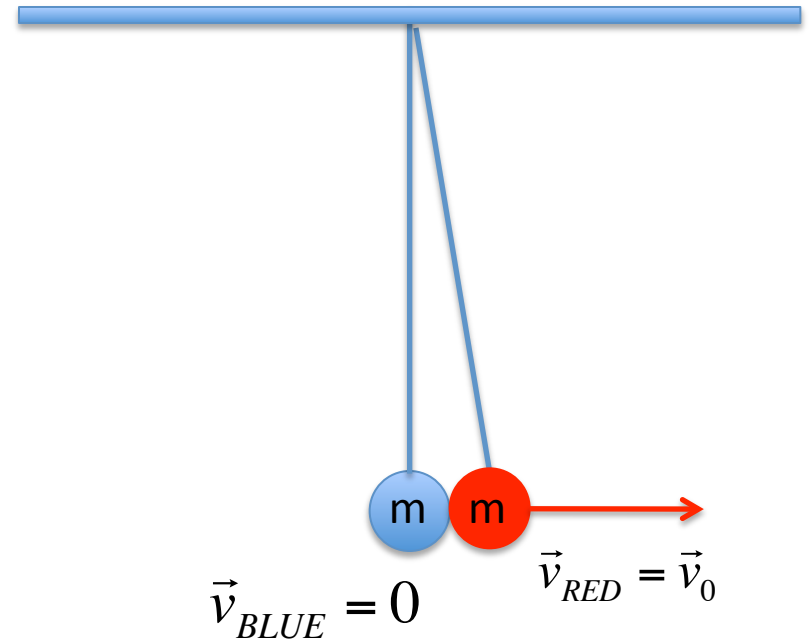
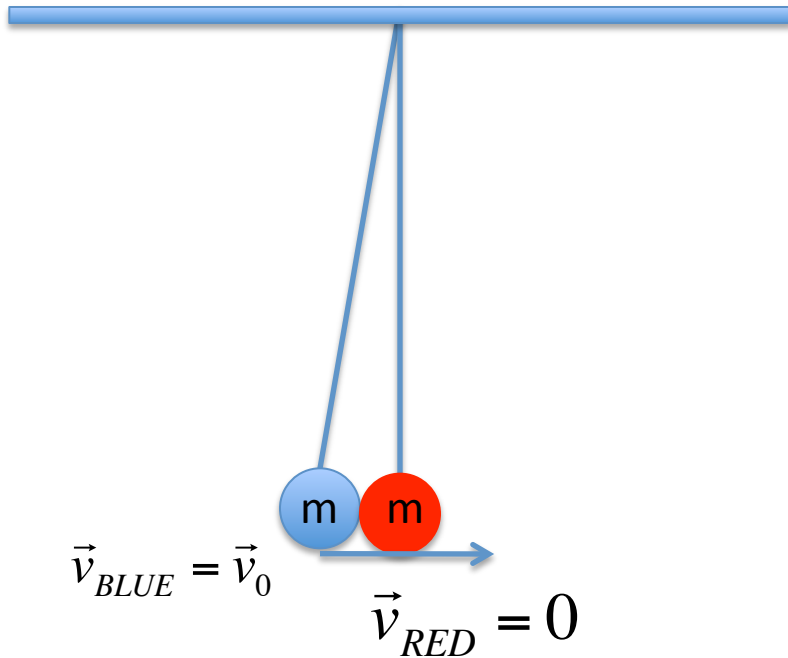


Spring 2014

PHYS-2010

Lecture 30

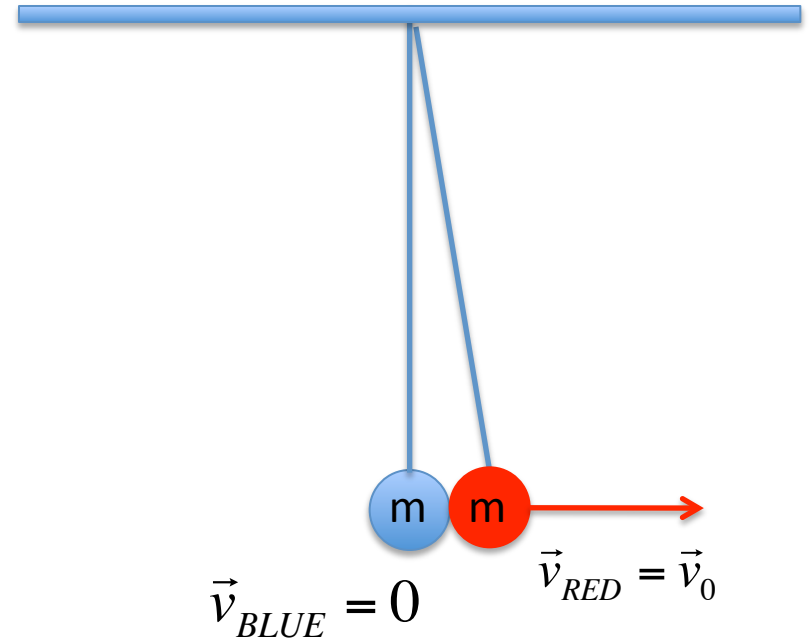
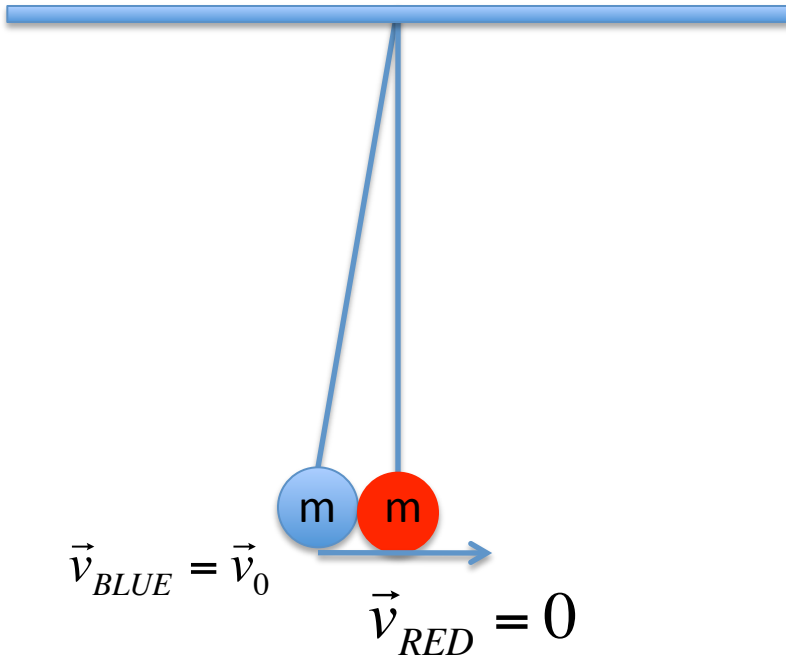
Consider a suspended blue sphere that collides **elastically** with a suspended red sphere of the same mass.



After impact, is the situation at right possible:

- A) Yes
- B) No

Consider a suspended blue sphere that collides **elastically** with a suspended red sphere of the same mass.

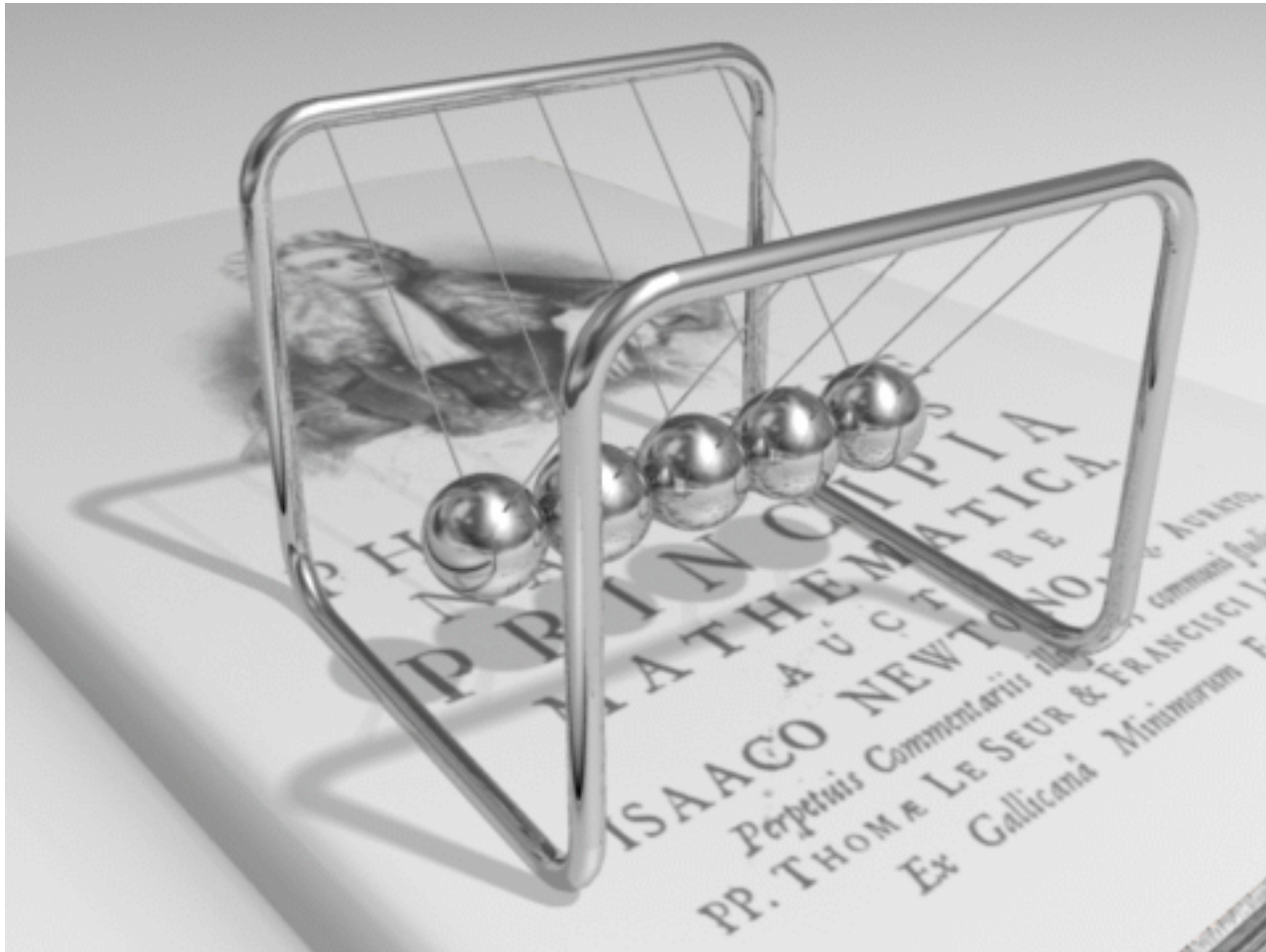


After impact, is the situation at right possible:

A) Yes

B) No

Newton's Cradle



Announcements

- Read Giancoli **Chapter 8 on Rotational Motion**.
- **CAPA 10 deadline postponed until Thur., Apr. 3, 11 pm !!!**
- **Next CAPA # 11 due April 8.**
- **Written Homework # 8 due this Friday, April 4.**
- **This week in Section: Lab # 6 “Momentum” with Prelab.**
- **Next week: Review Recitation and missed Lab make-up.**
 - at least 7 labs are required to pass the course;
 - contact your TA to arrange lab makeup ahead of time. You will need to attend twice: (1) for lab make-up; and (2) for review recitation. You can attend any other section (in addition to your regular one), with that section’s TA advance permission.
- **Study Session by Prof. Pollock: Apr. 1 and 8, 5-6pm, G125.**
- **Midterm Exam 3 on Thursday, April 10, 7:30 pm.**

ROTATIONAL MOTION

Rotational Motion

Motion of a “rigid” body about a fixed axis of rotation.

Translation ↔ Rotation

$$x \leftrightarrow \theta$$

$$v = \frac{\Delta x}{\Delta t} \leftrightarrow \omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r}$$

$$a = \frac{\Delta v}{\Delta t} \leftrightarrow \alpha = \frac{\Delta \omega}{\Delta t} = \frac{a_{\text{tan}}}{r}$$

$$F \leftrightarrow \tau = r F_{\perp}$$

$$M \leftrightarrow I = \sum m r^2$$

$$F_{\text{net}} = M a \leftrightarrow \tau_{\text{net}} = I \alpha$$

$$KE_{\text{trans}} = (1/2) M v^2 \leftrightarrow KE_{\text{rot}} = (1/2) I \omega^2$$

$$p = m v \leftrightarrow L = I \omega$$

$$F_{\text{net}} \Delta t = \Delta p \leftrightarrow \tau_{\text{net}} \Delta t = \Delta L$$

$$\Delta KE + \Delta PE = \text{constant} \leftrightarrow \Delta KE_{\text{trans}} + \Delta KE_{\text{rot}} + \Delta PE = \text{constant}$$

Conservation of mechanical energy

NII for rotations

Conservation of angular momentum



Rotational Motion

Motion of a “rigid” body about a fixed axis of rotation.

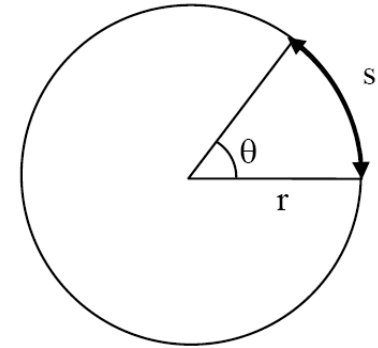
Translation \leftrightarrow Rotation

x

\leftrightarrow

θ

angle of rotation (rads)

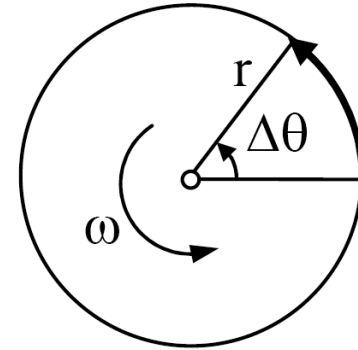


polar coordinates

Rotational Motion

Motion of a “rigid” body about a fixed axis of rotation.

<u>Translation</u>	\leftrightarrow	<u>Rotation</u>
x	\leftrightarrow	θ
$v = \frac{\Delta x}{\Delta t}$	\leftrightarrow	$\omega = \frac{\Delta \theta}{\Delta t}$
		angular velocity (rad/s)

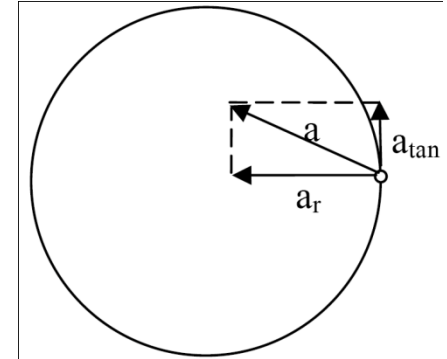


Rotational Motion

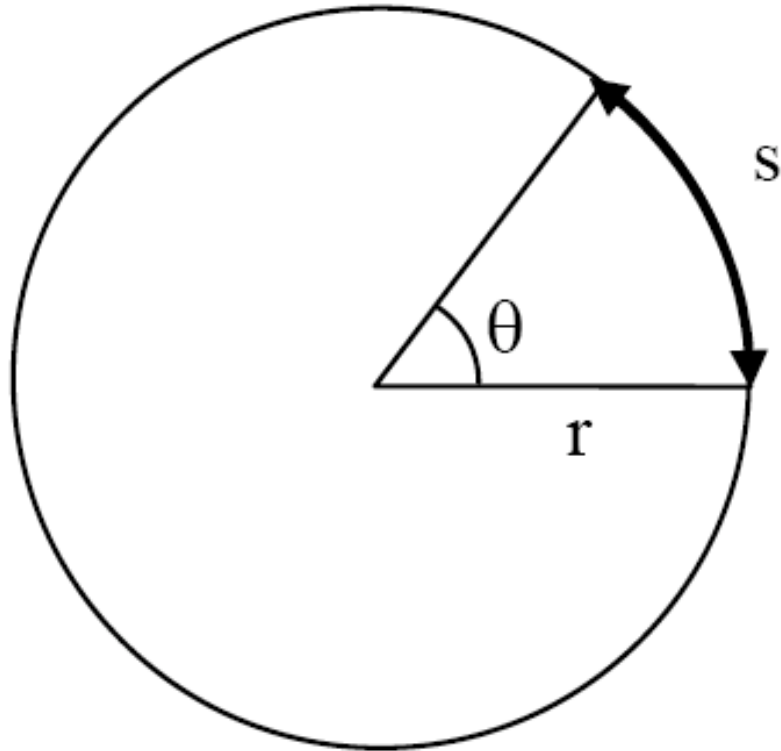
Motion of a “rigid” body about a fixed axis of rotation.

<u>Translation</u>	\leftrightarrow	<u>Rotation</u>
x	\leftrightarrow	θ
$v = \frac{\Delta x}{\Delta t}$	\leftrightarrow	$\omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r}$
$a = \frac{\Delta v}{\Delta t}$	\leftrightarrow	$\alpha = \frac{\Delta \omega}{\Delta t} = \frac{a_{\text{tan}}}{r}$

angular acceleration (rad/s²)



Rotational Kinematics



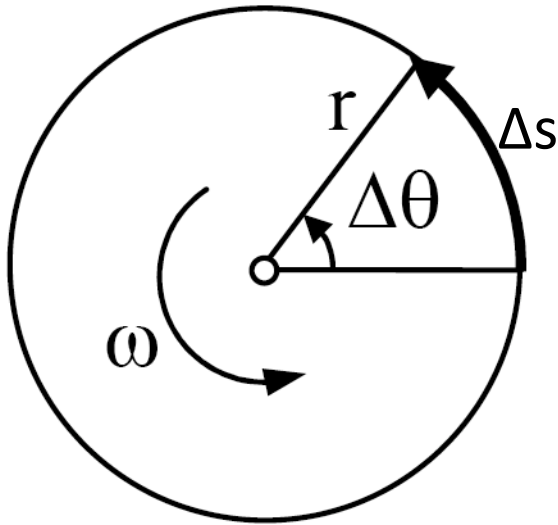
Remember: $s = r \theta$ (θ : rads)

(r, θ) polar coordinates

For circular motion, θ completely describes the motion.
It gives the “rotational position”.

Circumference: $C = 2\pi r$ $360^\circ = 2\pi \text{ rad}$
 $180^\circ = \pi \text{ rad}$
 $57.3^\circ = 1 \text{ rad}$

Rotational Kinematics



$$s = r \theta$$

arc-length
formula

$$\begin{aligned} v &= \frac{\Delta s}{\Delta t} \\ &= \frac{\Delta(r\theta)}{\Delta t} \\ &= r \frac{\Delta \theta}{\Delta t} \\ &= r \omega \end{aligned}$$

tangential velocity (m/s)

use arc-length formula

$r = \text{const}$ for circular motion

define: **angular velocity** ω

$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r}$$

Rate at which θ is changing

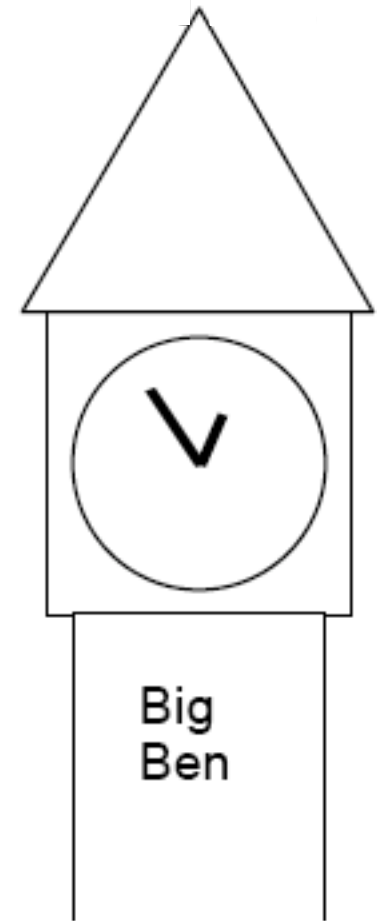
A pocket watch and Big Ben are both keeping perfect time.

Which minute hand has larger *angular velocity* ω ?

A) Pocket watch.

B) Big Ben.

C) Same ω .



A pocket watch and Big Ben are both keeping perfect time.

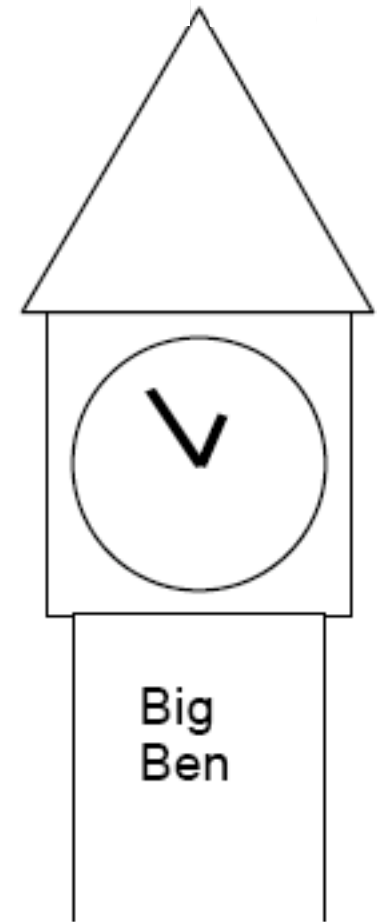
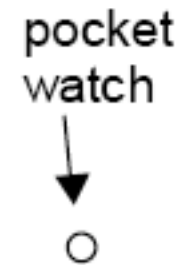
Which minute hand's tip has larger *tangential velocity* v ?

A) Pocket watch.

B) Big Ben.

C) Same v .

$$v = r\omega$$



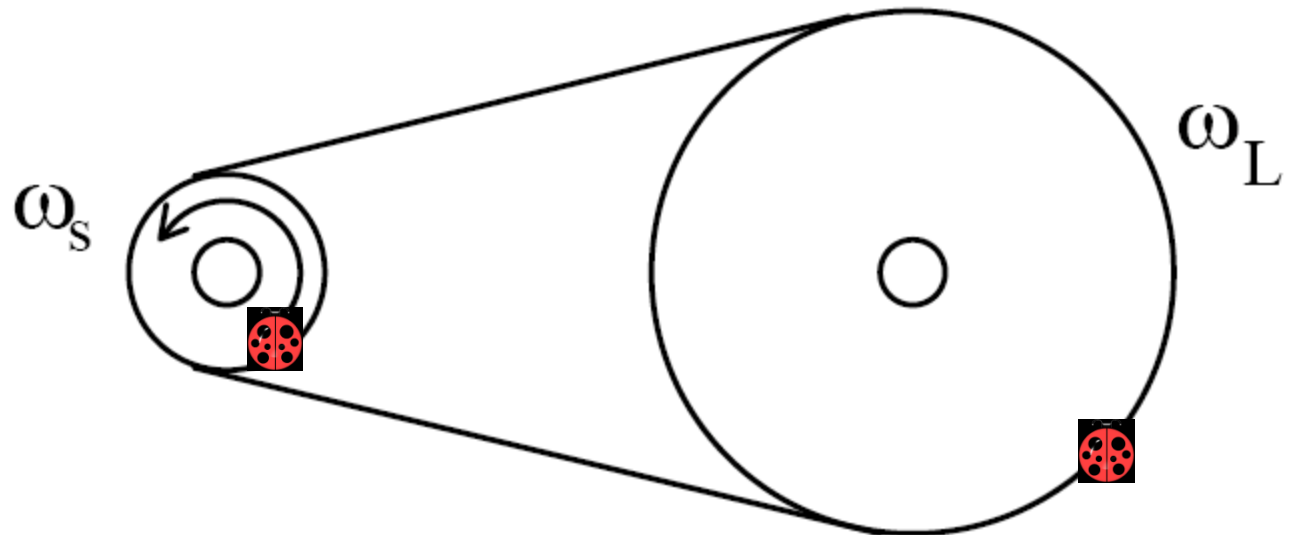
A small wheel and a large wheel are connected by a belt. The small wheel turns at a constant angular velocity ω_S .

There is a bug S on the rim of the small wheel and a bug L on the rim of the big wheel. How do their speeds compare?

A) $v_S = v_L$

B) $v_S > v_L$

C) $v_S < v_L$



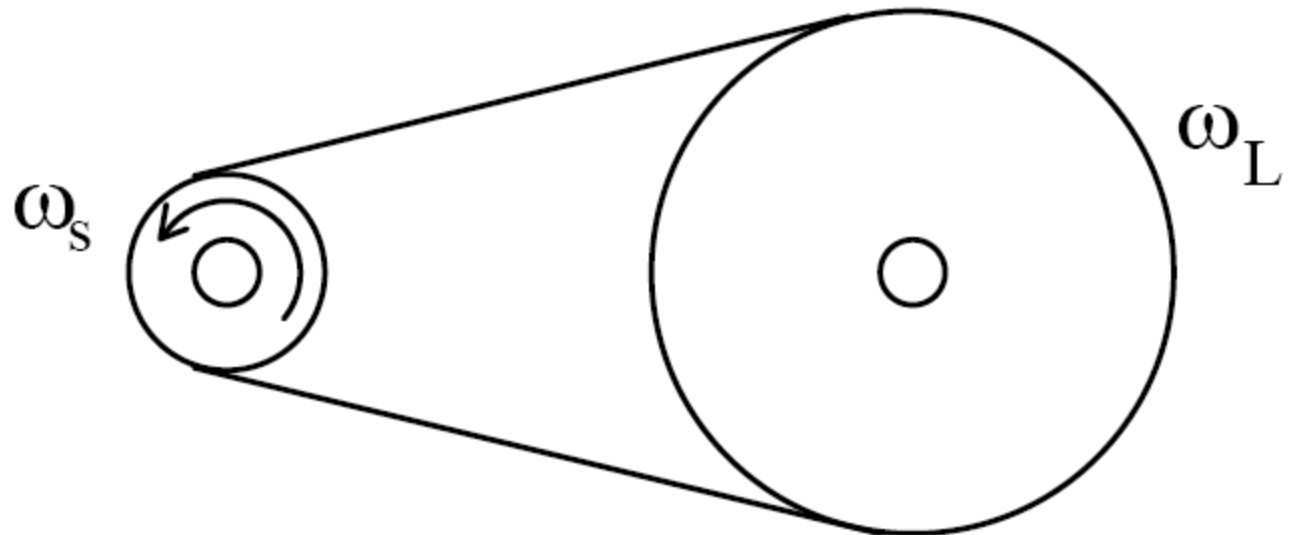
A small wheel and a large wheel are connected by a belt. The small wheel turns at a constant angular velocity ω_s .

How does the magnitude of the angular velocity of the large wheel ω_L compare to that of the small wheel ω_s ?

A) $\omega_s = \omega_L$

B) $\omega_s > \omega_L$

C) $\omega_s < \omega_L$



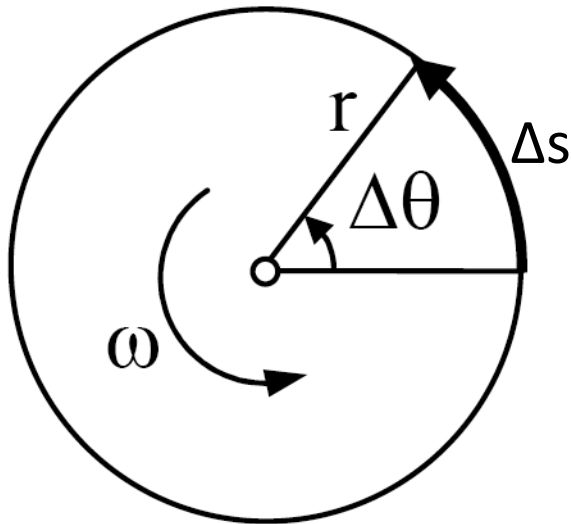
Rotational Kinematics

$$s = r \theta$$

arc-length
formula

$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r}$$

angular velocity



Units:

$$f = \frac{\# \text{ revolutions}}{\text{sec}} = \frac{1 \text{ rev}}{\text{period}} = \frac{1}{\tau} \quad (\text{Hz})$$

$$\omega = \frac{\# \text{ radians}}{\text{sec}} = \frac{2\pi}{\text{period}} = \frac{2\pi}{\tau} = 2\pi f$$

$$v = \omega r = \frac{2\pi r}{\tau} = 2\pi r f$$

Note:

$$\text{rpm} = 60 f = 60/\tau$$

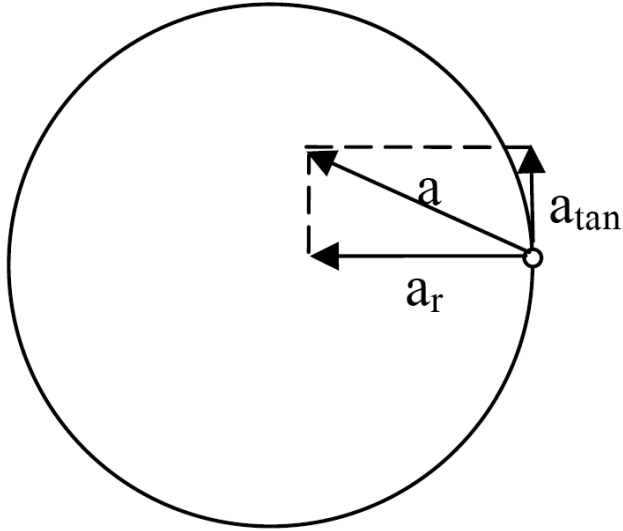
Rotational Kinematics

$$s = r \theta$$

arc-length formula

$$\omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r}$$

Rate at which θ is changing



a_r is due to change in direction of velocity vector \vec{v} (centripetal accel)

a_{tan} is due to change in the magnitude (speed) of \vec{v}

$$|\vec{a}| = a = \sqrt{a_{tan}^2 + a_r^2}$$

$$\begin{aligned} a_{tan} &= \frac{\Delta v}{\Delta t} \\ &= \frac{\Delta(r\omega)}{\Delta t} \\ &= r \frac{\Delta\omega}{\Delta t} \\ &= r\alpha \end{aligned}$$

tangential acceleration (m/s²)

use equation for ω

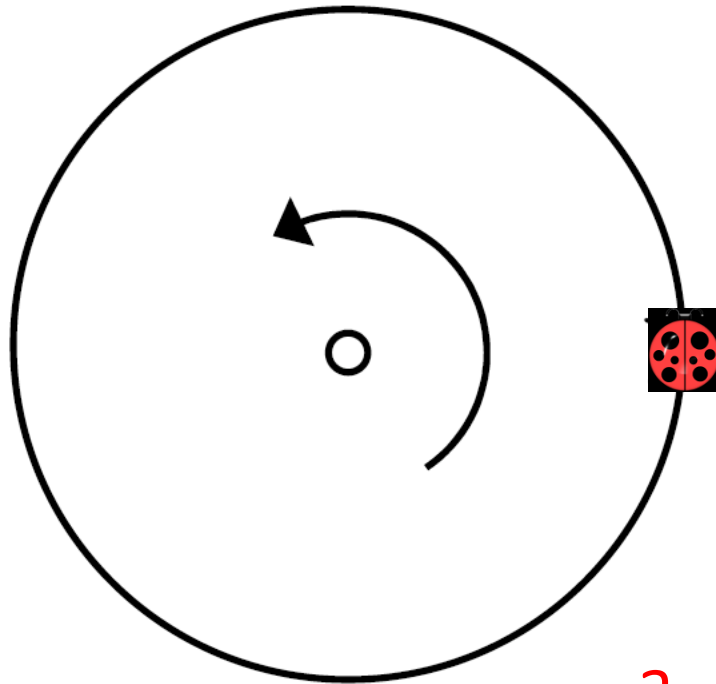
$r = \text{const}$ for circular motion

define: **angular acceleration α**

$$\alpha = \frac{\Delta\omega}{\Delta t} = \frac{a_{tan}}{r}$$

Rate at which ω is changing

A ladybug is clinging to the rim of a wheel spinning CCW. Assuming that the wheel is **spinning at a constant rate**, what is the direction of her acceleration when she's at the far right?



A) ↙

B) ↑

C) →

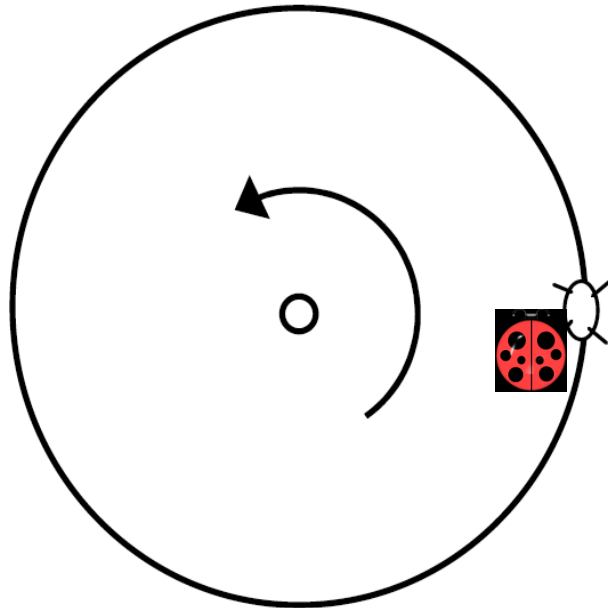
D) ←

E) ↖

Since her speed is constant, $a_{\text{tan}} = 0$, so the only acceleration is centripetal acceleration pointing toward the center of the wheel.

A ladybug is clinging to the rim of a wheel spinning CCW.

Assuming that the wheel is **speeding up**, what is the direction of her acceleration when she's at the far right?



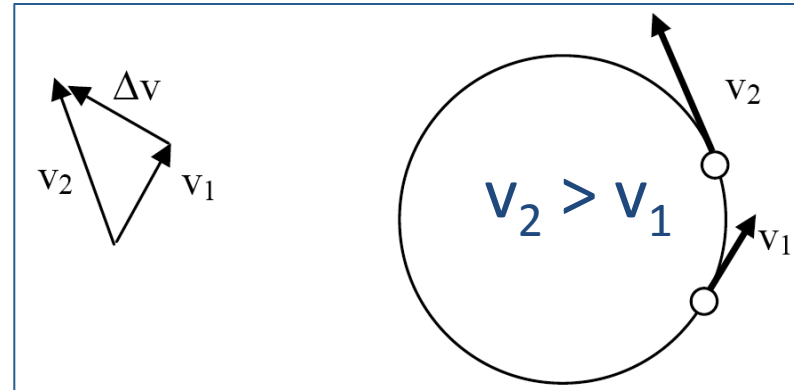
A) ↙

B) ↑

C) →

D) ←

E) ↖



Rotational Kinematics

<u>Translation</u>	\leftrightarrow	<u>Rotation</u>	
x	\leftrightarrow	θ	angle of rotation (rads)
$v = \frac{\Delta x}{\Delta t}$	\leftrightarrow	$\omega = \frac{\Delta \theta}{\Delta t} = \frac{v}{r} = \frac{2\pi}{\tau} = 2\pi f$	angular velocity (rad/s)
$a = \frac{\Delta v}{\Delta t}$	\leftrightarrow	$\alpha = \frac{\Delta \omega}{\Delta t} = \frac{a_{\text{tan}}}{r}$	angular acceleration (rad/s ²)

Constant acceleration a :

$$v = v_0 + at \quad \leftrightarrow$$

$$x = x_0 + v_0 t + \frac{1}{2} at^2 \quad \leftrightarrow$$

$$v^2 = v_0^2 + 2a\Delta x \quad \leftrightarrow$$

Constant angular acceleration α :

$$\omega = \omega_0 + \alpha t$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha\Delta\theta$$