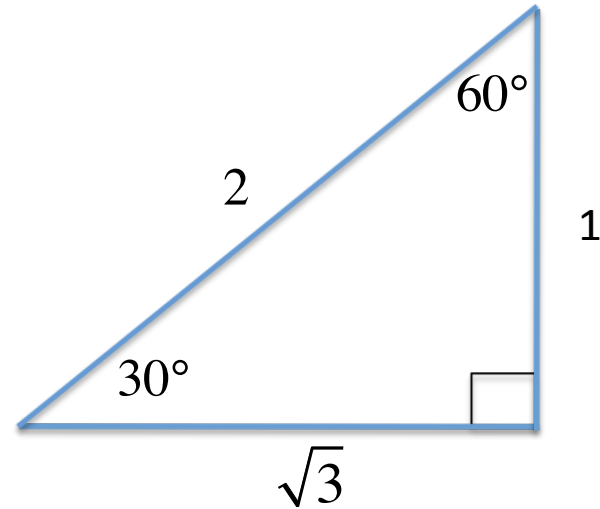
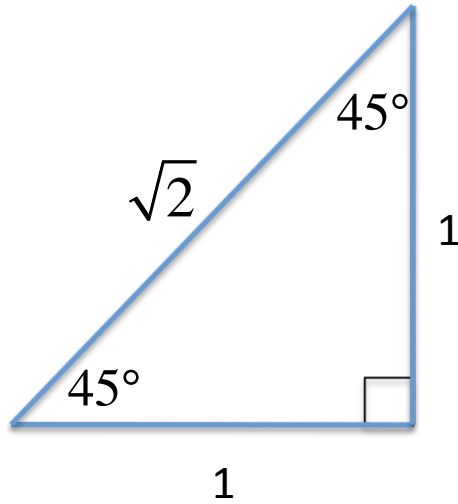
C)  $\sin \beta = 4/5$

D)  $\cos \beta = 3/4$

E)  $\tan \alpha = 4/3$



# Special Triangles:



$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}} \left( \frac{\sqrt{2}}{\sqrt{2}} \right) = \frac{\sqrt{2}}{2}$$



# Components $\leftrightarrow$ Length, Angle

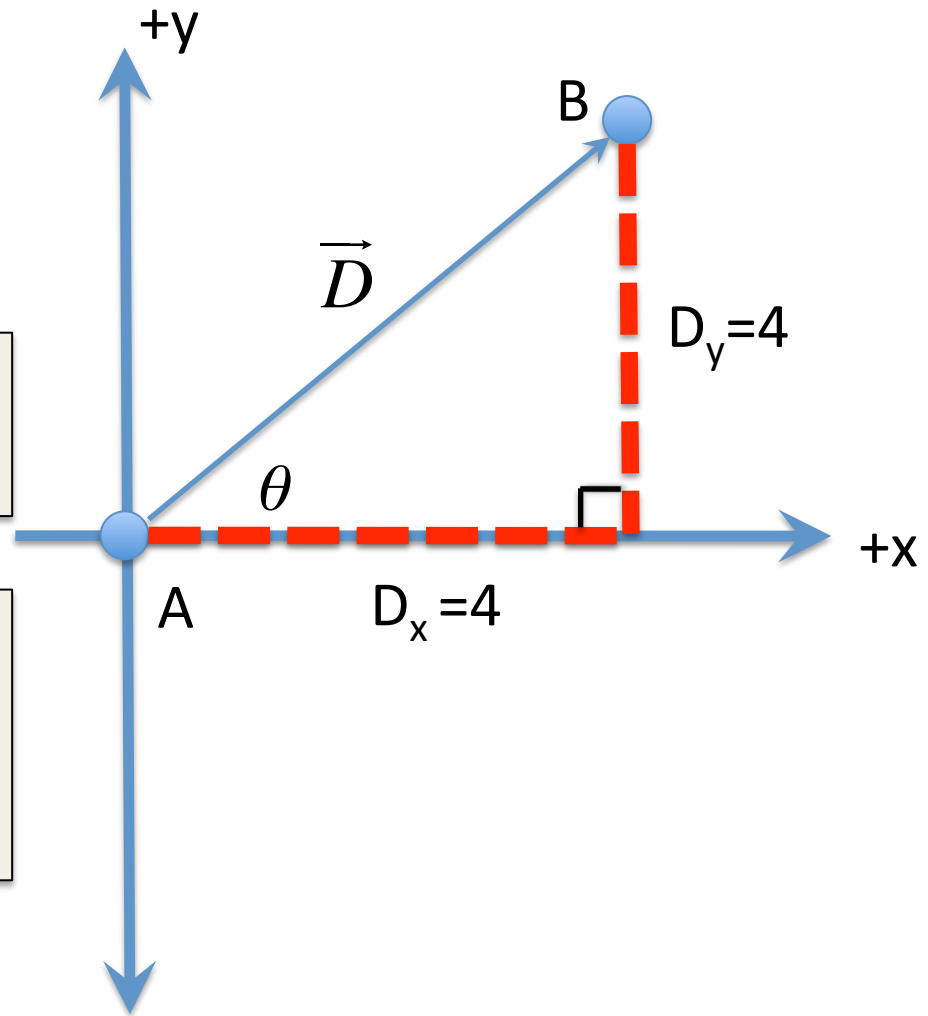
$$\vec{D} = (D_x, D_y) = (4, 4)$$

$$D = |\vec{D}| = \sqrt{D_x^2 + D_y^2} = \sqrt{32}$$

(Pythagorean Theorem)

$$\theta = \tan^{-1}\left(\frac{D_y}{D_x}\right) = \tan^{-1}(1) = \frac{\pi}{4} = 45^\circ$$

$$D_x = |\vec{D}| \cos \theta \quad \& \quad D_y = |\vec{D}| \sin \theta$$
$$= \sqrt{32} \frac{\sqrt{2}}{2} \qquad = \sqrt{32} \frac{\sqrt{2}}{2}$$



What is the correct formula for  $A_y$ , the y-component of the vector? (Note:  $A > 0$  is the length of the vector.)

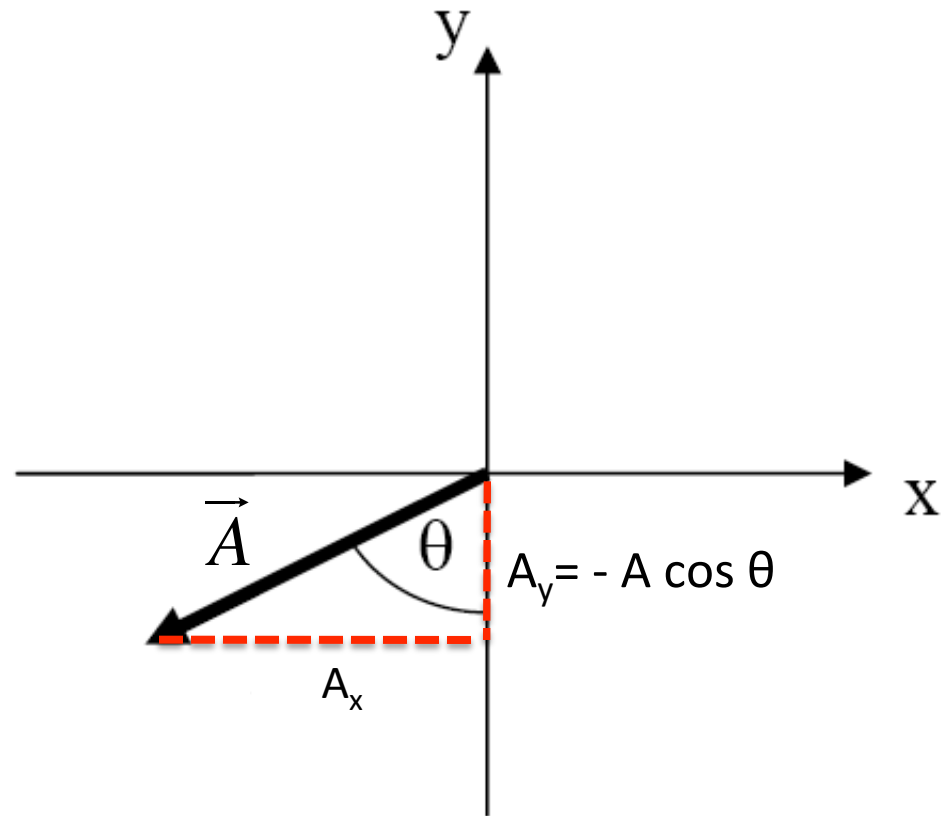
A)  $+A \cos\theta$

B)  $+A \sin\theta$

C)  $-A \cos\theta$

D)  $-A \sin\theta$

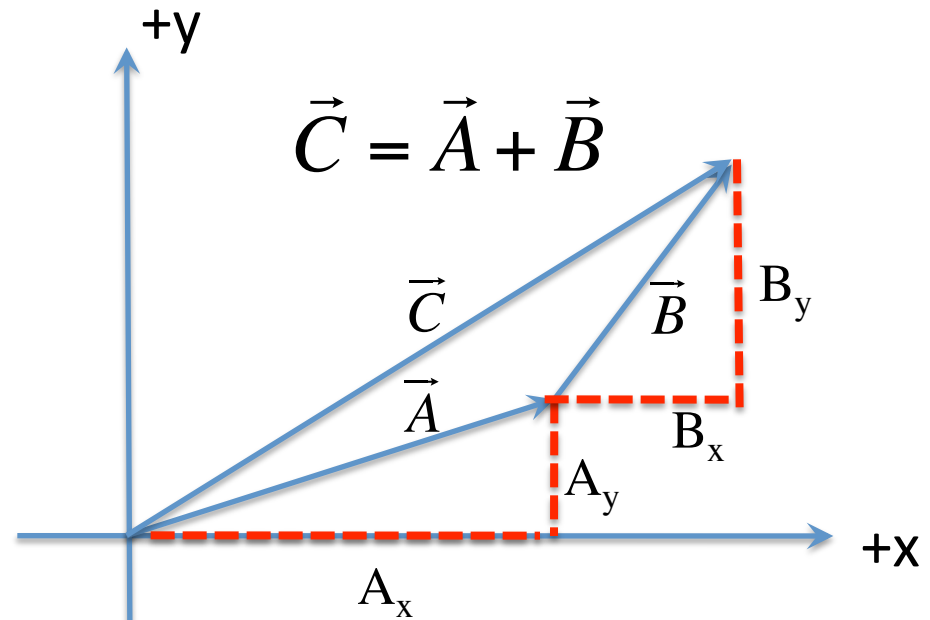
E) None of these.



# Vector Addition I

## Add components:

$$\begin{aligned}\vec{C} &= \vec{A} + \vec{B} \\ &= (A_x, A_y) + (B_x, B_y) \\ &= (A_x + B_x, A_y + B_y)\end{aligned}$$



Head-to-Tail graphical interpretation

For example, walk E 3 blks & N 2 blks.  
Then walk E 2 blks & N 4 blks.  
Result: E 5 blks & N 6 blks.