

Charge conservation in metals: dynamics

Suppose you dump some charge into the bulk of a metal at $t=0$.
What happens next?

1) Start with the continuity equation:

$$\nabla \cdot \vec{J} =$$

2) Use Ohm's law for the current density, to get

$$\nabla \cdot \underline{\hspace{2cm}} =$$

3) Assume the material is homogeneous (pull constants out of the derivative) so...

$$\underline{\hspace{1cm}} \nabla \cdot \underline{\hspace{2cm}} =$$

4) Apply Gauss' law in that last equation to simplify it

(We can't automatically assume $\rho=0$ inside a metal if we just DUMPED charge into it!)

5) You should have a first order differential equation. Can you solve it by inspection?

What do you conclude about the charge density inside the metal as time goes by?
(What is happening physically?)