

## Band gaps and LEDs

The Nobel Prize in Physics  
2014 was awarded jointly to  
Isamu Akasaki, Hiroshi Amano  
and Shuji Nakamura:

"for the invention of efficient  
blue light-emitting diodes which  
has enabled bright and energy-  
saving white light sources"



Day 36, Phys 2130  
Questions? Bonds Bands and LEDs

Next up: band structure/ LEDs,  
Semiconductors  
Tutorial?

Laser-- Light Amplification by Stimulated Emission of Radiation  
**lots of cloning of photons- LOTS of identical light.**

Figure out conditions for l.a.s.e.r.  
Important roles all played by:

- absorption
- stimulated emission
- spontaneous emission

Requires

1) more atoms in an upper level than a lower one  
("population inversion")  
*(hard part of making laser)*

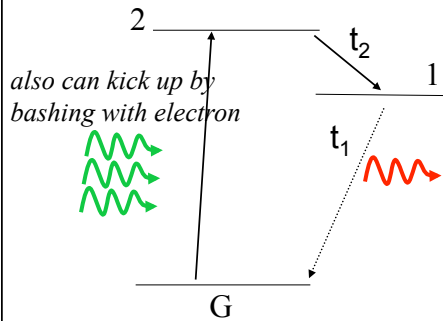
2) Method of re-cycling photons to clone more times ("feedback")  
*(mirrors)*

## Getting a population inversion

**need at least one more energy level involved.**

Trick: use a second color of light

(why two levels (one color) won't work as HW problem (maybe))



“pumping” process to produce population inversion

To create population inversion between G and level 1 would need:

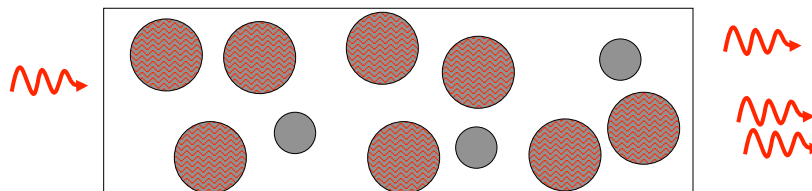
- a. time spent in level 2 ( $t_2$ ) before spontaneously jumping to 1 is long and time spent in level 1 ( $t_1$ ) before jumping to G is short.
- b.  $t_1 = t_2$
- c.  $t_2$  short,  $t_1$  long
- d. does not matter

ans. c. show on sim

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## Amplifying light:

Population inversion  $\Rightarrow$  give amplification of photons from left.



But much easier if not all light escapes.

Reuse. Use mirror to reflect the light. (sim)

If 3 in becomes 6 at end, What does 6 become?

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## Laser Gain

One photon becomes two,  
 2 becomes 4,  
 4 becomes 8,  
 8 sixteen.. Etc...

Do you know the words of AI Bartlett? (the lack of understanding the exponential function is the great failure of the human race)

May be bad for human population. Good for photon population.

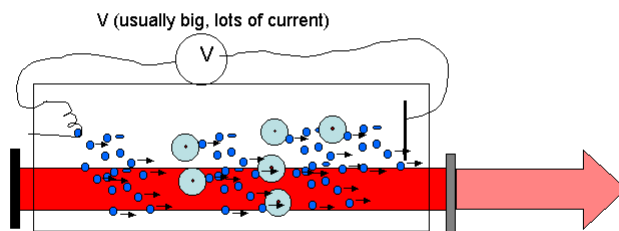
Number of photons between the mirrors,  $n = n_0 e^{Gt}$

“gain”  $G > 0$  exponential increase.

Very quickly increases until nearly all input power is going into laser light. Use *partially* reflective mirror on one end.

Let some of laser light inside leak out --- that's what we see. 6

Two types of lasers: He-Ne and Diode



Gas laser like Helium Neon.

Just like neon sign with helium and neon mixture in it and mirrors on end.

Diode laser-

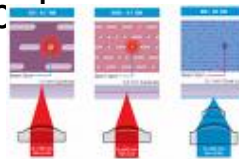
Same basic idea, but light from diode at P-N diode junction.

Mirrors on it.

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## Many applications of lasers

- High energy small area:
  - Cutting: surgery, laser welding
  - “communication” (and weapons)
- Focus light into extremely small spot
  - (diffraction limit, because in phase!)
  - CDs, DVDs, ...
- Collimated beam
  - Tracking, leveling,
- Pure color
  - LIDAR....



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### End of general atomic spectra.

- Understanding of what has been observed, how implies electrons in atoms only in certain energy levels.
- When hop from higher to lower give off light.
- Applications: neon lights, lasers

*Questions?*

### Next:

## Band structure / LEDs

Build from single atom / energy levels to more complex  
what happens to energy levels  
when atoms interact

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## Bonding

- Main ideas:

**1. involves outermost electrons and their wave functions**

**2. interference of wave functions**

(one wave function from each atom) that produces situation where atoms want to stick together.

**3. degree of sharing of an electron** across 2 or more atoms determines the type of bond

Degree of sharing of electron		
<u>Ionic</u>	<u>Covalent</u>	<u>Metallic</u>
electron completely transferred from one atom to the other	electron equally shared between two adjacent atoms	electron shared between all atoms in solid
$\text{Li}^+ \text{F}^-$	$\text{H}_2$	Solid Lead

## Ionic Bond (NaCl)

Na (outer shell  $3s^1$ )

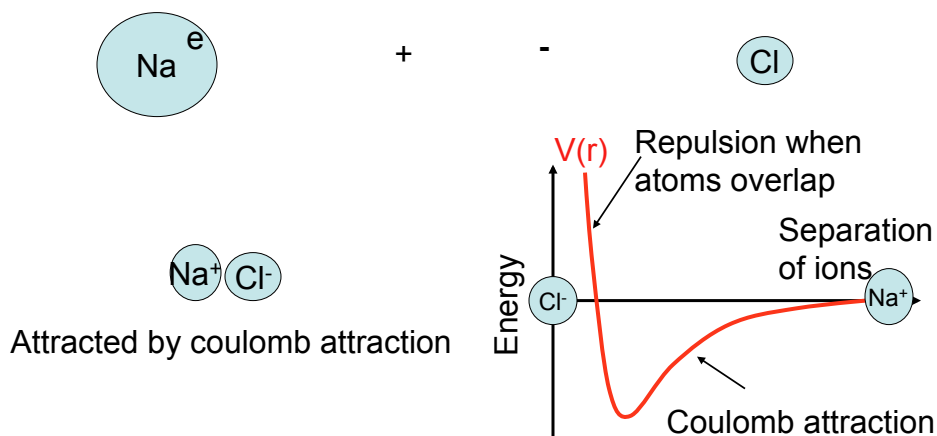
Has one weakly bound electron

**Low ionization energy**

Cl (outer shell  $3s^23p^5$ )

Needs one electron to fill shell

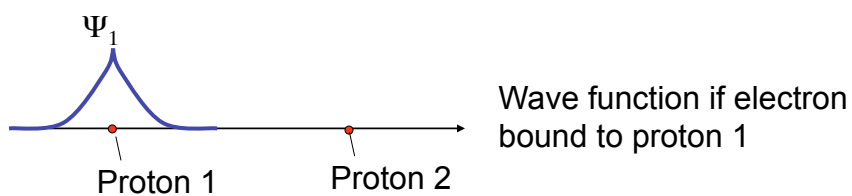
**Strong electron affinity**



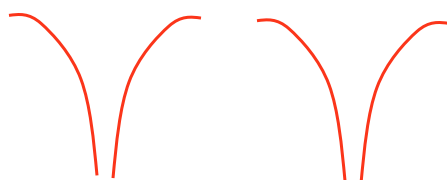
## Covalent Bond

Sharing of an electron... look at example  $H_2^+$   
(2 protons (H nuclei), 1 electron)

Protons far apart ...



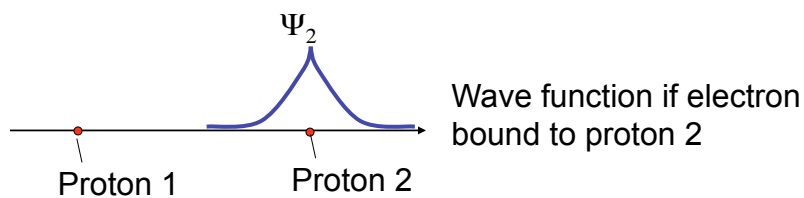
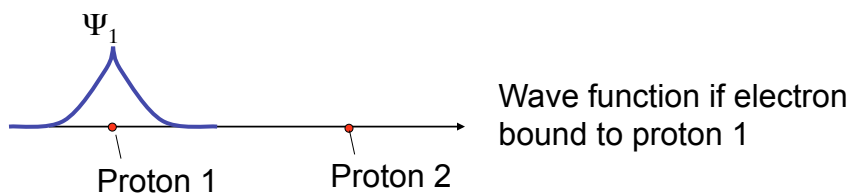
Potential energy curve



## Covalent Bond

Sharing of an electron... look at example  $H_2^+$   
(2 protons (H nuclei), 1 electron)

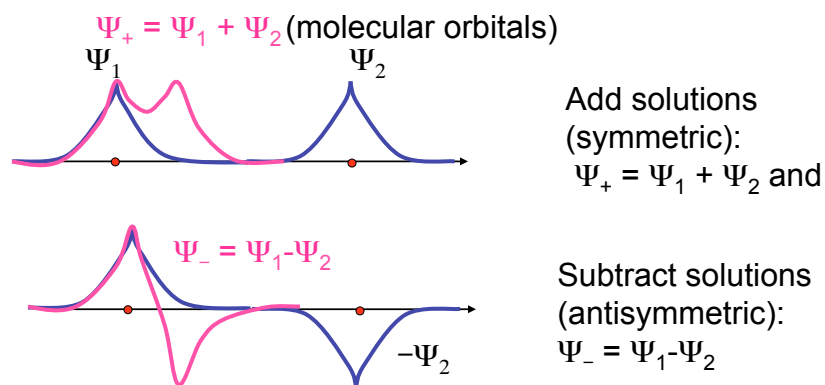
Protons far apart ...



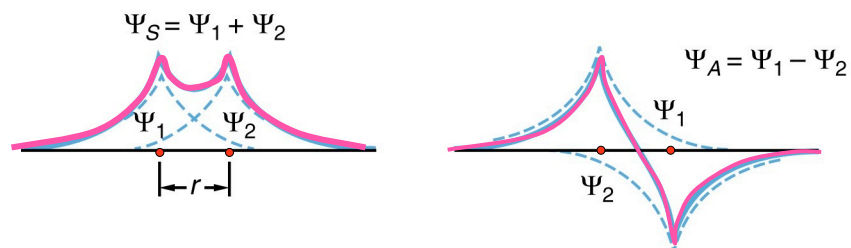
## Covalent Bond

Sharing of an electron... look at example  $H_2^+$   
(2 protons (H nuclei), 1 electron)

If  $\Psi_1$  and  $\Psi_2$  are both valid solutions,  
then **any combination** is also valid solution.



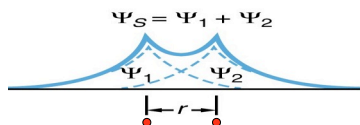
Look at what happens to these wave functions as bring protons closer...



**Visualize how electron cloud is distributed...** for which wave function would this cloud distribution tend to keep protons together? (bind atoms?) ... what is your reasoning?

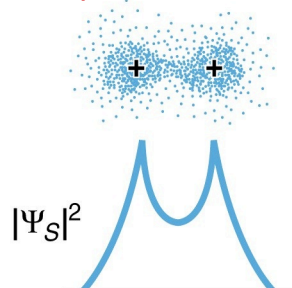
- $\Psi_S$  or  $\Psi_+$
- $\Psi_A$  or  $\Psi_-$

Look at what happens to these wave functions as bring protons closer...



$\Psi_+$  puts electron density between protons .. glues together protons.

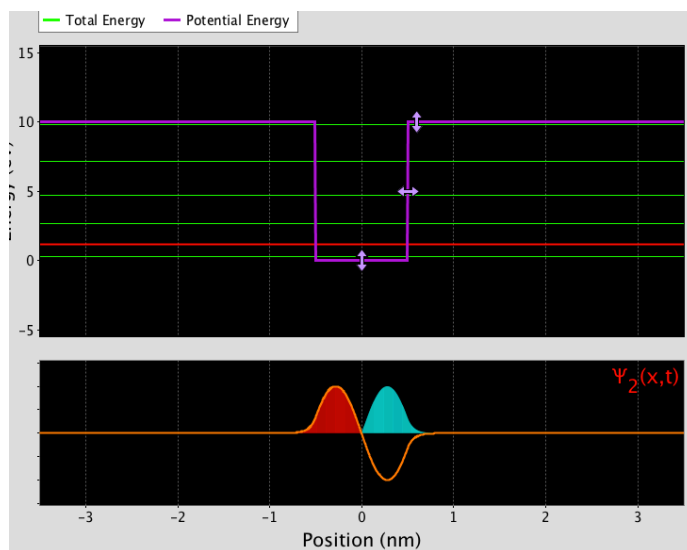
between protons ... protons repel (not stable)



Bonding Orbital

Antibonding Orbital

## Quantum Bound State Sim





**Big Picture. Now almost infinite power!**

Know how to predict **everything** about behavior of atoms and electrons or anything made out of them:

1. Write down all contributions to potential energy, includes e-e, nuc.-nuc., nuc.-e for all electrons and nuclei.

$$q_1 q_2 / r_{1-2} + q_2 q_3 / r_{1-3} + q_{\text{nuc}1} q_{\text{nuc}2} / r_{q_{\text{nuc}1} - q_{\text{nuc}2}} + q_1 q_{\text{nuc}1} / r_{1-\text{nuc}1} +$$

one spin up and one down electron per state req....

(plus little terms involving spin, magnetism, applied voltage)

2. Plug potential energy into Schrod. eq., add boundary. cond.

3. Solve for wave function  $\Psi_{\text{elec}1, \text{elec}2, \text{nuc}1, \text{nuc}2, \dots}(r_1, r_2, r_{\text{nuc}1}, \dots)$

get energy levels  
for system

**calculate/predict everything there is to know!!**

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## Demo

- Which is more reactive?
- He<sub>2</sub>
- H<sub>2</sub>

## Limitations of Schrodinger

- With three objects (1 nuclei + 2 electrons) solving eq. very hard.
- Gets much harder with each increment in number of electrons and nuclei !!

### Give up on solving S. E. exactly--

Use various models and approximations.

Not perfect but very useful, tell a lot.

*(lots of room for cleverness, creativity, intuition)*

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## How does atom-atom interaction lead to band structure?

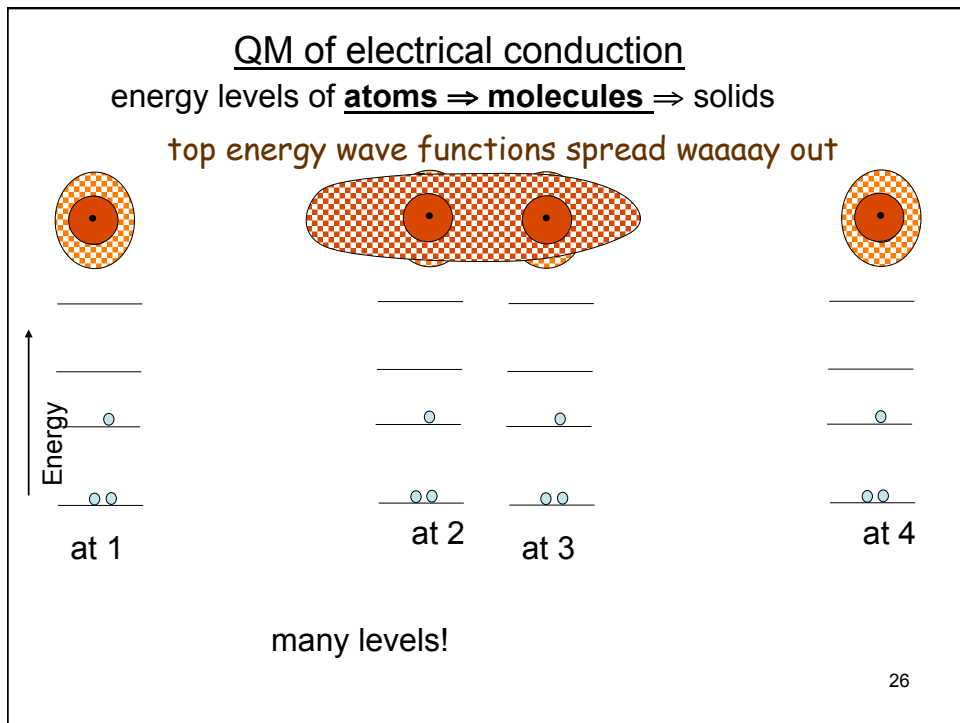
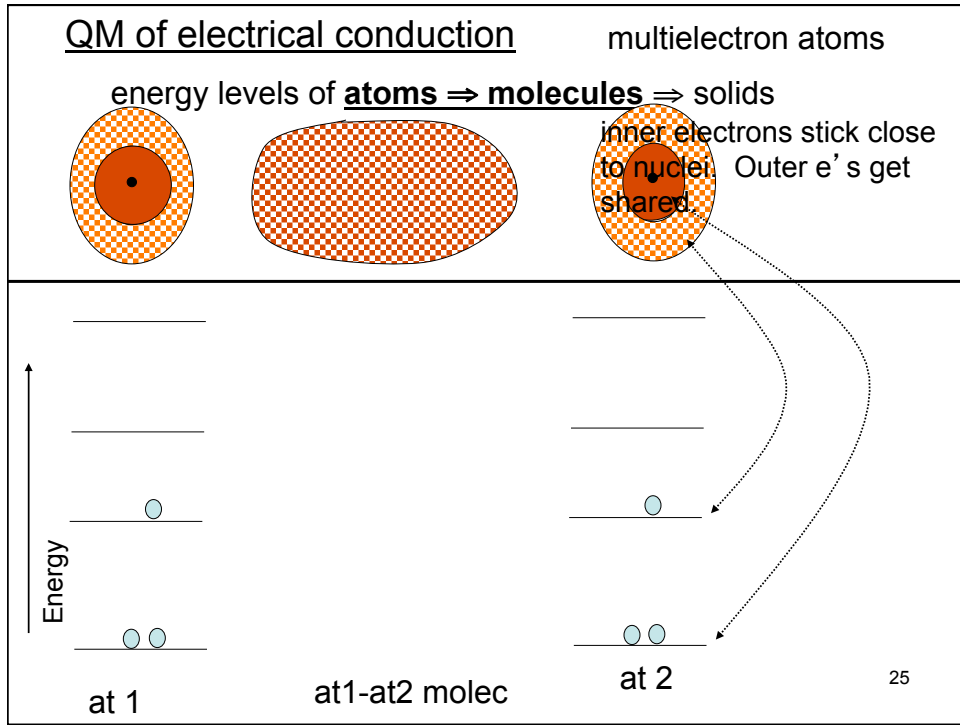
1. Energy levels and spacings in atoms  $\Rightarrow$  molecules  $\Rightarrow$  solids
2. How energy levels determine how electrons move.  
Insulators, conductors, semiconductors.
3. Using this physics for nifty stuff like (old) copying machines, diodes and transistors (all electronics), light-emitting diodes.

Spacing of gap to the next higher, open energy level for electron is the critical feature.

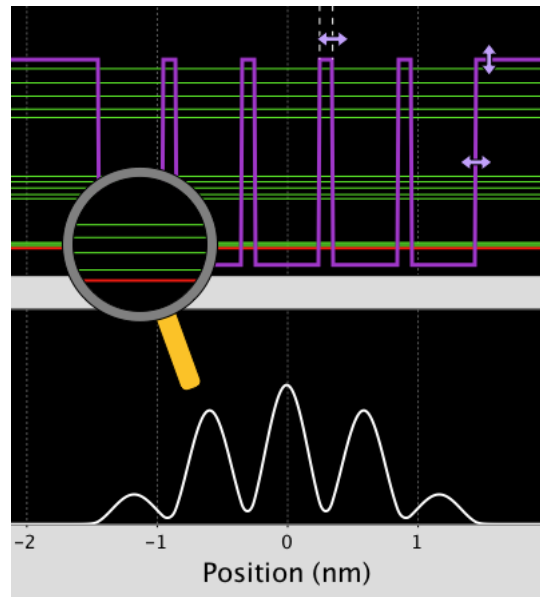
Small, large, in middle compared to  $kT$  ( $\sim 1/40$  eV)?

What happens to energy levels as put bunch of atoms together?

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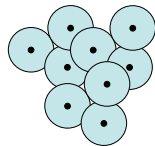


### Bound State Sim.. Many Wells

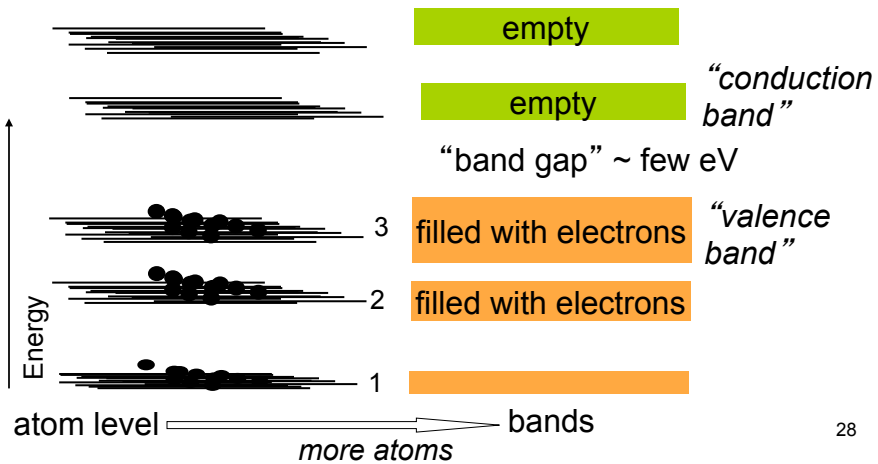


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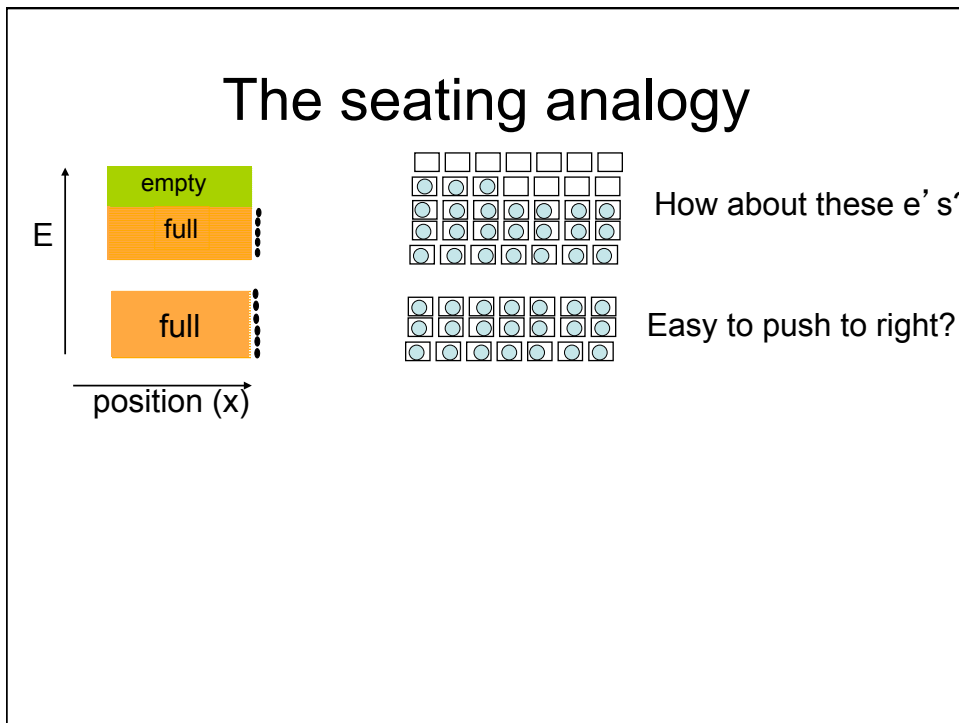
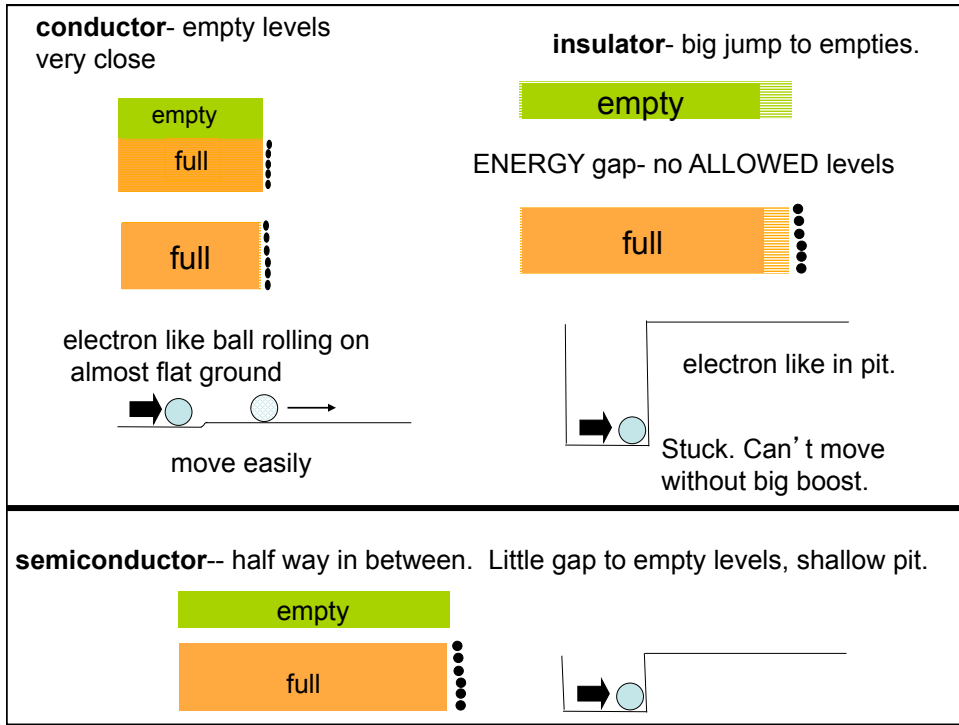
In solid,  $\sim 10^{22}$  atoms/cm<sup>3</sup>, many!! electrons, and levels



countless levels smeared together, individual levels indistinguishable.  $\Rightarrow$  "bands" of levels. Each level filled with 2 electrons until run out.



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Energy

3

2

1

0...

moving

stationary

V

If push on electrons (apply voltage to material) which ones will move?

- all of them in bands 1,2,3
- only top one in band 3
- all of them in band 3
- only the top few in band three
- none of them will move

**d. only the top few in band 3.**

The others have no higher level they can move into, all filled with other electrons. *After top one has gotten pushed up, is room to move next one below it. so include those within  $\sim kT = 1/40$  eV of top (room temp). Band gaps and widths  $\sim$  eVs. Small fraction, still big #.*

Which band structure goes with which material?  
(be ready to give reasoning)

Legend: ■ empty, ■ full

**1. Diamond    2. copper    3. germanium (poor conductor)**

a. 1=w, 2=x, 3=y    b. 1=z, 2=w, 3=y    c. 1=z, 2=y, 3=x  
d. 1=y, 2= w, 3=y.    e. 1=w, 2=x, 3=y

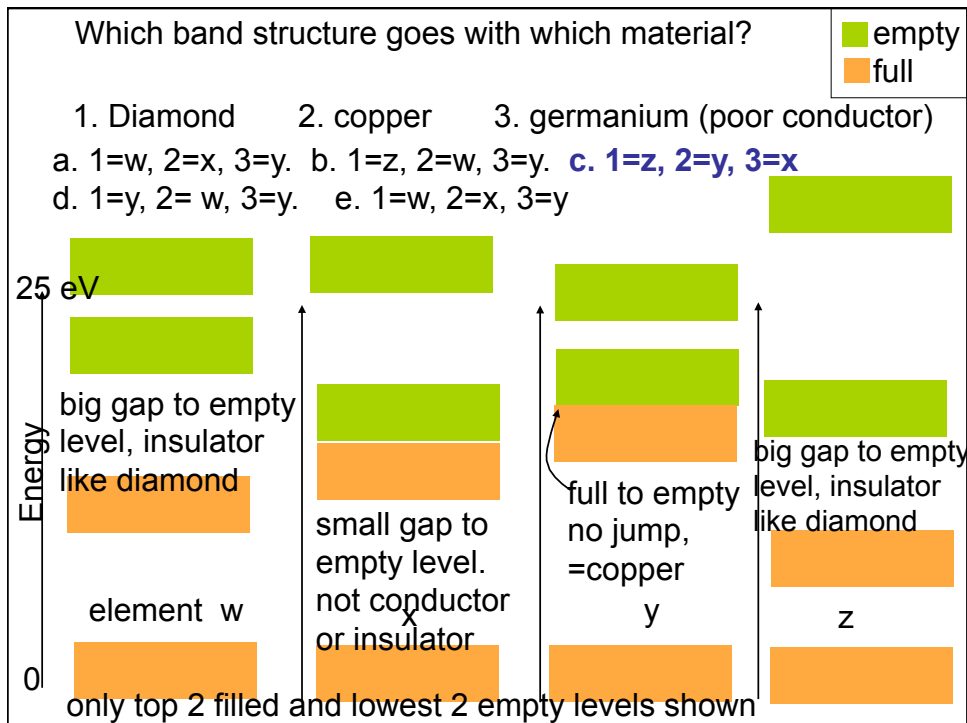
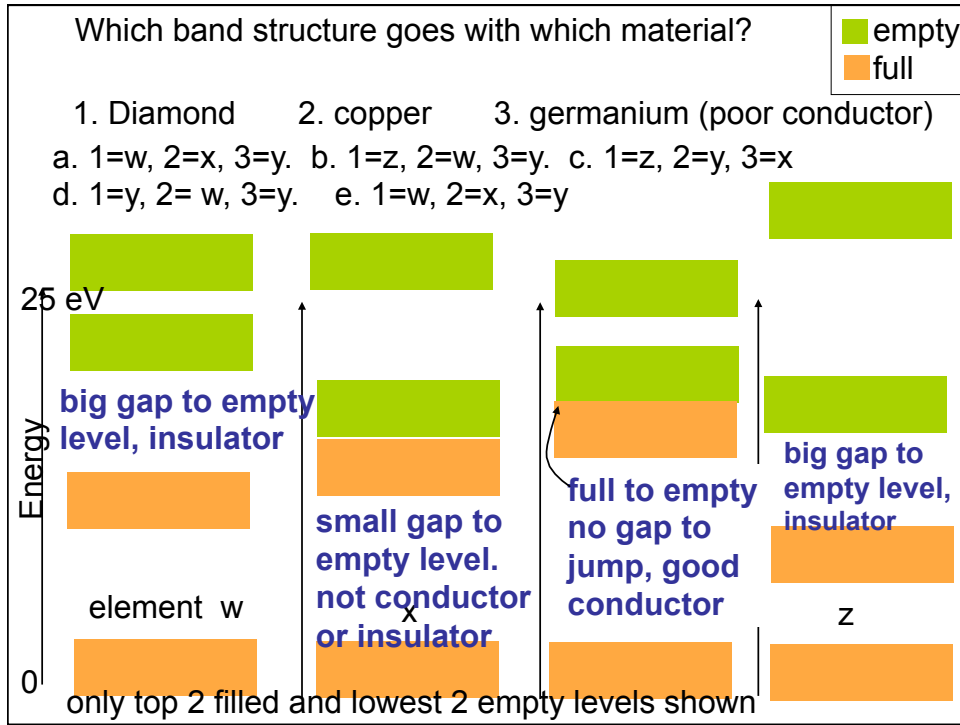
25 eV

Energy

0

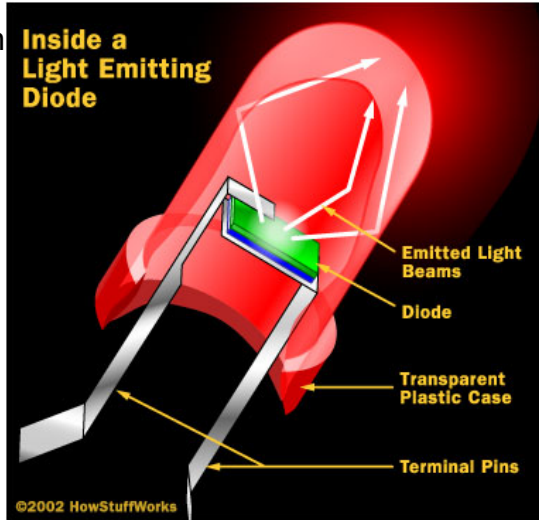
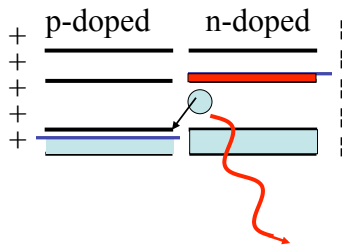
element w    x    y    z

only top 2 filled and lowest 2 empty bands shown



LEDs -- don't burn out, high efficiency. Stoplights, bike lights, fancy flashlights.

Really good LEDs reach laser conditions-- diode lasers



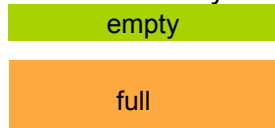
<http://www.howstuffworks.com/index.htm>

**Insulators and conductors**

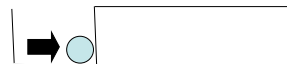
Good in wires, electricity for lights and heating, electric motors, telegraph ( $I=V/R$  stuff).

For more interesting electrical stuff need more control- small currents & voltages control higher powers ("nonlinear circuit elements").

**Semiconductor**-- half way in between. Little gap to empty levels.



how many have class on semicond?



sensitive enough so people can affect conductivity of material

What are possible ways could get electron to higher empty level (out of pit), so could move to conduct electricity?

Discuss as many as can think of that are practical.

**n.b.** Applying a voltage across (battery) will not work... why? Think about voltage /electron.... (how much V how many e's...?)