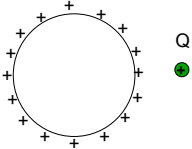


2.29
alt

We place a charge Q just outside an insulating, spherical shell (*fixing* all surface charges uniformly around the sphere)

What is the electric field *inside* the sphere?

A: 0 everywhere inside
 B: non-zero everywhere in the sphere
 C: Something else
 D: Not enough info given

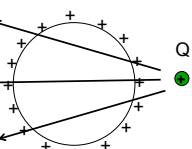


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What is the electric field *inside* the sphere?

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Click only when you are done with the yellow sheet:

What is the answer to the last question:
 iv) Where is this E-field's divergence zero?

A) $\text{div}(E)=0$ everywhere
 B) $\text{div}(E)=0$ Nowhere
 C) $\text{div}(E)=0$ everywhere OUTSIDE the pipe
 D) $\text{div}(E)=0$ on the surface of the pipe only
 E) Something else!

I would like to find the E field directly above the center of a uniform (finite) disk.
 Can we use Gauss' law with the Gaussian surface depicted below?

Gaussian surface:
 Flat, massive, uniform disk

A) Yes, and it would be pretty easy/elegant...
 B) Yes, but it's not easy.
 C) No. Gauss' law applies, but it can not be used here to compute E directly.
 D) No, Gauss' law would not even apply in this case⁴

Which is true about $|\mathbf{E}|$ at points on the *imaginary dashed triangle*?

(I) (II)
 Uniform Charge $+3Q$

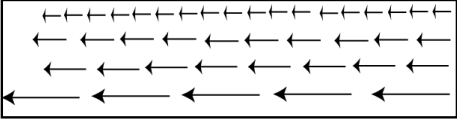
A. $|\mathbf{E}|$ same everywhere (uniform) in (I) ONLY
 B. $|\mathbf{E}|$ uniform in (II) ONLY
 C. Uniform in both, but *different* in cases I & II
 D. Uniform in both, and same in cases I & II.
 E. $|\mathbf{E}|$ varies from point to point in both cases

2.27
 A cubical non-conducting *shell* has a **uniform** positive charge density on its surface. (There are no other charges around)
 What is the field inside the box?

A: $\mathbf{E}=0$ everywhere inside
 B: \mathbf{E} is non-zero everywhere inside
 C: $\mathbf{E}=0$ only at the very center, but non-zero elsewhere inside.
 D: Not enough info given

1.7c

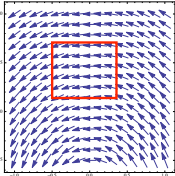
What is the curl of this vector field, in the region shown below?



A. non-zero everywhere
 B. Non-zero at a limited set of points
 C. zero curl everywhere
 D. We need a formula to decide for sure

1.8

What is the curl of this vector field, \mathbf{V} in the region shown below?

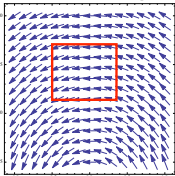


$\vec{V} = c \hat{\phi}$

A. non-zero everywhere
 B. Zero at some points, non-zero others
 C. zero curl everywhere shown

1.8

What is the curl of this vector field, \mathbf{V} in the region shown below?



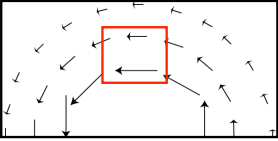
$\vec{V} = c \hat{\phi}$

$$\nabla \times \vec{V} = \left[\frac{1}{s} \frac{\partial v_z}{\partial \phi} - \frac{\partial v_\phi}{\partial z} \right] \hat{s}$$

$$+ \left[\frac{\partial v_s}{\partial z} - \frac{\partial v_z}{\partial s} \right] \hat{\phi} + \frac{1}{s} \left[\frac{\partial (s v_\phi)}{\partial s} - \frac{\partial v_s}{\partial \phi} \right] \hat{z}$$

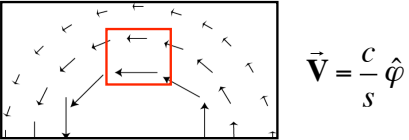
A. non-zero everywhere
 B. Zero at some points, non-zero others
 C. zero curl everywhere shown

^{1.8} What is the curl of this vector field, in the red region shown below?



A. non-zero everywhere in the box
 B. Non-zero at a limited set of points
 C. zero curl everywhere shown
 D. We need a formula to decide for sure

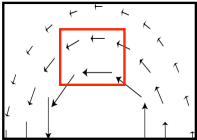
^{1.8} What is the curl of this vector field, in the red region shown below?



$\vec{V} = \frac{c}{s} \hat{\phi}$

A. non-zero everywhere in the box
 B. Non-zero at a limited set of points
 C. zero curl everywhere shown

^{1.8} What is the curl of this vector field, in the red region shown below?



$\vec{V} = \frac{c}{s} \hat{\phi}$

$\nabla \times \vec{V} = \left[\frac{1}{s} \frac{\partial v_z}{\partial \phi} - \frac{\partial v_\phi}{\partial z} \right] \hat{s}$
 $+ \left[\frac{\partial v_s}{\partial z} - \frac{\partial v_z}{\partial s} \right] \hat{\phi} + \frac{1}{s} \left[\frac{\partial (sv_\phi)}{\partial s} - \frac{\partial v_s}{\partial \phi} \right] \hat{z}$

A. non-zero everywhere in the box
 B. Non-zero at a limited set of points
 C. zero curl everywhere shown

2.43b/1.7b

Which of the following *could* be a static physical E-field in a small region?

I

II

A) Only I B) Only II
 C) Both D) Neither
 E) Cannot answer without further info

Why is $\int \vec{E} \cdot d\vec{l} = 0$ in electrostatics?

a) Because $\nabla \times \vec{E} = 0$
 b) Because E is a conservative field
 c) Because the potential between two points is independent of the path
 d) All of the above
 e) NONE of the above - it's not true!

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho(\mathbf{r}') \hat{\mathfrak{R}}}{\mathfrak{R}^2} d\tau'$$

$$\hat{\mathfrak{R}} = \mathbf{r} - \mathbf{r}' = (x - x', y - y', z - z')$$

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho(\mathbf{r}') \hat{\mathfrak{R}}}{\mathfrak{R}^2} d\tau'$$

(with $\vec{\mathfrak{R}} = \mathbf{r} - \mathbf{r}' = (x - x', y - y', z - z')$)

It is also true that $\frac{\hat{\mathfrak{R}}}{\mathfrak{R}^2} = -\nabla \frac{1}{|\mathfrak{R}|}$

where $\nabla = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right)$

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho(\mathbf{r}') \hat{\mathfrak{R}}}{\mathfrak{R}^2} d\tau'$$

(with $\vec{\mathfrak{R}} = \mathbf{r} - \mathbf{r}' = (x - x', y - y', z - z')$)

It is also true that $\frac{\hat{\mathfrak{R}}}{\mathfrak{R}^2} = -\nabla \frac{1}{|\mathfrak{R}|}$

where $\nabla = \left(\frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right)$

Question: is the following mathematically ok?

$$\mathbf{E}(\mathbf{r}) = \frac{1}{4\pi\epsilon_0} \iiint \rho(\mathbf{r}') \left(-\nabla \frac{1}{|\mathfrak{R}|} \right) d\tau' = -\nabla \frac{1}{4\pi\epsilon_0} \iiint \frac{\rho(\mathbf{r}')}{|\mathfrak{R}|} d\tau'$$

A) Yes B) No C) ???

243

Which of the following electrostatic fields could exist in a finite region of space that contains no charges?

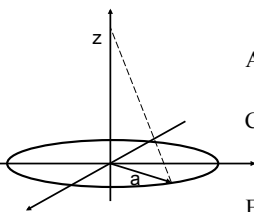
A) $Axyz(\hat{i} + \hat{j})$

B) $A(xz\hat{i} - xz\hat{j})$

C) $A(-xy\hat{j} + xz\hat{k})$

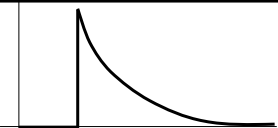
D) None of these

A uniformly charged ring, in the xy plane, centered on the origin, has radius a and total charge Q . $V(r = \infty) = 0$.
 What is the voltage at z on the z-axis?



A) $\frac{kQ}{a}$ B) $\frac{kQ}{z}$
 C) $\frac{kQ}{\sqrt{a^2 + z^2}}$ D) $\frac{kQ}{a^2 + z^2}$
 E) None of these

244



Could this be a plot of $|E|(r)$? Or $V(r)$?
 (for SOME physical situation?)

A) Could be $E(r)$, or $V(r)$
 B) Could be $E(r)$, but can't be $V(r)$
 C) Can't be $E(r)$, could be $V(r)$
 D) Can't be either E) ???

245

Given a sphere with uniform surface charge density σ what can you say about the potential V *inside* this sphere?
 (Assume as usual, $V(\infty)=0$)

A) $V=0$ everywhere inside
 B) $V =$ non-zero constant everywhere inside
 C) V must vary with position, but is zero at the center.
 D) None of these.

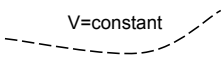
The voltage is zero at a point in space.

You can conclude that :

- A) The E-field is zero at that point.
- B) B) The E-field is non-zero at that point
- C) You can conclude nothing at all about the E-field at that point

The voltage is constant everywhere along a line in space.

$V = \text{constant}$



You can conclude that :

- A) The E-field has constant magnitude along that line.
- B) The E-field is zero along that line.
- C) You can conclude nothing at all about the magnitude of **E** along that line.
