

## CHAPTER 6

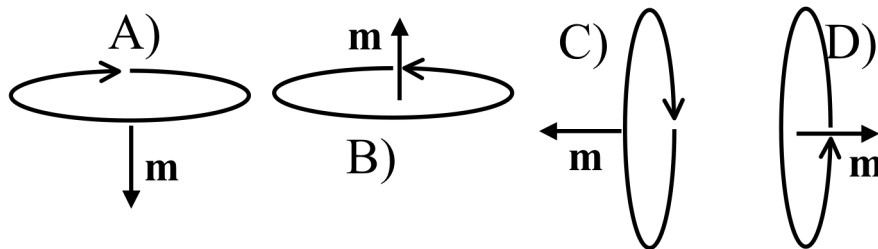
## MAGNETIZATION

6.1

Griffiths argues that the torque *on* a magnetic dipole in a  $\mathbf{B}$  field is:

$$\vec{\tau} = \vec{\mathbf{m}} \times \vec{\mathbf{B}}$$

How will a small current loop line up if the  $\mathbf{B}$  field points uniformly up the page?



6.2

Griffiths argues that the force *on* a magnetic dipole in a  $\mathbf{B}$  field is:  $\vec{\mathbf{F}} = \vec{\nabla}(\vec{\mathbf{m}} \cdot \vec{\mathbf{B}})$

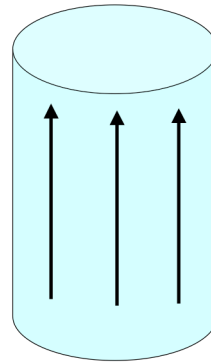
If the dipole  $\mathbf{m}$  points in the  $z$  direction, what can you say about  $\mathbf{B}$  if I tell you the force is in the  $x$  direction?

- A)  $\mathbf{B}$  simply points in the  $x$  direction
- B)  $B_z$  must depend on  $x$
- C)  $B_z$  must depend on  $z$
- D)  $B_x$  must depend on  $x$
- E)  $B_x$  must depend on  $z$

6.3

A solid cylinder has uniform magnetization  $\mathbf{M}$  throughout the volume in the  $z$  direction as shown. **Where do bound currents show up?**

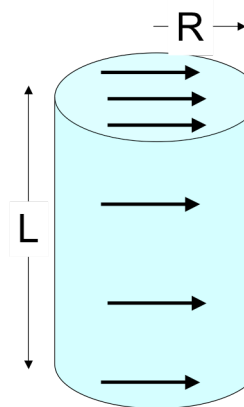
- A) Everywhere: throughout the volume and on all surfaces
- B) Volume only, not surface
- C) Top/bottom surface only
- D) Side (rounded) surface only
- E) All surfaces, but not volume



6.4

A solid cylinder has uniform magnetization  $\mathbf{M}$  throughout the volume in the  $x$  direction as shown. **What's the magnitude of the total magnetic dipole moment of the cylinder?**

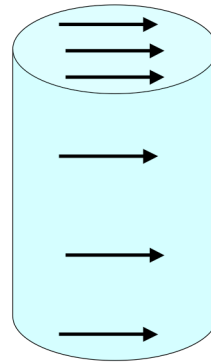
- A)  $\pi R^2 L M$
- B)  $2\pi R L M$
- C)  $2\pi R M$
- D)  $\pi R^2 M$
- E) Something else, it's more complicated



6.5

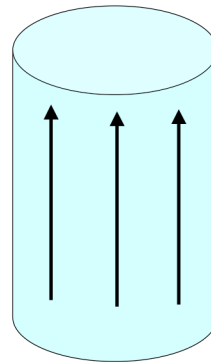
A solid cylinder has uniform magnetization  $\mathbf{M}$  throughout the volume in the x direction as shown. **Where do bound currents show up?**

- A) Top/bottom surface only
- B) Side (rounded) surface only
- C) Everywhere
- D) Top/bottom, and parts of (but not all of) side surface (but not in the volume)
- E) Something different/other combination!



To discuss:

A solid cylinder has uniform magnetization  $\mathbf{M}$  throughout the volume in the z direction as shown. **What will the B field look like?** (Consider if the cylinder is tall and thin, or short and fat, separately)



6.6

A sphere has uniform magnetization  $M$  in the  $z$  direction.

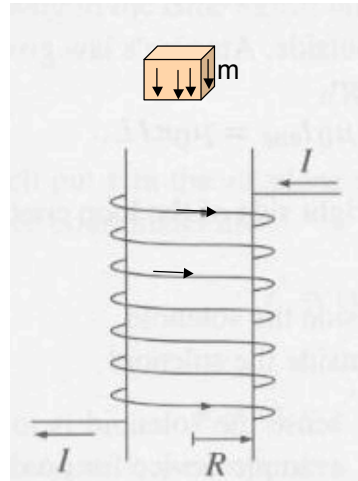
Which formula is correct for this surface current?

- A)  $M \sin\theta \hat{\theta}$
- B)  $M \sin\theta \hat{\phi}$
- C)  $M \cos\theta \hat{\theta}$
- D)  $M \cos\theta \hat{\phi}$
- E) None of these!

Coming up first today: Write down (by yourself, *without* book or notes or collaboration, yet!) what you remember about electric Polarization  $P$ , and all related concepts and formulas we've worked with!

6.7  
a A small chunk of material (the “tan cube”) is placed above a solenoid. It magnetizes, weakly, as shown by small arrows inside. What kind of material must the cube be?

- A) Dielectric
- B) Conductor
- C) Diamagnetic
- D) Paramagnetic
- E) Ferromagnetic



6.7  
b Predict the results of the following experiment: a paramagnetic bar and a diamagnetic bar are pushed inside of a solenoid.

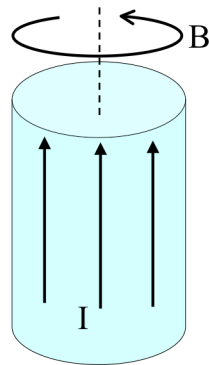
- a) The paramagnet is pushed out, the diamagnet is sucked in
- b) The diamagnet is pushed out, the paramagnet is sucked in
- c) Both are sucked in, but with different force
- d) Both are pushed out, but with different force

## AUXILIARY FIELD $\mathbf{H}$

- 6.8 A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction. We know  $\mathbf{B}$  will be CCW as viewed from above. (Right?)

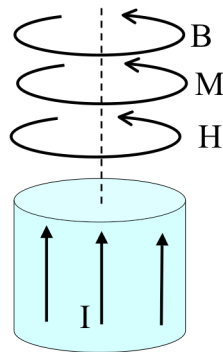
What about  $\mathbf{H}$  and  $\mathbf{M}$  inside the cylinder?

- A) Both are CCW
- B) Both are CW
- C)  $\mathbf{H}$  is CCW, but  $\mathbf{M}$  is CW
- D)  $\mathbf{H}$  is CW,  $\mathbf{M}$  is CCW
- E) ???



A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction. We know  $\mathbf{B}$  will be CCW as viewed from above. (Right?)

What about  $\mathbf{H}$  and  $\mathbf{M}$  inside the cylinder?



## LINEAR AND NONLINEAR MEDIA

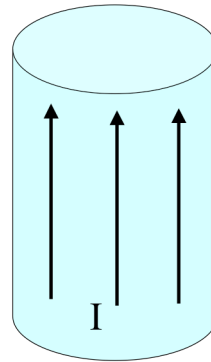


6.9

A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction.

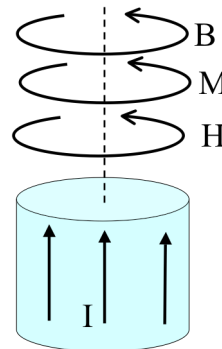
What is the direction of the bound volume current?

- A)  $\mathbf{J}_B$  points parallel to  $I$
- B)  $\mathbf{J}_B$  points anti-parallel to  $I$
- C) Other/not sure



A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction. What is the direction of the bound volume current?

- A)  $\mathbf{J}_B$  points parallel to  $I$

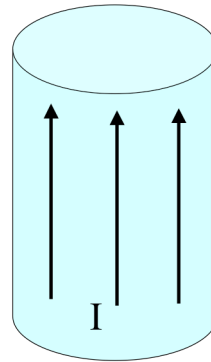


6.9  
b

A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction.

What is the direction of the bound surface current?

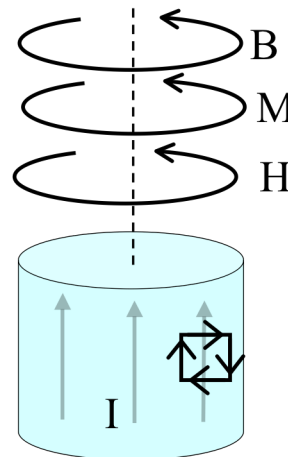
- A)  $\mathbf{K}_B$  points parallel to  $I$
- B)  $\mathbf{K}_B$  points anti-parallel to  $I$
- C) Other/not sure



A very long aluminum (paramagnetic!) rod carries a uniformly distributed current  $I$  along the  $+z$  direction.

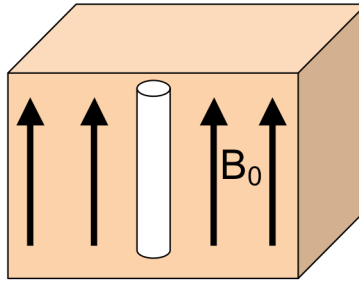
What is the direction of the bound volume current?

$\mathbf{K}_B$  points anti-parallel to  $I$



6.10

A large chunk of paramagnetic material ( $\chi_m > 0$ ) has a uniform field  $B_0$  throughout its interior. We cut out a cylindrical hole (very skinny, very tall!)

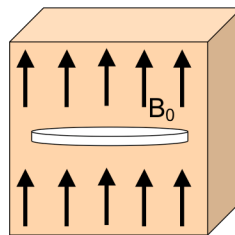


What is  $B$  at the center of that hole?

- A)  $B_0$
- B) more than  $B_0$
- C) less than  $B_0$
- D) ??

6.10  
b

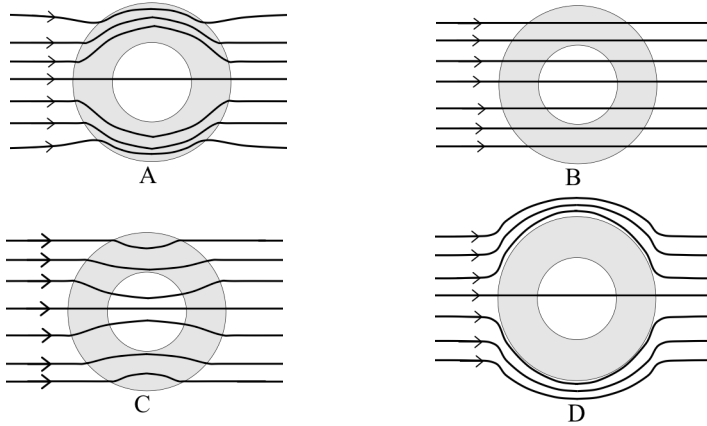
A large chunk of paramagnetic material ( $\chi_m > 0$ ) has a uniform field  $B_0$  throughout its interior. We cut out a wafer-like hole (very wide, very short!)



What is  $B$  at the center of that hole?

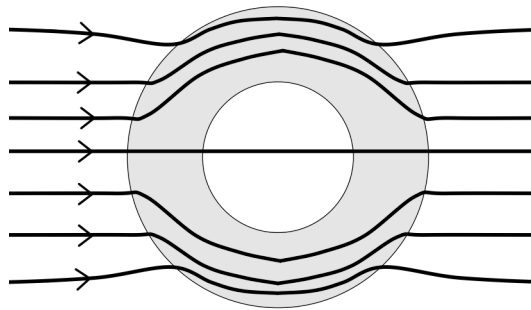
- A)  $B_0$
- B) more than  $B_0$
- C) less than  $B_0$
- D) ??

6.11 A sphere (with a spherical cavity inside it) is made of a material with very large positive  $\chi_m$ . It is placed in a region of uniform B field. Which figure best shows the resulting B field lines?



E) None of these can be even remotely correct

6.11 b Mu-metal (75% nickel, 15% iron, plus copper and molybdenum) acts as a sort of “magnetic shield”... (there is no perfect “Faraday cage” effect for magnetism - why not)



6.12 A superconducting ring sits above a strong permanent magnet (N side up). If you drop the ring, **which way will current flow (as viewed from above), and what kind of force will the ring feel?**

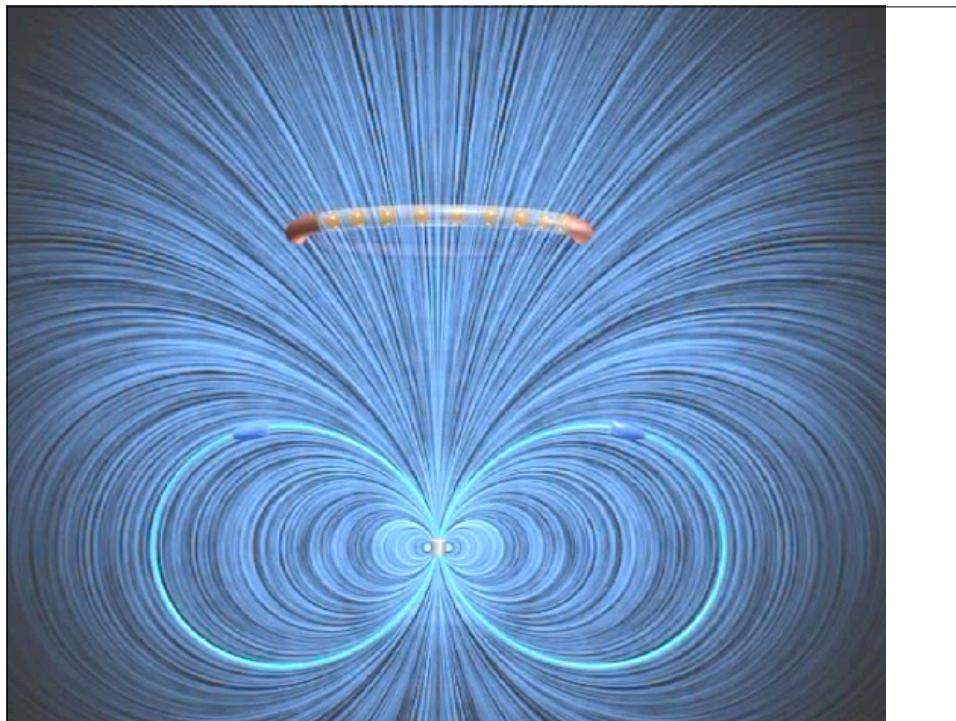
- A) CW/repulsive
- B) CW/attractive
- C) CCW/repulsive
- D) CCW/attractive
- E) No net current will flow/no net force

To think about/discuss:

Remember Lenz' law? What does it say about this situation?

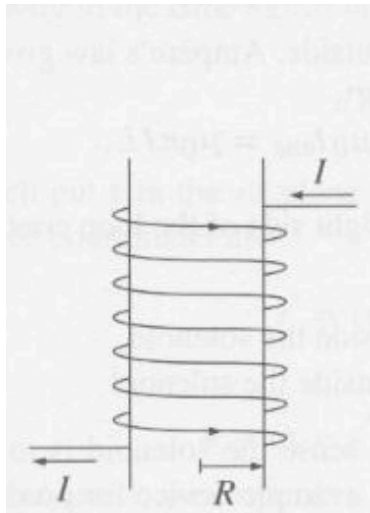
What will the resulting *motion* of the ring look like?

What if you dropped a magnet onto the ring, instead of dropping the ring onto the magnet?



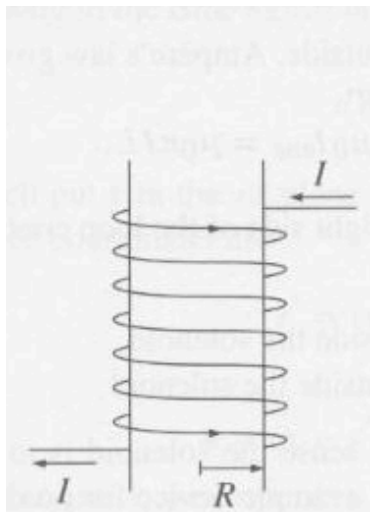
6.13 Inside a hollow solenoid,  
 $B=B_0=\mu_0 nI$ , ( so  $H=H_0=nI$  )  
If the solenoid is filled with a paramagnetic  
material, what is  $B$  inside?...

- A)  $B_0$
- B) a little more than  $B_0$
- C) a lot more than  $B_0$
- D) a little less than  $B_0$
- E) a lot less than  $B_0$



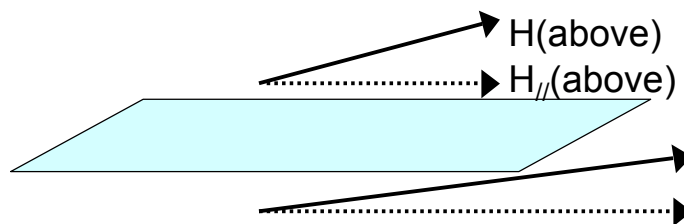
6.14 Inside a hollow solenoid,  
 $B=B_0=\mu_0 nI$ , ( so  $H=H_0=nI$  )  
If the solenoid is filled with iron,  
what is  $H$  inside?...

- A)  $H_0$
- B) a little more than  $H_0$
- C) a lot more than  $H_0$
- D) a little less than  $H_0$
- E) a lot less than  $H_0$



# BOUNDARY VALUE PROBLEMS

6.11 I have a boundary sheet, and would like to learn about the change (or continuity!) of  $H$ (parallel) across the boundary.



Am I going to need to know about

A)  $\nabla \times \mathbf{H}$

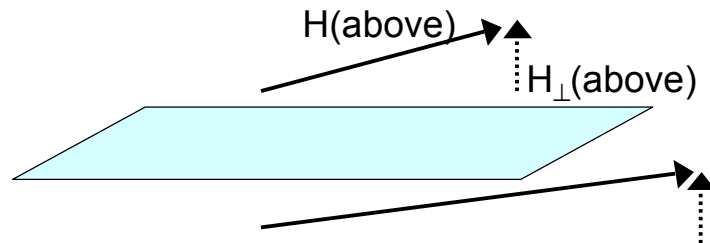
B)  $\nabla \cdot \mathbf{H}$

C) ???

6.11

b

I have a boundary sheet, and would like to learn about the change (or continuity!) of  $H(\text{perp})$  across the boundary.



Am I going to need to know about

A)  $\nabla \times \mathbf{H}$

B)  $\nabla \cdot \mathbf{H}$

C) ???