

The electric field for a plane wave is given by:

$$\mathbf{E}(\mathbf{r}, t) = \vec{E}_0 e^{i(\vec{\mathbf{k}} \cdot \vec{\mathbf{r}} - \omega t)}$$

Suppose  $\mathbf{E}_0$  points in the +x direction.  
Which direction is this wave moving?

- A) The x direction.
- B) The radial ( $\mathbf{r}$ ) direction
- C) A direction *perpendicular* to both  $\mathbf{k}$  and  $\mathbf{x}$
- D) The  $\mathbf{k}$  direction
- E) None of these/MORE than one of these/???

Think about the first of Maxwell's Equations (Gauss's Law) in vacuum:  $\vec{\nabla} \cdot \vec{E} = 0$

Try a complex exponential "linearly polarized plane wave":

$$\vec{E}(x, y, z, t) = \vec{E}_0 \exp \left[ i(\vec{k} \cdot \vec{r} - \omega t) \right]$$

Then, Gauss's Law becomes:

$$\text{A) } i\vec{k} \cdot \vec{E}_0 = 0$$

$$\text{C) } i\vec{k} \times \vec{E}_0 = 0$$

$$\text{B) } \vec{k} |\vec{E}_0| = 0$$

$$\text{D) } |i\vec{k}| |\vec{E}_0| = 0$$

E) None of these.

What does this mean, in words?