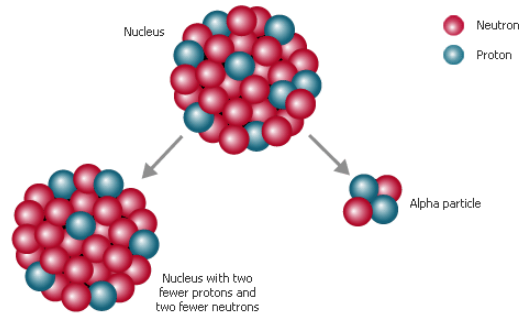


Golly... tunneling seemed pretty abstract... I wonder what those ideas could be applied to? Hmm...



Day 31:

Questions?

Reminders: Schrödinger Wave Eq' n
Potential Wells & Tunneling

Reminders:

HW

Next up: STMs & Nukes

0

L

$\psi(L)$

$\psi(L) * 1/e$

E_{electron}

$1/\alpha$

wire

$$\frac{d^2\psi(x)}{dx^2} = \frac{2m}{\hbar^2}(V - E)\psi(x) = \alpha^2\psi(x)$$

How far does wave extend into this "classically forbidden" region?

$$\psi(x) = Be^{-\alpha x}$$

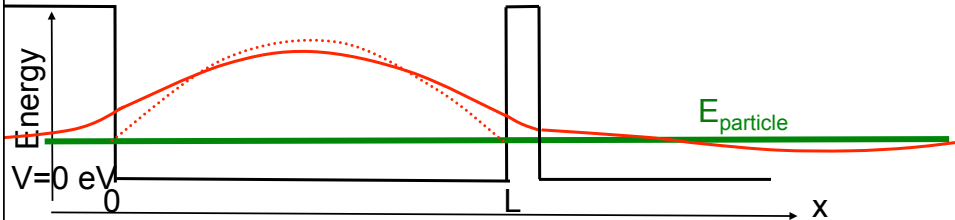
$\alpha = \sqrt{\frac{2m}{\hbar^2}(V - E)}$

α big -> quick decay
 α small -> slow decay

Measure of penetration depth = $1/\alpha = \eta$ (Knight book)
→ ψ decreases by factor of $1/e$

For $V-E = 4.7\text{eV}$, $1/\alpha \approx 9 \times 10^{-11}$ meters (very small ~ an atom!!!)

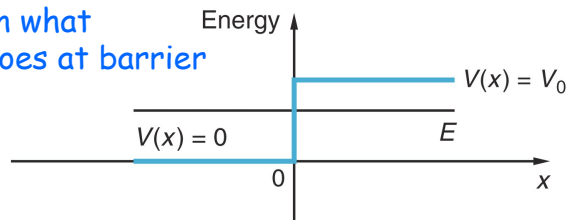
So the thinner, the shorter the barrier, the easier it is to tunnel ...



And particle can escape...

Application: Alpha-Decay,
Scanning tunneling microscope

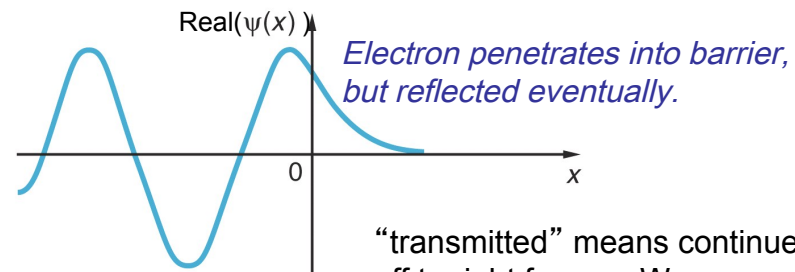
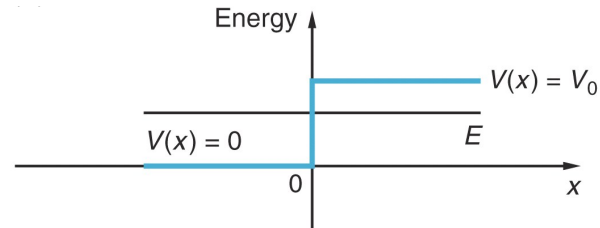
warm up on what
electron does at barrier
then apply



If the total energy E of the electron is LESS than the work function of the metal, V_0 , when the electron reaches the end of the wire, (and no other wire is near by) it will...

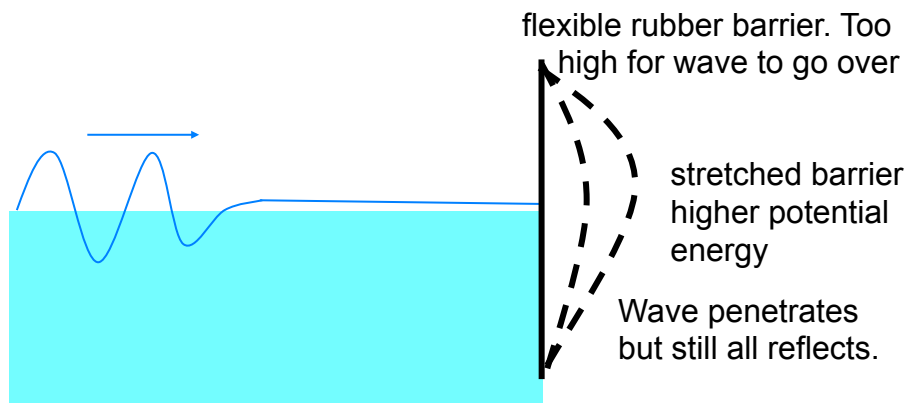
- stop.
- be reflected back.
- exit the wire and keep moving to the right.
- either be reflected or transmitted with some probability.
- I have *no* idea

Once you have amplitudes, can draw wave function:

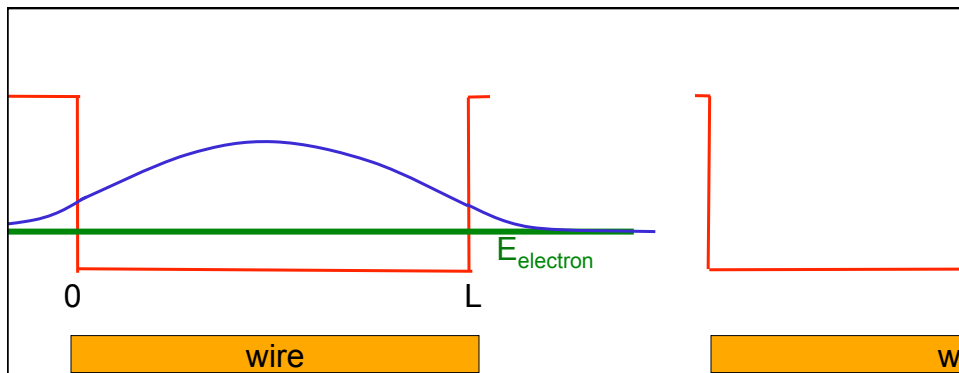
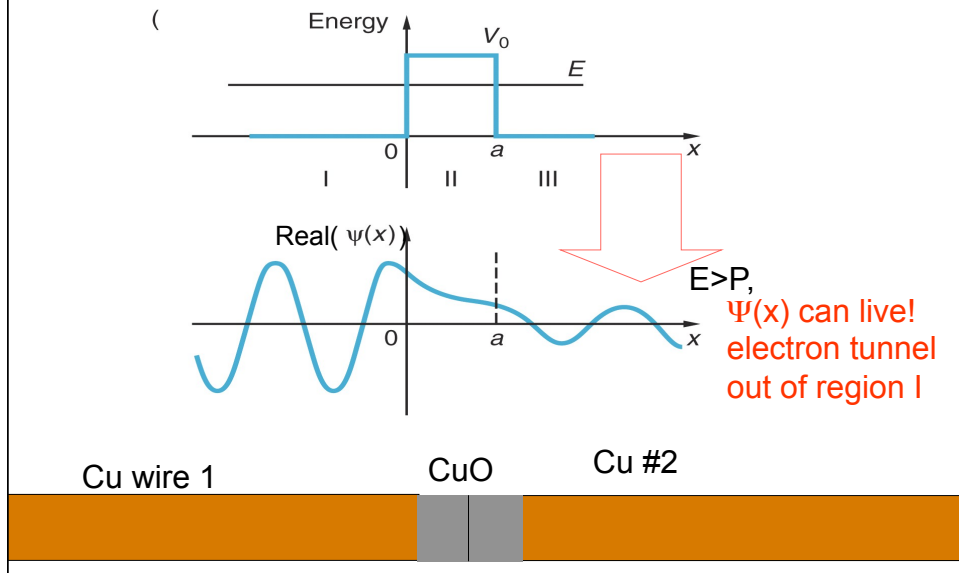


“transmitted” means continues off to right forever. Wave function not go down to zero.

water wave ~ analogy for reflection and tunneling



Can have transmission only if third region where solution is not real exponential! (electron tunneling through oxide layer between wires)



If very very long wire gets closer and closer to this very short, what will eventually happen?

- electron is "shared" between wires, with fraction in each constant over time
- the electron will flow away through wire 2
- electron will jump back and forth between wire 1 and wire 2
- electron stays in wire 1.
- something else happens.

Tutorial (Long Answer HW 8)

