

Could we use the method of images for THIS problem: Find $V(r)$ everywhere $z > 0$, Given these two charges above a (grounded, infinite, conducting) plane?

A) Yes, it requires 1 "image charge"
 B) Yes, it requires more than 1 image charge
 C) No, this problem can NOT be solved using the "trick" of image charges...

On paper (don't forget your name!) in your own words (by yourself):

What is the idea behind the method of images? What does it accomplish? What is its relation to the uniqueness theorem?

3.9 Two ∞ grounded conducting slabs meet at right angles. How many image charges are needed to solve for $V(r)$?

A) one
 B) two
 C) three
 D) more than three
 E) Method of images won't work here

Say you have three functions $f(x)$, $g(y)$ and $h(z)$.
 $f(x)$ depends on 'x' but not on 'y' and 'z'.
 $g(y)$ depends on 'y' but not on 'x' and 'z'.
 $h(z)$ depends on 'z' but not on 'x' and 'y'.

If $f(x) + g(y) + h(z) = 0$ for all x, y, z , then:

- A) All three functions are constants (i.e. they do not depend on x, y, z at all.)
- B) At least one of these functions has to be zero everywhere.
- C) All of these functions have to be zero everywhere.
- D) All three functions have to be linear functions in x, y , or z respectively (such as $f(x)=ax, a \neq 0$ etc.)

Second uniqueness Theorem: In a volume surrounded by conductors and containing a specified charge density $\rho(r)$, the electric field is uniquely determined if the total charge on each conductor is given. (The region as a whole can be bounded by another conductor, or else unbounded.)

Griffiths, 3.1.6

3.10 Suppose $V_1(\mathbf{r})$ and $V_2(\mathbf{r})$ are linearly independent functions which *both* solve Laplace's equation, $\nabla^2 V = 0$

Does $aV_1(\mathbf{r}) + bV_2(\mathbf{r})$ also solve it (with a and b constants)?

- A) Yes. The Laplacian is a linear operator
- B) No. The *uniqueness theorem* says this scenario is impossible, there are never two independent solutions!
- C) It is a definite yes or no, but the *reasons* given above just aren't right!
- D) It depends...

What is the value of $\int_0^{2\pi} \sin(2x)\sin(3x)dx$?

A) Zero
 B) π
 C) 2π
 D) other
 E) I need resources to do an integral like this!

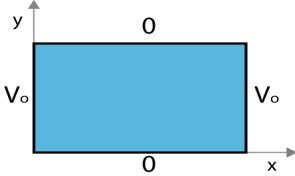
3.11 Given the two diff. eq's :
 $\frac{1}{X} \frac{d^2X}{dx^2} = C_1$ $\frac{1}{Y} \frac{d^2Y}{dy^2} = C_2$

where $C_1 + C_2 = 0$. Given the boundary conditions in the figure, which coordinate should be assigned to the negative constant (and thus the sinusoidal solutions)?

A) x B) y

C) $C_1 = C_2 = 0$ here

D) It doesn't matter



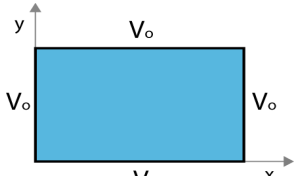
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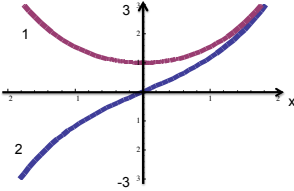
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C) $C_1 = C_2 = 0$ here

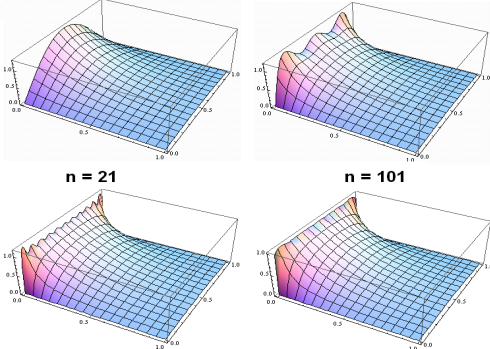
D) It doesn't matter



Two solutions for *positive C* are $\sinh x$ and $\cosh x$:



Which is which?
 A) Curve 1 is $\sinh x$ and curve 2 is $\cosh x$
 B) Curve 1 is $\cosh x$ and curve 2 is $\sinh x$

$$V(x, y) = \frac{4V_0}{\pi} \sum_{n=1,3,5,\dots}^{\infty} \frac{1}{n} e^{-n\pi x/a} \sin(n\pi y/a)$$


3.11 The $X(x)$ equation in this problem involves the "positive constant" solutions:
 $A \sinh(kx) + B \cosh(kx)$

What do the boundary conditions say about the coefficients A and B above?

A) $A=0$ (pure \cosh)
 B) $B=0$ (pure \sinh)
 C) Neither: you should rewrite this in terms of $A' e^{kx} + B' e^{-kx}$!
 D) Other/not sure?

