A neutral, infinite current sheet, **K**, flows in the *x-y* plane, in the +*y* direction. To the right of the *x-y* plane, according to what you know from Phys 3310, the **E** and **B** field directions are:

r1















A) Yes, and I can defend my answer

r7

- B) Yes, but I cannot explain why I believe this
- C) No, and I can defend my answer
- D) No, but I cannot explain why I believe this
- E) It depends on the reference frame of the observer!







You are FAR from a small oscillating dipole,  $I(t) = -q_0 \omega \sin \omega t$ and you want to compute the vector potential:  $\rightarrow$  $\vec{A}(\vec{r},t) = \frac{\mu_0}{4}$  $4\pi$  $\frac{\vec{J}(\vec{r}',t_R)}{|\vec{r}-\vec{r}'|}$ |  $\iiint \frac{\vec{J}(\vec{r}',t_R)}{|\vec{r}-\vec{r}'|} d^3 \vec{r}'$ , with  $t_R = t - \frac{|\vec{r}-\vec{r}'|}{c}$ *c* What is the leading order approximate expression for **A**(**r**, t) ? A)  $\frac{\mu_0}{4}$  $4\pi$  $-q_0 \omega \sin \omega t$ *r z*ˆ *B*)  $\frac{\mu_0}{4}$  $4\pi$  $-q_0 \omega \sin \omega (t - r/c)$ *r z*ˆ  $C)\frac{\mu_0}{4}$  $4\pi$  $d \frac{-q_0 \omega \sin \omega t}{ }$ *r z*ˆ *D*)  $\frac{\mu_0}{4}$  $4\pi$  $d \frac{-q_0 \omega \sin \omega (t - r/c)}{r}$ *r z*ˆ E) Something else?! **r**   $\begin{matrix} 1 \\ 0 \\ 1 \end{matrix}$ 

What is 
$$
\hat{z}
$$
, in spherical coordinates?  
\nA)  $\cos\theta \hat{r}$   
\nB)  $\sin\theta \hat{r} + \cos\theta \hat{\theta}$   
\nC)  $\cos\theta \hat{r} + \sin\theta \hat{\theta}$   
\nD)  $\cos\theta \hat{r} - \sin\theta \hat{\theta}$   
\nE) Something else?  
\nThus,  $\vec{A}(r,t) = \frac{\mu_0}{4\pi} d \frac{-q_0 \omega \sin\omega(t - r/c)}{r} \left(\cos\theta \hat{r} - \sin\theta \hat{\theta}\right)$   
\n $\vec{B}(r,t) = \nabla \times \vec{A}(r,t) = \frac{-\mu_0 p_0 \omega^2}{4\pi} \sin\theta \frac{\cos\omega(t - r/c)}{rc} \hat{\phi}$ 

r13  $B(r,t) \hat{\varphi} = \frac{-\mu_0 p_0 \omega^2}{4}$  $4\pi$  $\sin \theta \frac{\cos \omega (t - r/c)}{}$ *rc*  $\hat{\varphi}$ For an oscillating dipole,  $p=p_0 \cos(\omega t)$ , we worked out last class (assuming  $r \gg \lambda \gg d$ ) that: To think about (be prepared to discuss): In what ways is it like (and not like) our familiar free-space "traveling plane wave"? Which of the following describes the E field? A)  $\overline{\phantom{a}}$  $\vec{E} = cB \hat{\phi}$  B)  $\vec{E}$ = cB  $\hat{\theta}$  $\theta$  C)  $\rightarrow$  $\hat{E} = cB \hat{r}$  D)  $\rightarrow$  $E = cB \hat{z}$ E) None of these/something else?

r14 Total power radiated by a small electric dipole is  $=\frac{\mu_0 p_0^2 \omega^4}{2}$  $6\pi c$  $\cos^2 \omega(t - r/c)$ What is the time averaged power? What is the time averaged intensity at distance "r"?  $P = \int \frac{\mu_0 p_0^2 \omega^4}{(16 \pi^2)^2}$  $\iint \frac{\mu_0 P_0 \omega}{(16\pi^2) cr^2} \sin^2 \theta \cos^2 \omega (t - r/c) da$ 

<sup>15</sup> The time averaged Poynting vector (far from a small electric dipole) is approximately:

$$
\left\langle \vec{S} \right\rangle = \frac{\mu_0 p_0^2 \omega^4}{32\pi c r^2} \sin^2 \theta \ \hat{r}
$$

Describe this energy flow in words, pictures, or graph.

$$
R_{rad} \equiv \frac{P_{ave}}{I_{rms}^2}
$$
  
Recall, we found  $I = -q_0 \omega \cos(\omega t)$ .  
So what is  $I_{rms}$ ?  
A)  $q_0 \omega$  B)  $q_0 \omega/2$  C)  $q_0 \omega/\sqrt{2}$  D)  $\sqrt{2}q_0 \omega$   
E) None of these/sometimes else?  

$$
R_{rad} = \sqrt{\frac{\mu_0}{\epsilon_0}} \frac{2\pi}{3} (d/\lambda)^2
$$

r17 We're interested in power radiated by a wiggling charge. 1) What physics variables might this power possibly depend on? (Come up with a complete, but not OVERcomplete list) 2) If your list of variables was  $v_1$ ,  $v_2$ , etc..., we're saying  $P = V_1^a V_2^b ...$ Look at the SI UNITS of all quantities involved. I claim you should be able to uniquely figure out those powers (a,b, …) ! Try it.

Hint: My list of variables is q, a, c, and  $\mu_0$ 

The TOTAL power of an accelerating (non-relativistic) charge is called **Larmor's formula**.

It depends on c,  $\mu_0$  a (acceleration) and q (charge).

So I presume that means  $P = c^A \mu_0^B a^C q^D$ (!? It's at least a plausible guess…)

Figure out the *constants* A-D in that formula, without using any physics beyond units! (This is *dimensional analysis)* 

Note:  $[P]$  = Watts = kg m<sup>2</sup>/s<sup>3</sup>,  $[\mu_0] = N/A^2 = kq \ m/C^2$ 

r18



