

Snell's law

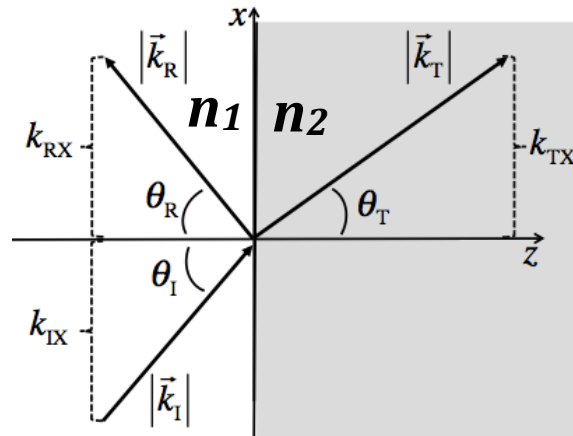
A. An EM plane wave traveling in the x - z plane (i.e., $\vec{k}_1 = k_{1x}\hat{x} + k_{1z}\hat{z}$) is incident on a material at an angle θ_1 relative to the z -axis:

$$\vec{E}_I(\vec{r}, t) = \vec{E}_I \exp\left[i(\vec{k}_1 \cdot \vec{r} - \omega t)\right]$$

$$\vec{E}_R(\vec{r}, t) = \vec{E}_R \exp\left[i(\vec{k}_R \cdot \vec{r} - \omega t)\right]$$

$$\vec{E}_T(\vec{r}, t) = \vec{E}_T \exp\left[i(\vec{k}_T \cdot \vec{r} - \omega t)\right]$$

We argued from continuity of $E_{//}$ that $\vec{k}_I \cdot \vec{r} = \vec{k}_R \cdot \vec{r} = \vec{k}_T \cdot \vec{r}$ for any \mathbf{r} in the $z=0$ plane. (E.g. $\vec{r} = \hat{x}$)



I got briefly hung up on the

algebra at the board last class, so let's work it out again:

Derive the following ratio for incident and transmitted wave angles.

(Express it first in terms of magnitudes of \mathbf{k} vectors, but then write it simply in terms of the index of refraction in the two regions, n_1 and n_2)

$$\frac{\sin \theta_T}{\sin \theta_I} =$$